

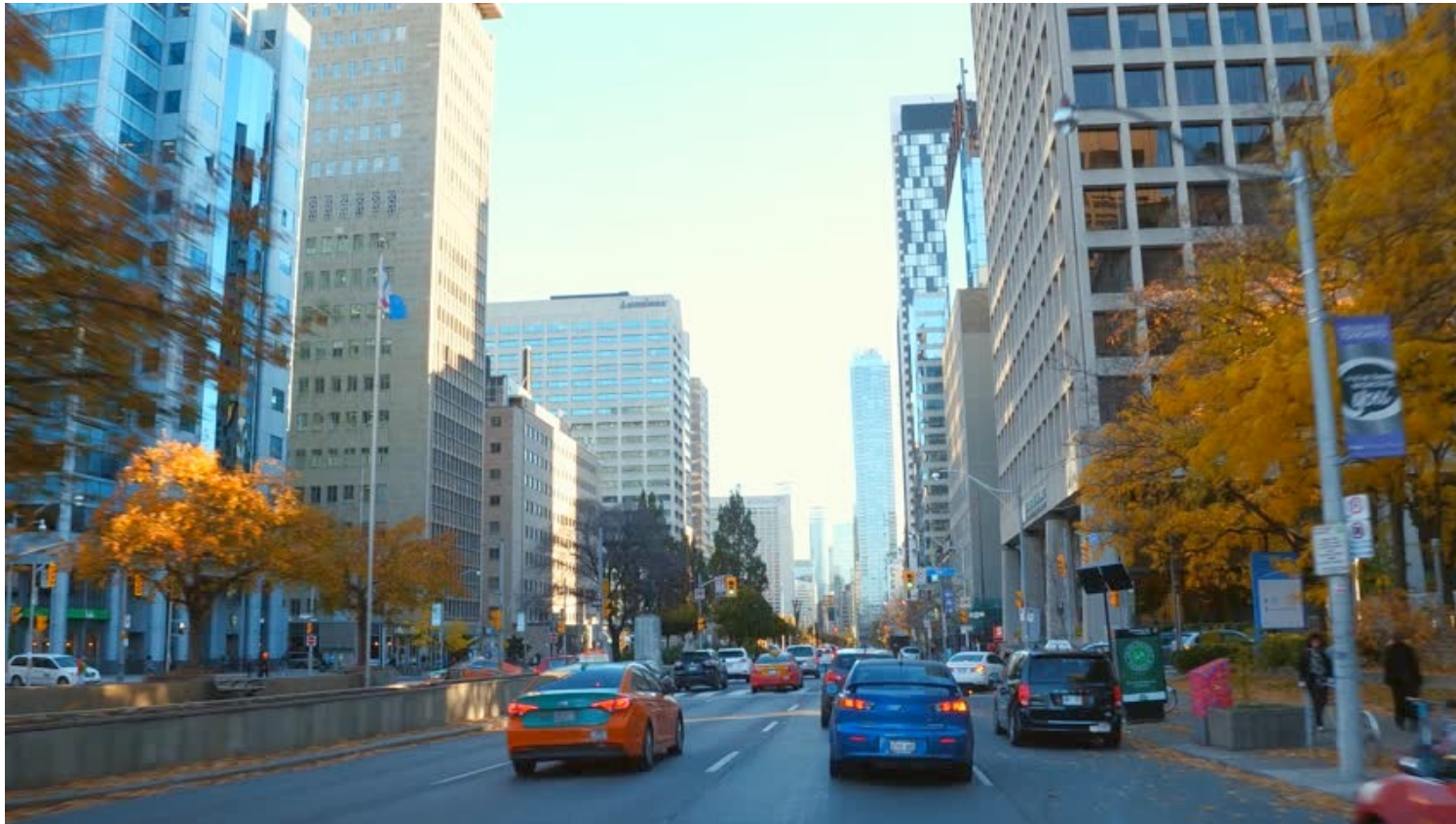
Learning 3D reconstruction in  
underconstrained settings

# 2.5D vs 3D

- 2.5D: Reconstruct only the visible pixels
- 3D: Reconstruct full 3D shapes

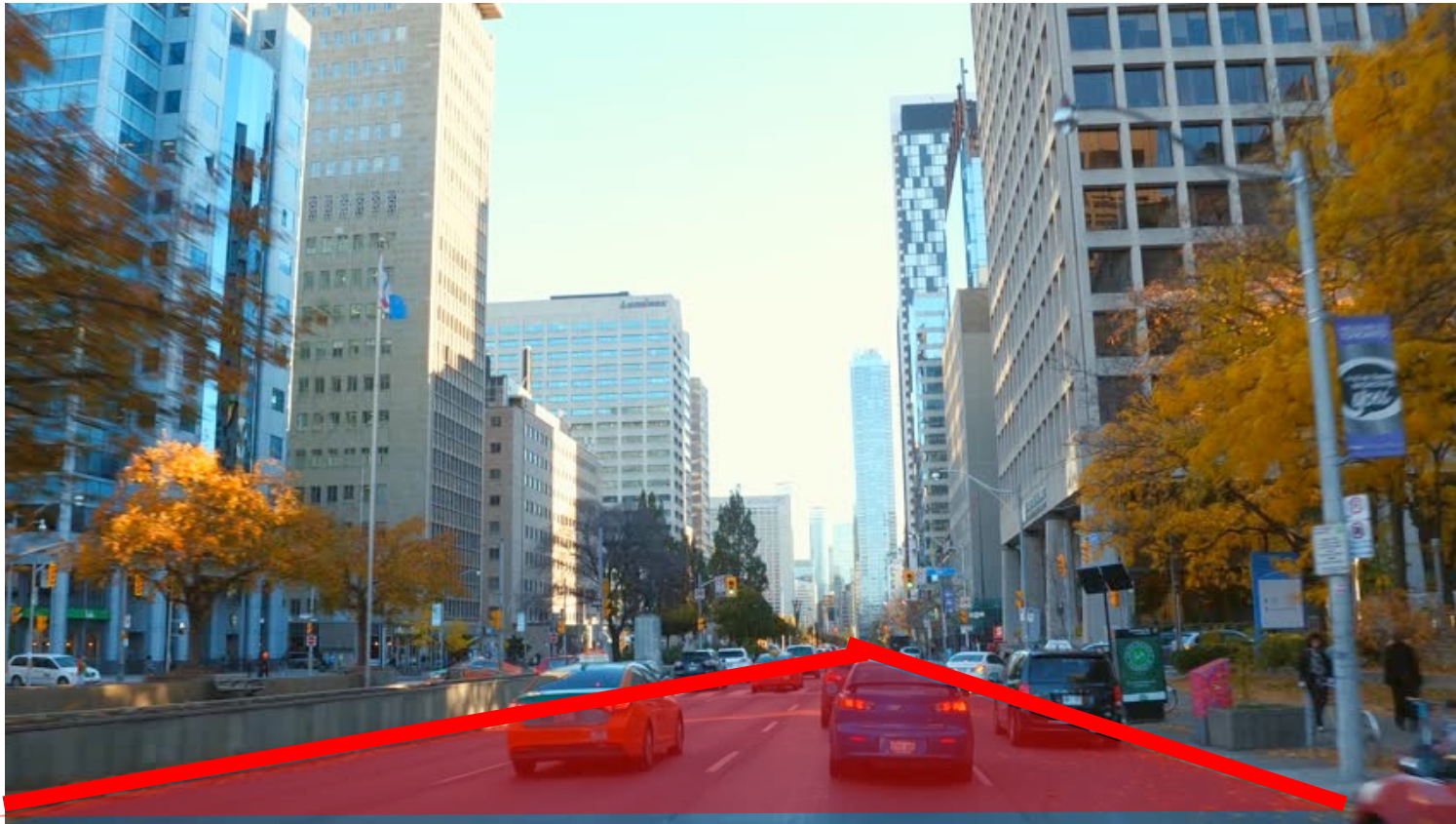
# Estimating depth from a single image

- Why is this even possible?



# Estimating depth from a single image

- Why is this even possible?



Vanishing lines indicate  
plane orientations

# Estimating depth from a single image

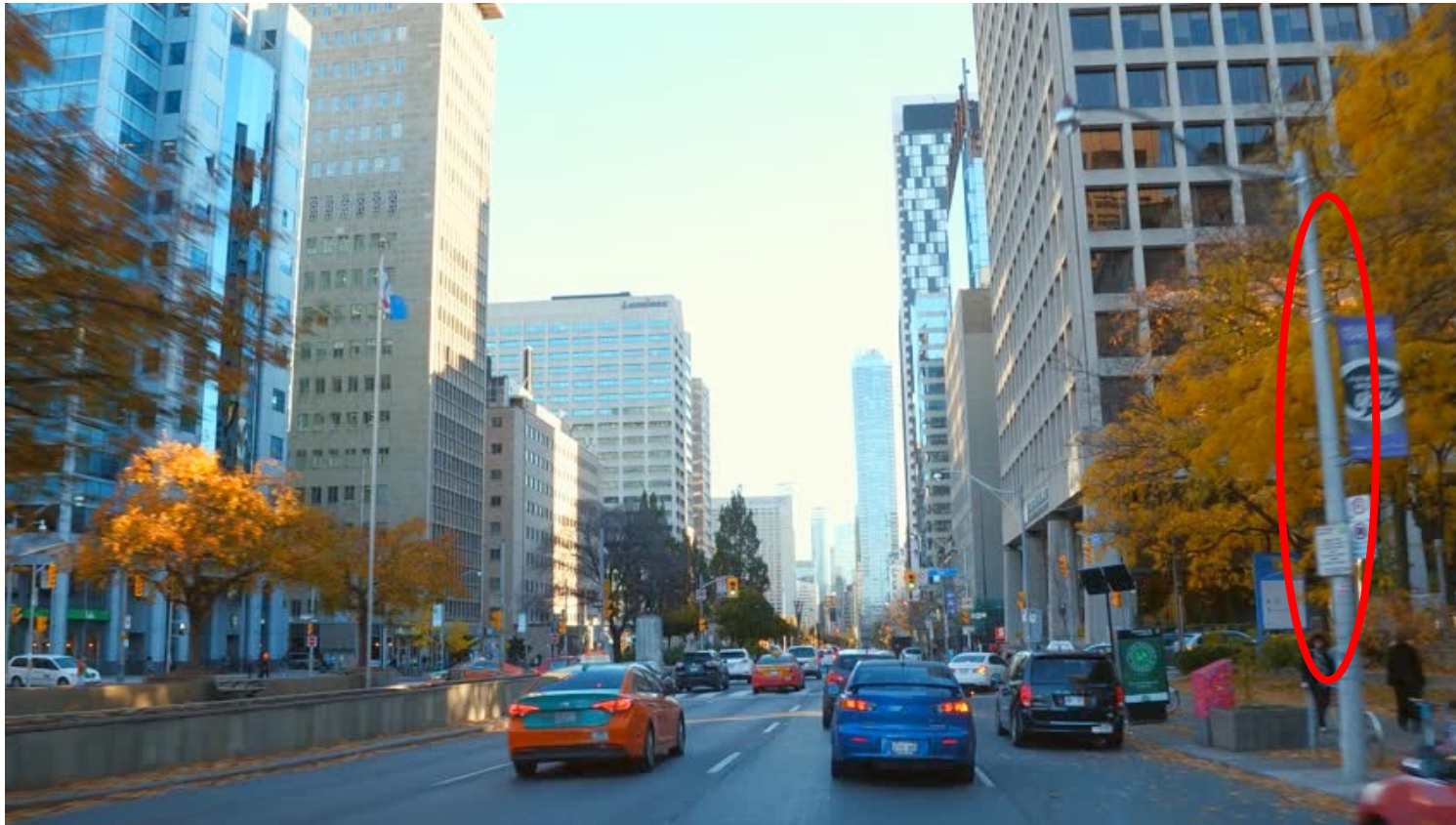
- Why is this even possible?



Apparent object height relative to true height indicates depth

# Estimating depth from a single image

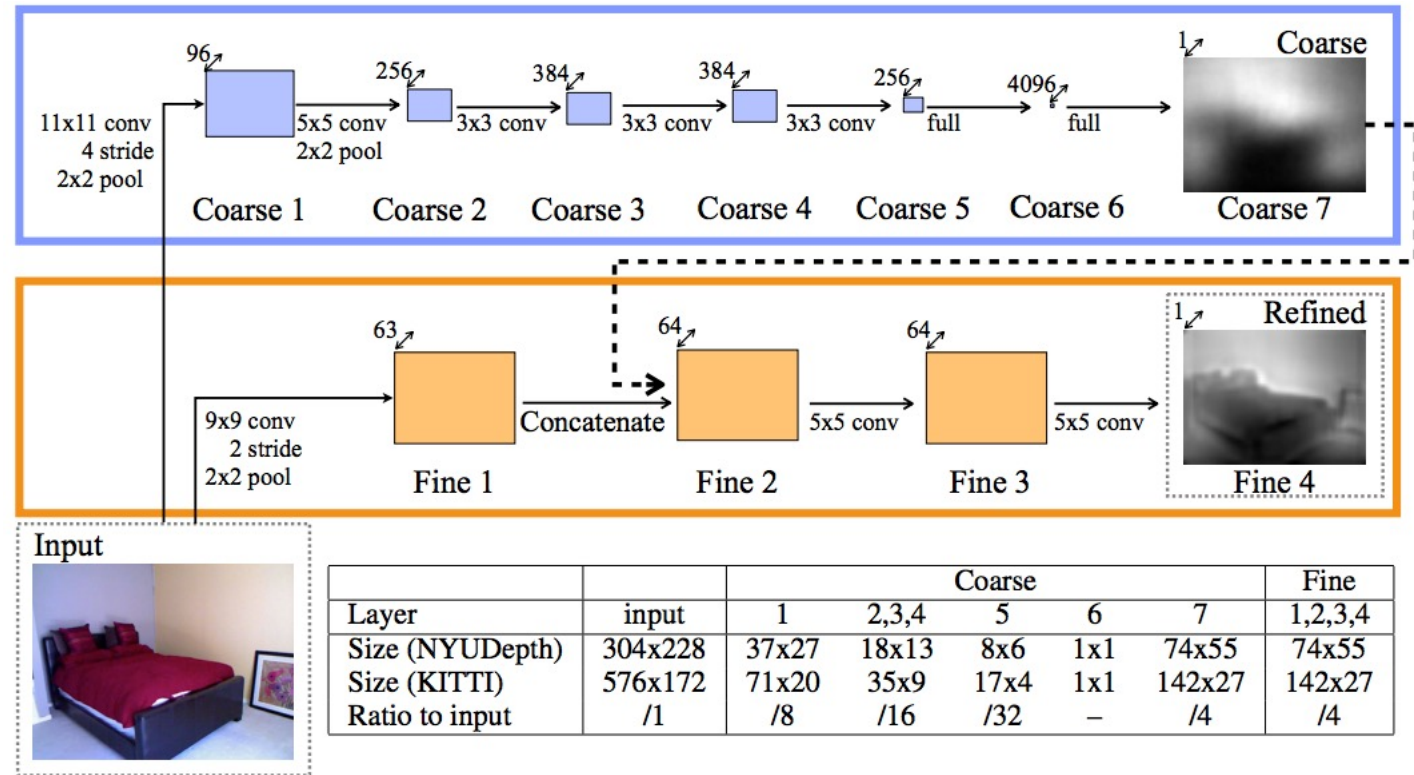
- Why is this even possible?



Occlusion indicates depth ordering

# Estimating depth from a single image

- Image-in, image-out
- Similar to segmentation
- Again, resolution issues



Metric depth is a bad target





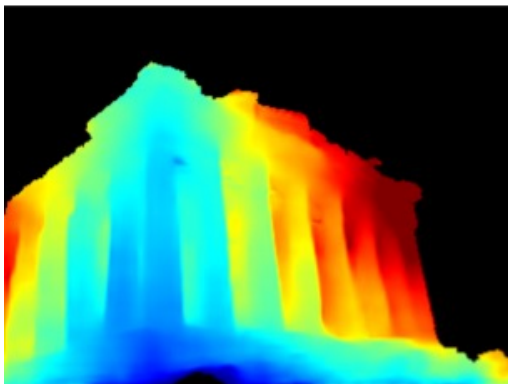
# Metric depth is a bad target

- Only relative depths matter
- Only logarithmic scales matter

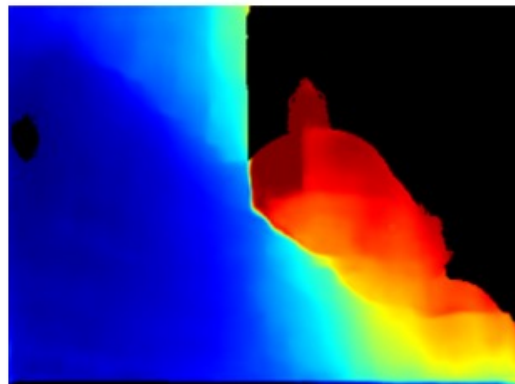
$$D(y, y^*) = \frac{1}{n^2} \sum_{i,j} ((\log y_i - \log y_j) - (\log y_i^* - \log y_j^*))^2$$

# Depth estimation today

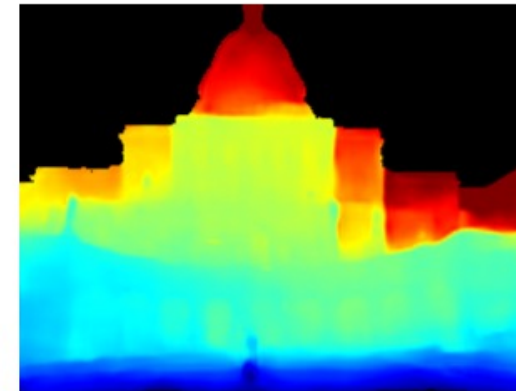
- MegaDepth, learnt from large SfM models



**Parthenon, Athens**

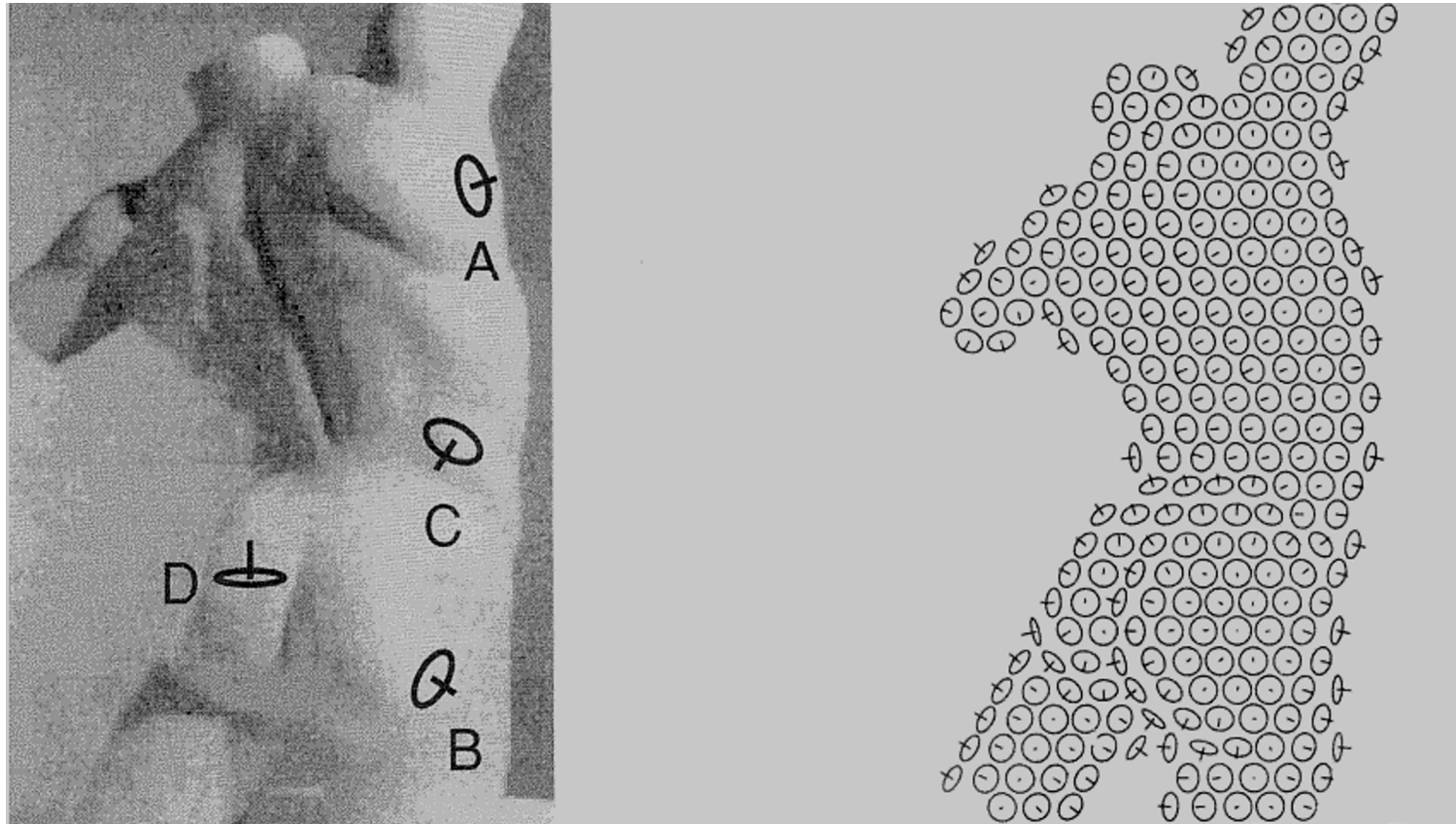


**Florence Cathedral, Florence**

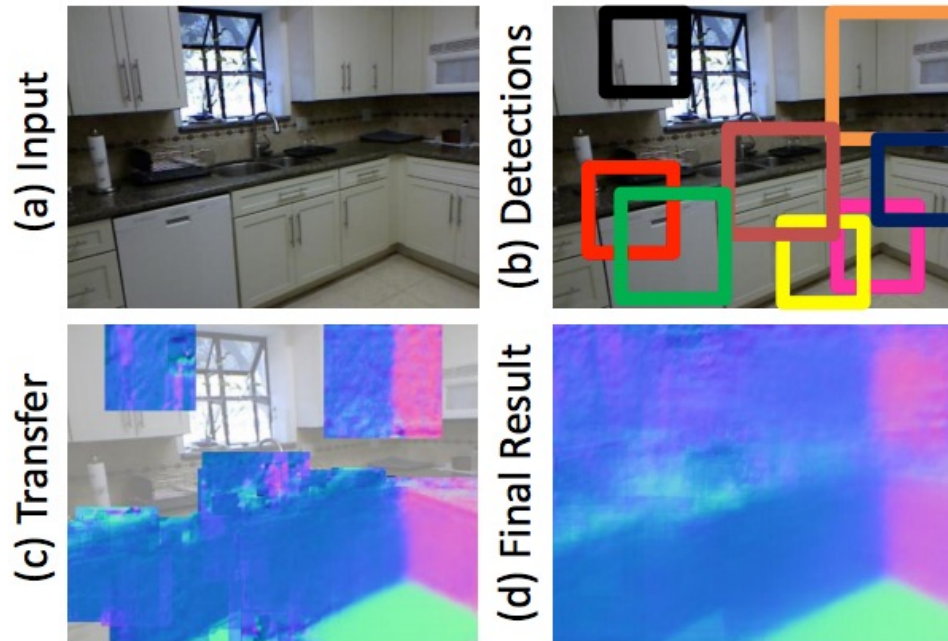


**United States Capitol, D.C.**

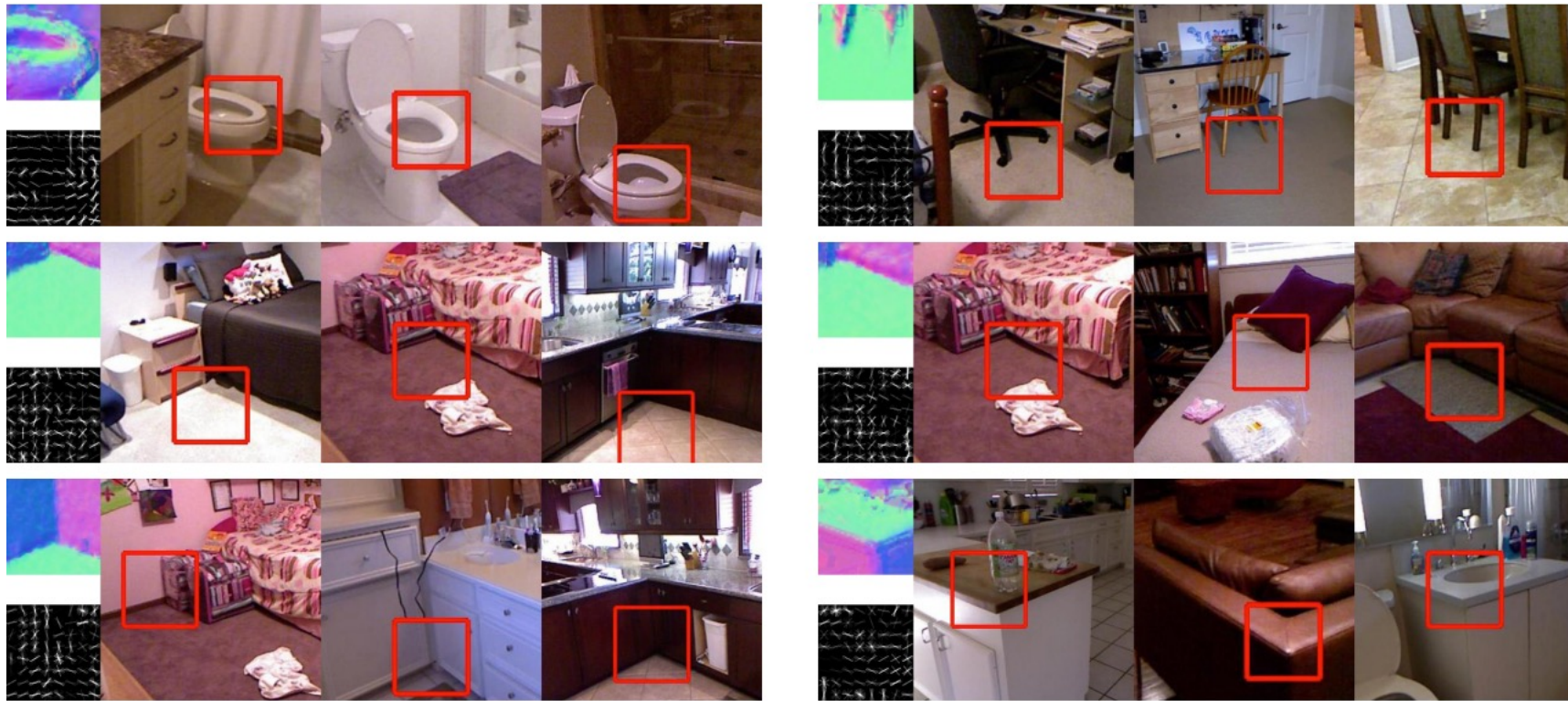
Humans perceive surface normals, not just depth, through a combination of various pictorial cues



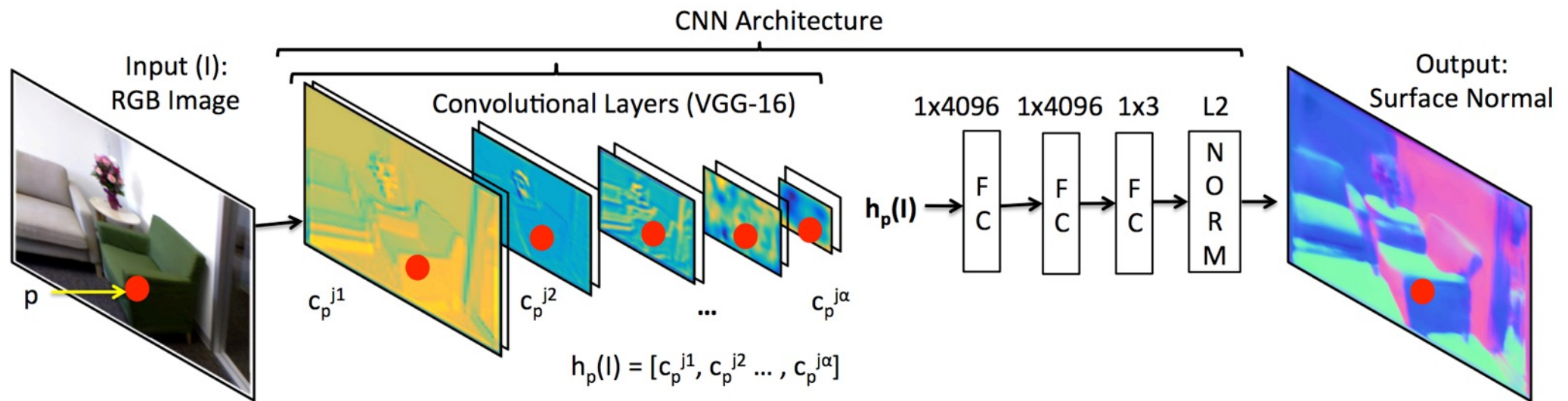
# Estimating normals from a single image



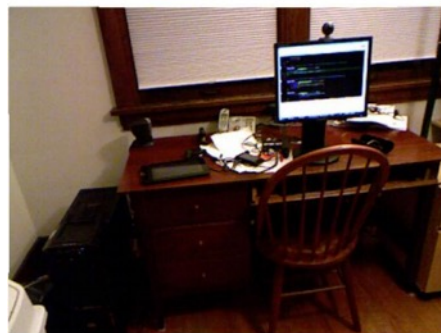
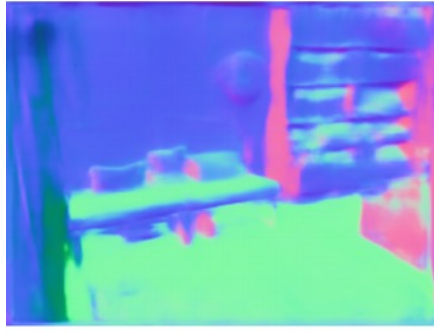
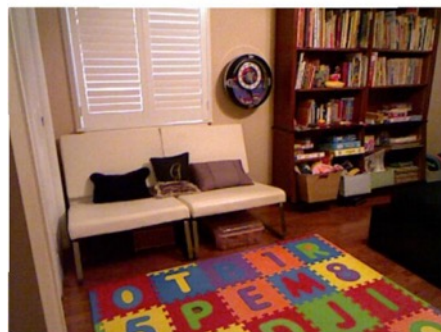
# Estimating normals from a single image



# Estimating normals from a single image



# Estimating normals from a single image



# 2.5D vs 3D prediction

- Predicting depth / surface normals for every pixel is not full reconstruction
  - “2.5D reconstruction”
    - Does not contain parts of the scene that are hidden from view
- Can we do full 3D reconstruction?
- Simpler situation: can we do full 3D reconstruction of isolated objects?



# Shapenet



# Reconstructing 3D shapes from images using machine learning

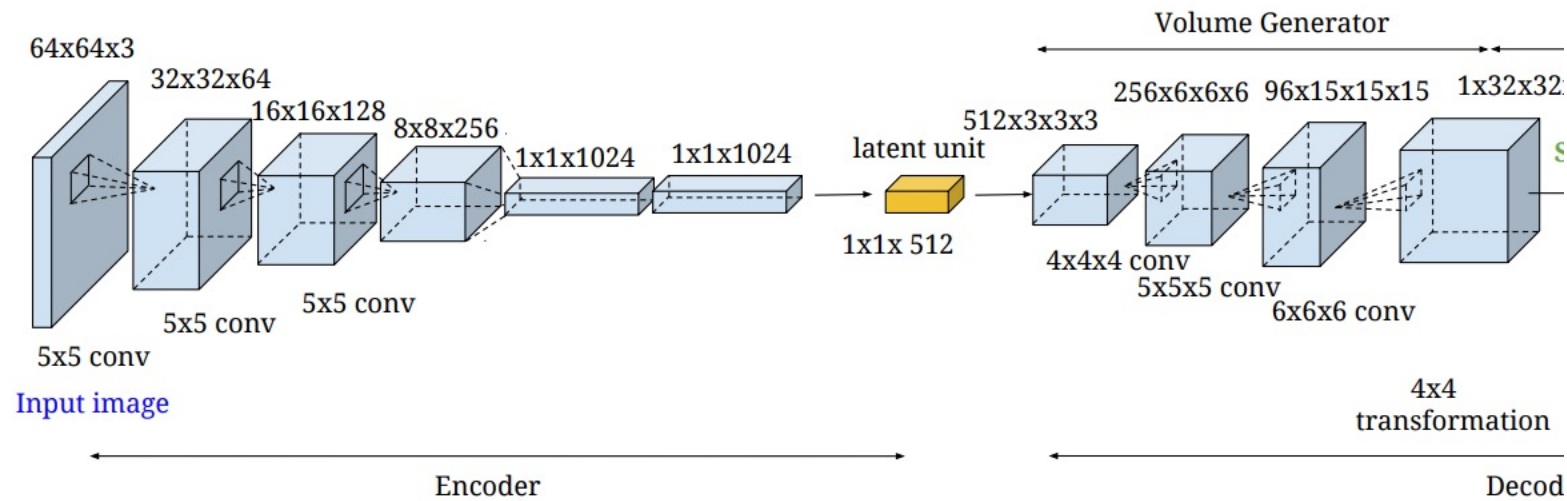
- Input:
  - Single image or multiple images of the same object
- Output:
  - 3D shape
- Representation?

# Representation of 3D shapes

- Voxel grids
  - Discretize volume into grid cells
  - Identify cells that are occupied by object
- Advantages:
  - Easy representation for ML: analog of pixels
- Disadvantages:
  - Memory-inefficient
  - Difficult to capture surface



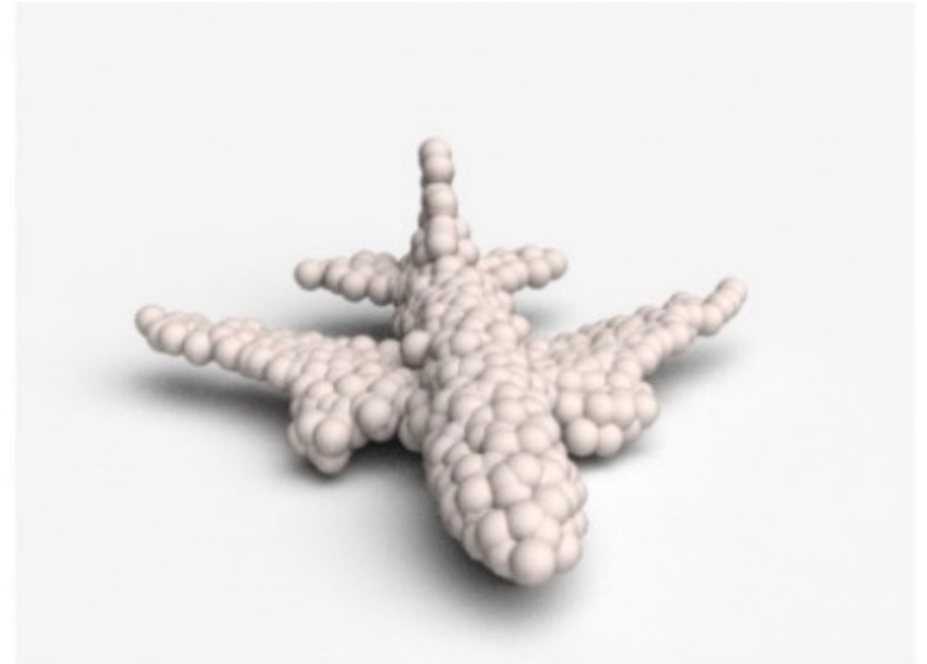
# Architectures for generating voxel grids



1. Choy, Christopher B., et al. "3d-r2n2: A unified approach for single and multi-view 3d object reconstruction." *European conference on computer vision*. Springer, Cham, 2016.
2. Yan, Xinchun, et al. "Perspective transformer nets: Learning single-view 3d object reconstruction without 3d supervision." *Advances in Neural Information Processing Systems*. 2016.

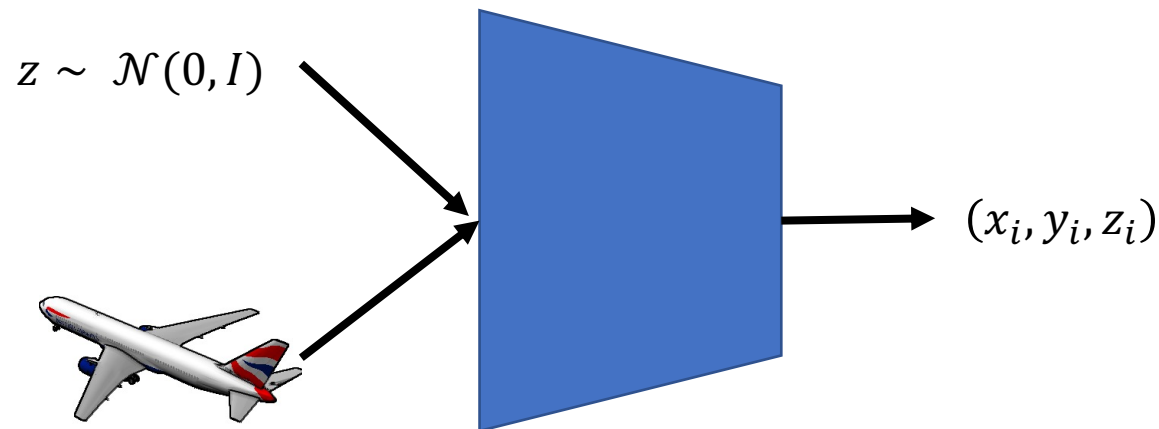
# Representation of 3D shapes

- Point clouds
- Each point lies on surface
- Advantages:
  - Common representation produced by sensors (e.g. LiDAR)
  - Sparse, so memory efficient
- Disadvantages:
  - Difficult output to predict: sets
  - Difficult to extract surface



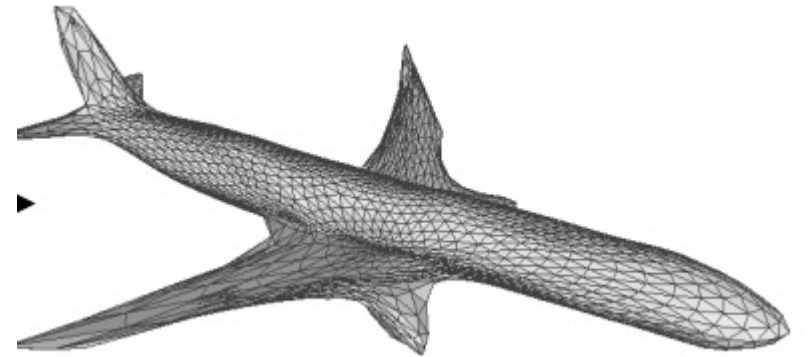
# Architecture for generating point clouds

- Not an established answer
- One possibility: cloud of points = *samples* from an underlying distribution
- Generative modeling



# Representation of 3D shapes

- Meshes
- Advantages
  - Common in graphics
  - Surfaces are triangles in the mesh
  - Sparse representation: memory efficient
  - Can easily encode color, texture, surface normals
- Disadvantages
  - Extremely difficult to predict: graph



# Architecture for producing meshes

- Assume connectivity and faces are the same as that of a sphere
- Move only vertices
- Cannot change *topology* of objects



# Where do we get ground truth?

S H A P E N E T

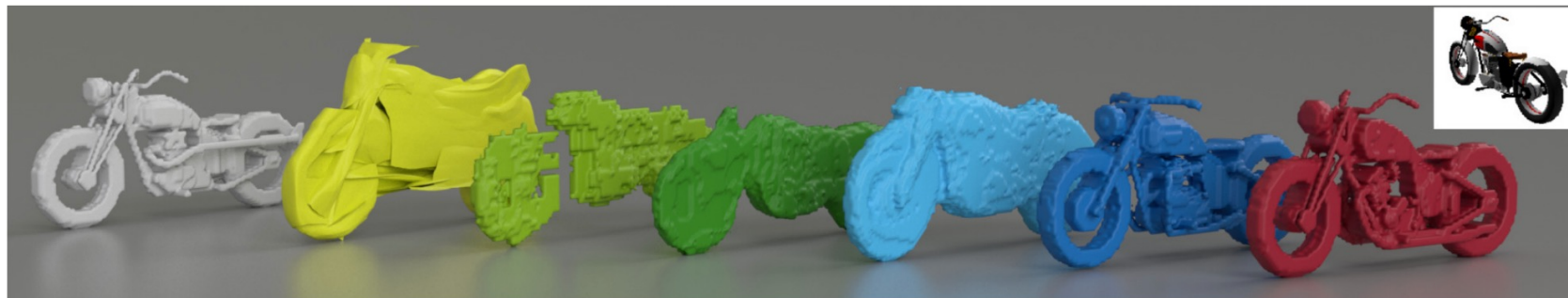
IMAGENET

# Categories	55	1000
# Instances / class	50 – 8000	1300

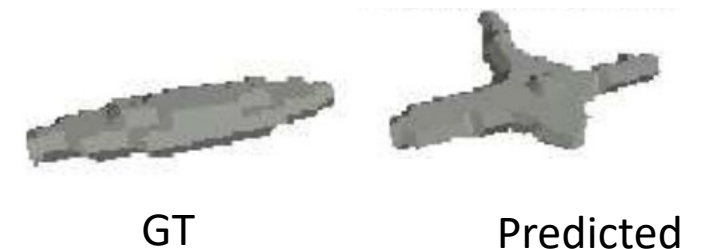
- Models created by 3D artists
- Laser scans
- Structure-from-motion

# Challenges with single view 3D reconstruction

- Clear evidence that SVR networks are mostly doing retrieval



AtlasNet (light green, 0.38) OGN (green, 0.46) Matryoshka Networks (dark green, 0.47) Clustering (light blue, 0.46) Retrieval (dark blue, 0.57)

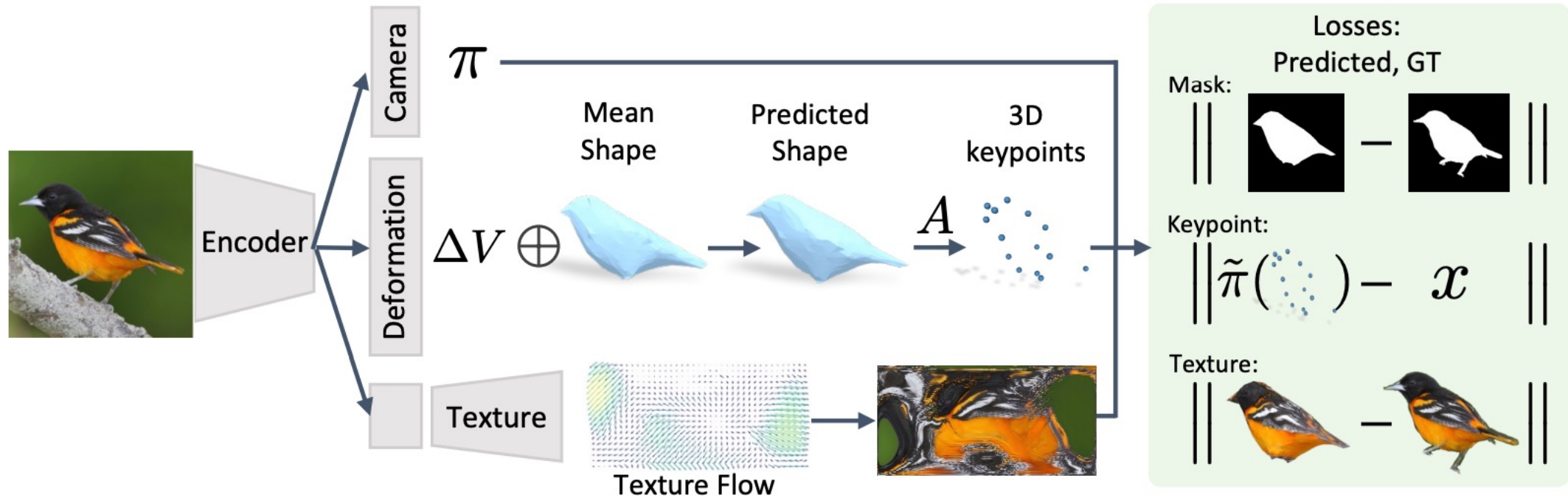


# Supervision?

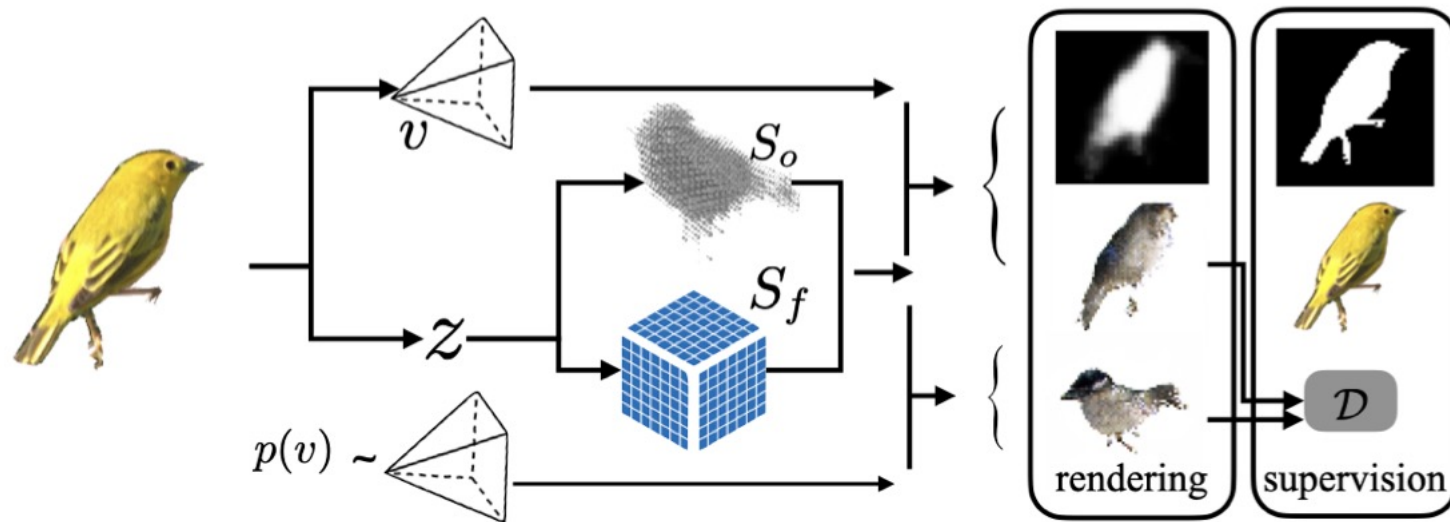
- Fully supervised [1]
- Supervised with multiple views from *known* cameras [2]
  - Predict shape from one image
  - Project it to other views
  - Ensure *photometric consistency*
- Supervised with multiple views from *unknown* cameras [3]
  - Also jointly learn to predict camera pose

1. Choy, Christopher B., et al. "3d-r2n2: A unified approach for single and multi-view 3d object reconstruction." *European conference on computer vision*. Springer, Cham, 2016.
2. Yan, Xinchun, et al. "Perspective transformer nets: Learning single-view 3d object reconstruction without 3d supervision." *Advances in Neural Information Processing Systems*. 2016.
3. Tulsiani, Shubham, et al. "Multi-view supervision for single-view reconstruction via differentiable ray consistency." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2017.

# 3D reconstruction with limited ground truth

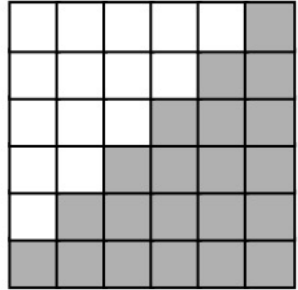


# 3D reconstruction with limited ground truth



Neural representations of shape

# Shape representations



(a) Voxel

- Easy to produce
- Very expensive to store
- Limited resolution

# Implicit vs explicit equations

- Explicit representations of a curve
  - $y = f(x)$
- Implicit representation of a curve
  - $f(x, y) = 0$

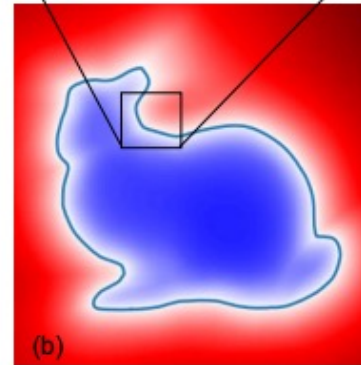
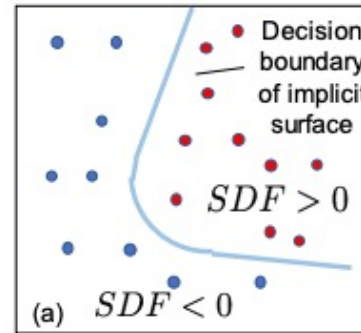


# Implicit representations of 3D shape

- Shape can be represented by the *level sets* of a function  $f: \mathbb{R}^3 \rightarrow \mathbb{R}$
- Occupancy:
  - $f(x, y, z)$  is the probability  $(x, y, z)$  is inside the object
  - Surface is given by  $f(x, y, z) = 0.5$
- Signed distance fields
  - $f(x, y, z)$  is the signed distance of  $(x, y, z)$  from the surface
  - Sign is positive for points inside, negative for points outside
  - Surface is given by  $f(x, y, z) = 0$

# Neural implicit representations

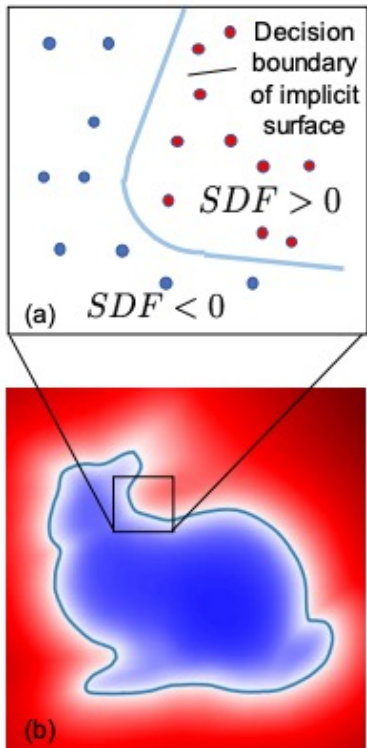
- Traditionally  $f$  is tabular array
- But can approximate with a neural network



Mescheder, Lars, et al. "Occupancy networks: Learning 3d reconstruction in function space." *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*. 2019.

Park, Jeong Joon, et al. "Deepsdf: Learning continuous signed distance functions for shape representation." *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*. 2019.

# Neural Implicit shapes



Park, Jeong Joon, et al. "Deepsdf: Learning continuous signed distance functions for shape representation." *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*. 2019.

Mescheder, Lars, et al. "Occupancy networks: Learning 3d reconstruction in function space." *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*. 2019.

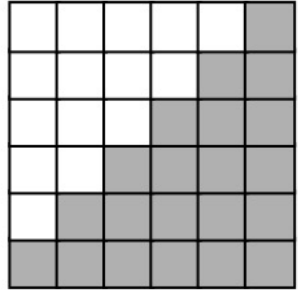
# Representation of 3D shapes

- Implicit shapes
- A shape is a *function* that takes  $(x, y, z)$  as input and produces as output
  - Boolean on whether it is inside shape or not
  - Real value indicating distance from surface ("signed distance functions")
- This *function* can be a *neural network*
- Thus each shape is a *neural network*
- Can additionally take e.g. feature vector as input

Park, Jeong Joon, et al. "DeepSDF: Learning continuous signed distance functions for shape representation." *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*. 2019.

Mescheder, Lars, et al. "Occupancy networks: Learning 3d reconstruction in function space." *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*. 2019.

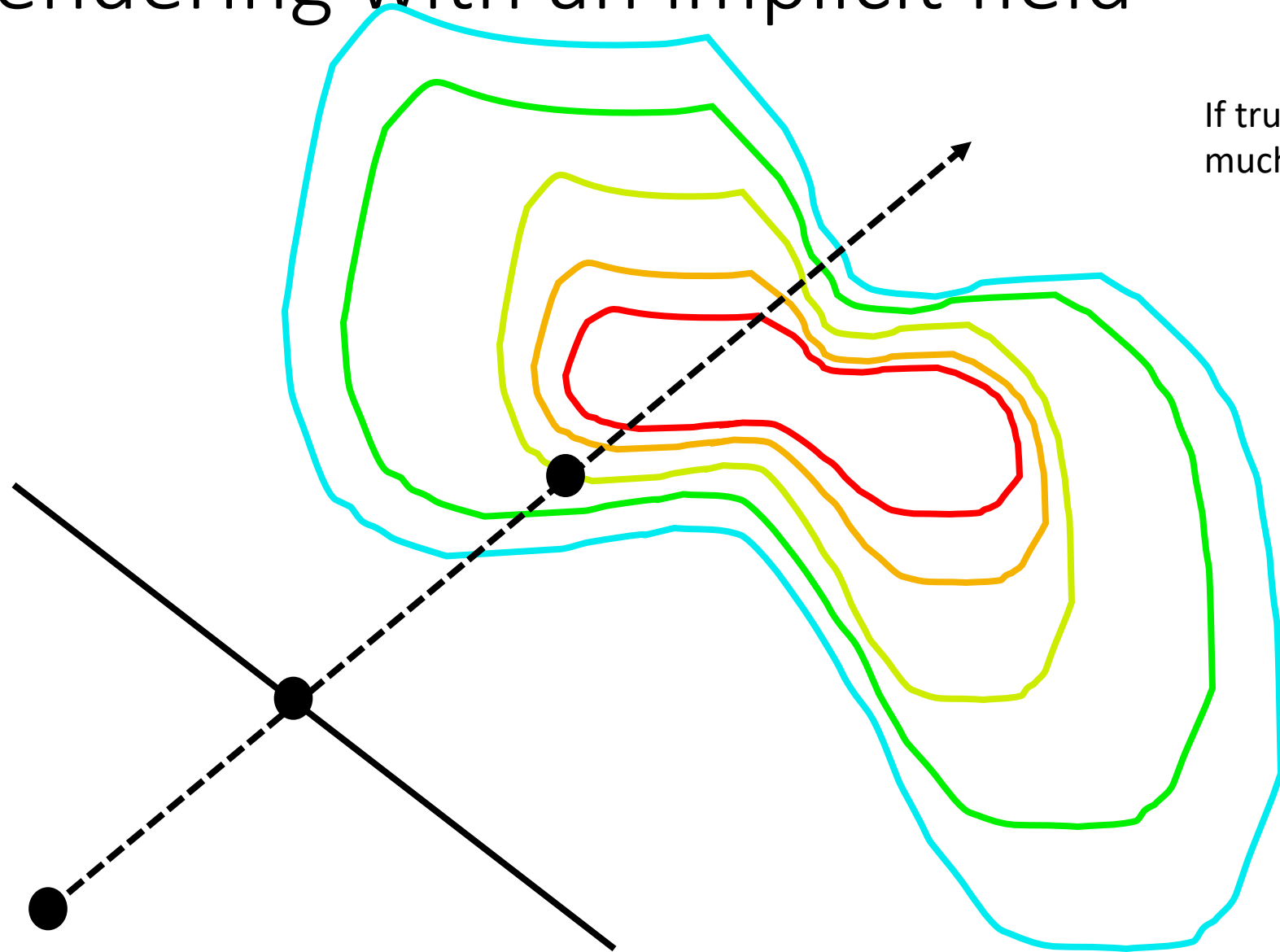
# Shape representations



(a) Voxel

- Easy to produce
- Very expensive to store
- Limited resolution

# Rendering with an implicit field

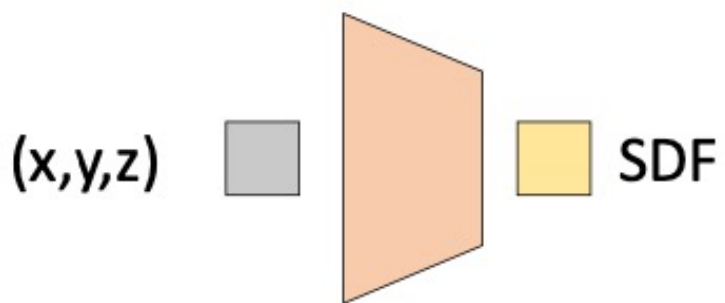


If true SDF, then can perform much faster – Sphere tracing

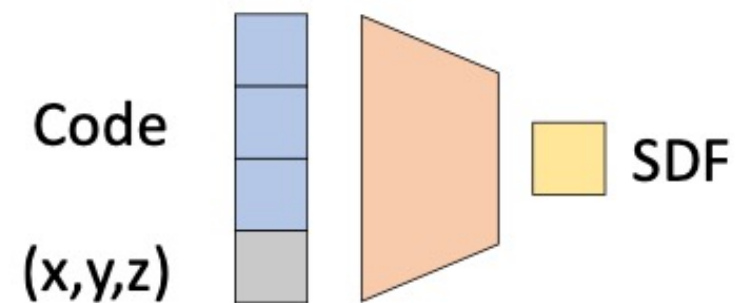
# Generalization with neural fields

- Each neural field captures a particular shape
- Shape is encoded in the weights of the neural network
- How to generalize to new shapes?
  - Latent codes
  - Transfer learning

# Implicit fields with latent codes



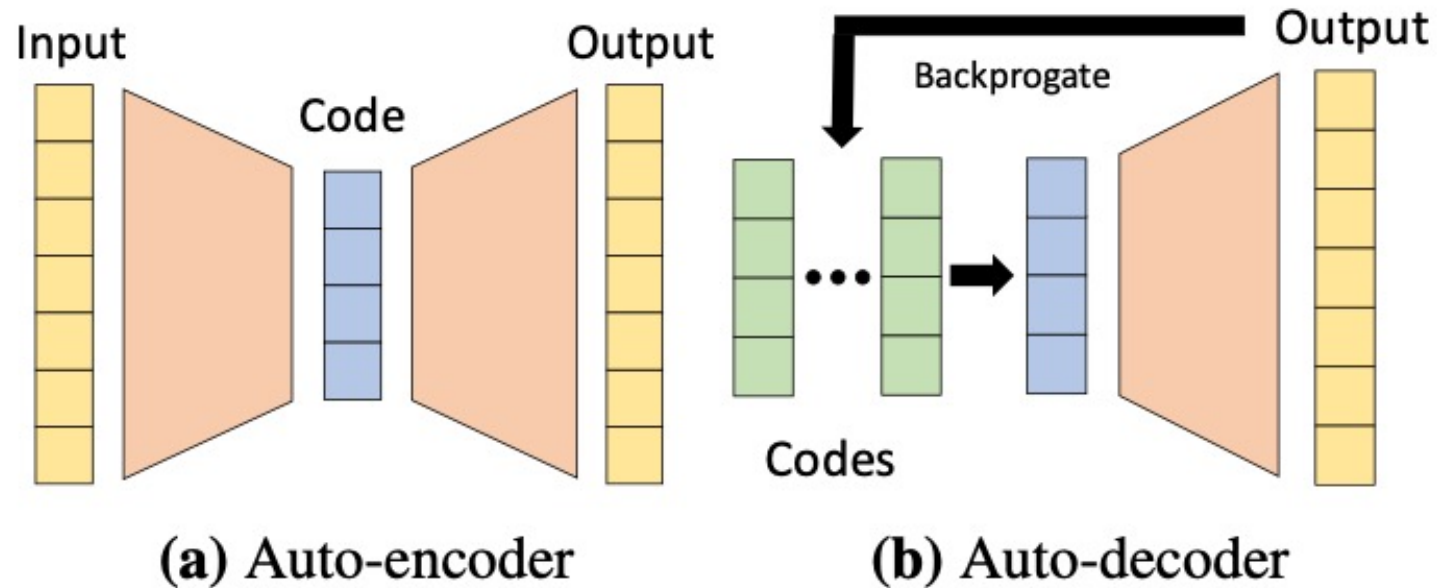
**(a)** Single Shape DeepSDF



**(b)** Coded Shape DeepSDF



# Producing latent codes for input shapes



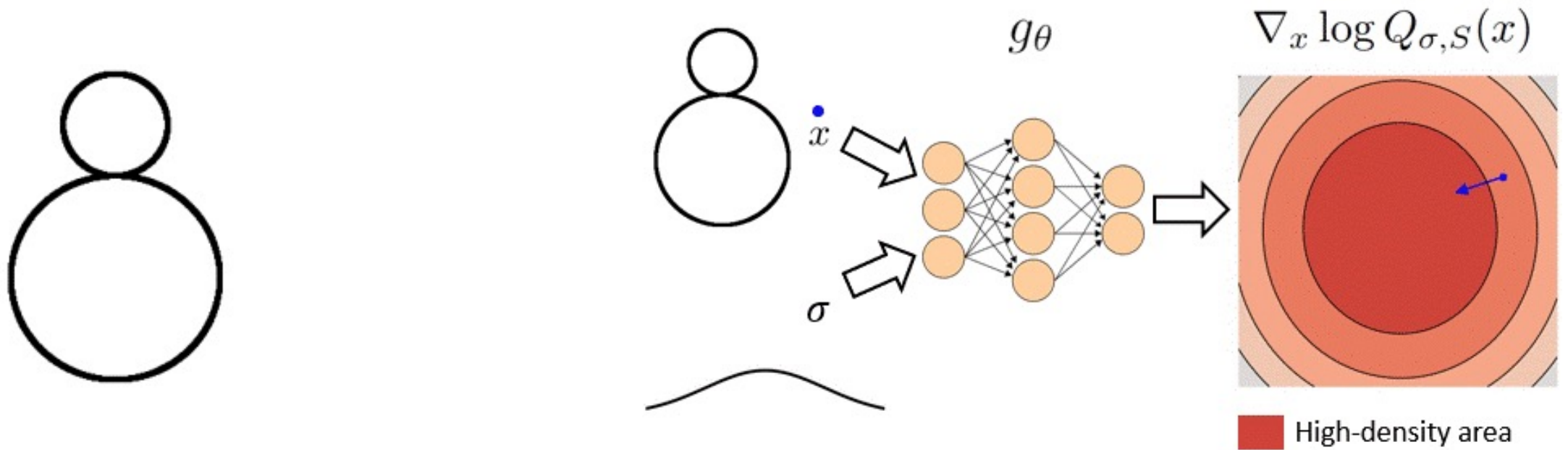
# Fitting an implicit field

- Occupancy
  - Essentially a binary classification problem
  - Sample points, label them as inside or outside the surface
- SDF
  - Essentially a regression problem
  - Sample points, label them with true signed distance
- In both cases, need watertight meshes to compute

# Fitting implicit fields from point clouds

- Most 3D data comes in the form of point clouds
- Watertight meshes / ground truth SDFs generally hard to acquire
- How to train with point clouds?
- One approach: assume point clouds are sampled from underlying distribution
- Thus shape = generative model!

# Fitting implicit fields from point clouds



# Representing high frequency details

- Standard neural networks use ReLU as activation
- So they approximate functions with piecewise linear functions
- Bad idea for high-frequency signals
  - Common in images, textured 3D surfaces etc
  - Need lots and lots of pieces!



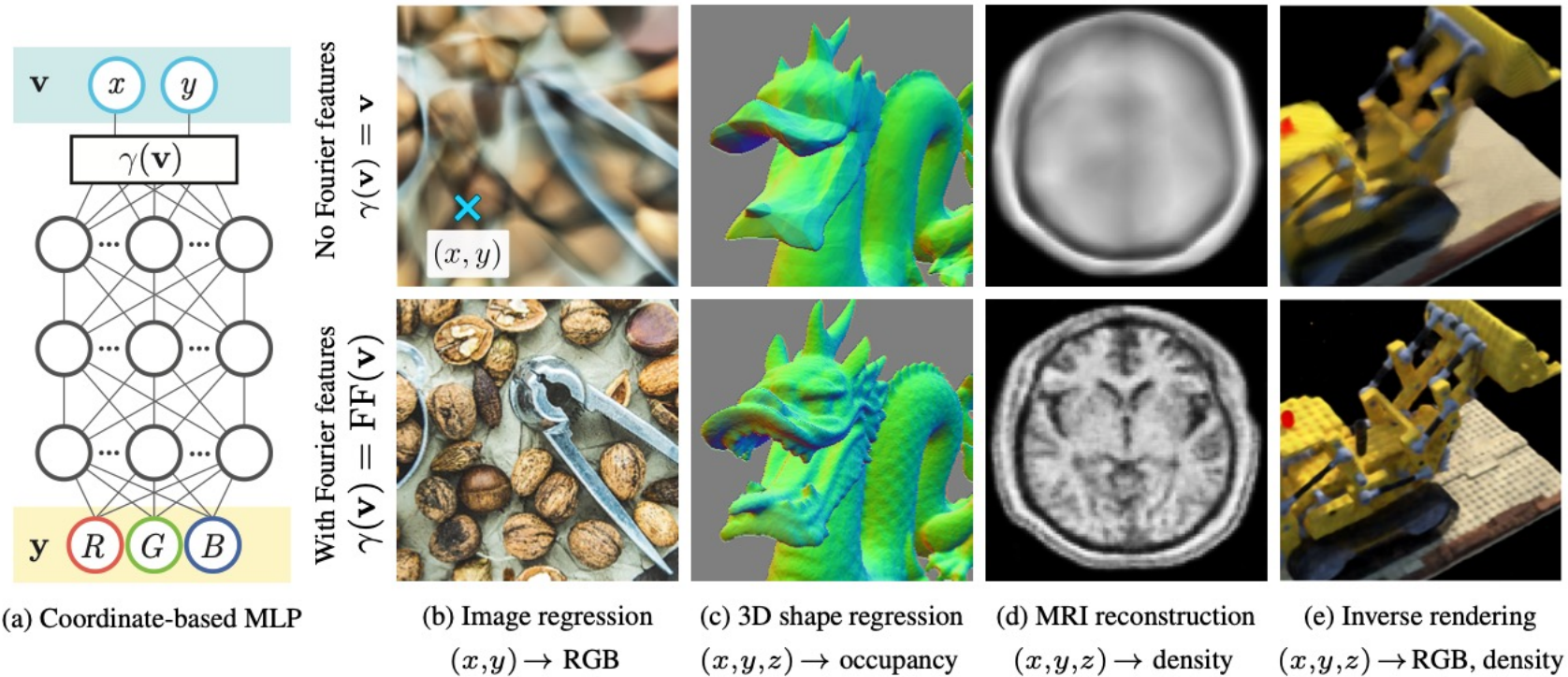
# Representing high frequency details – Fourier features

$$\mathbf{v} = (x, y, z)$$

$$\gamma(\mathbf{v}) = [a_1 \cos(2\pi \mathbf{b}_1^T \mathbf{v}), a_1 \sin(2\pi \mathbf{b}_1^T \mathbf{v}), \dots, a_m \cos(2\pi \mathbf{b}_m^T \mathbf{v}), a_m \sin(2\pi \mathbf{b}_m^T \mathbf{v})]^T$$

- Instead of  $f(\mathbf{v})$ , do  $f(\gamma(\mathbf{v}))$

# Representing high frequency details – Fourier features



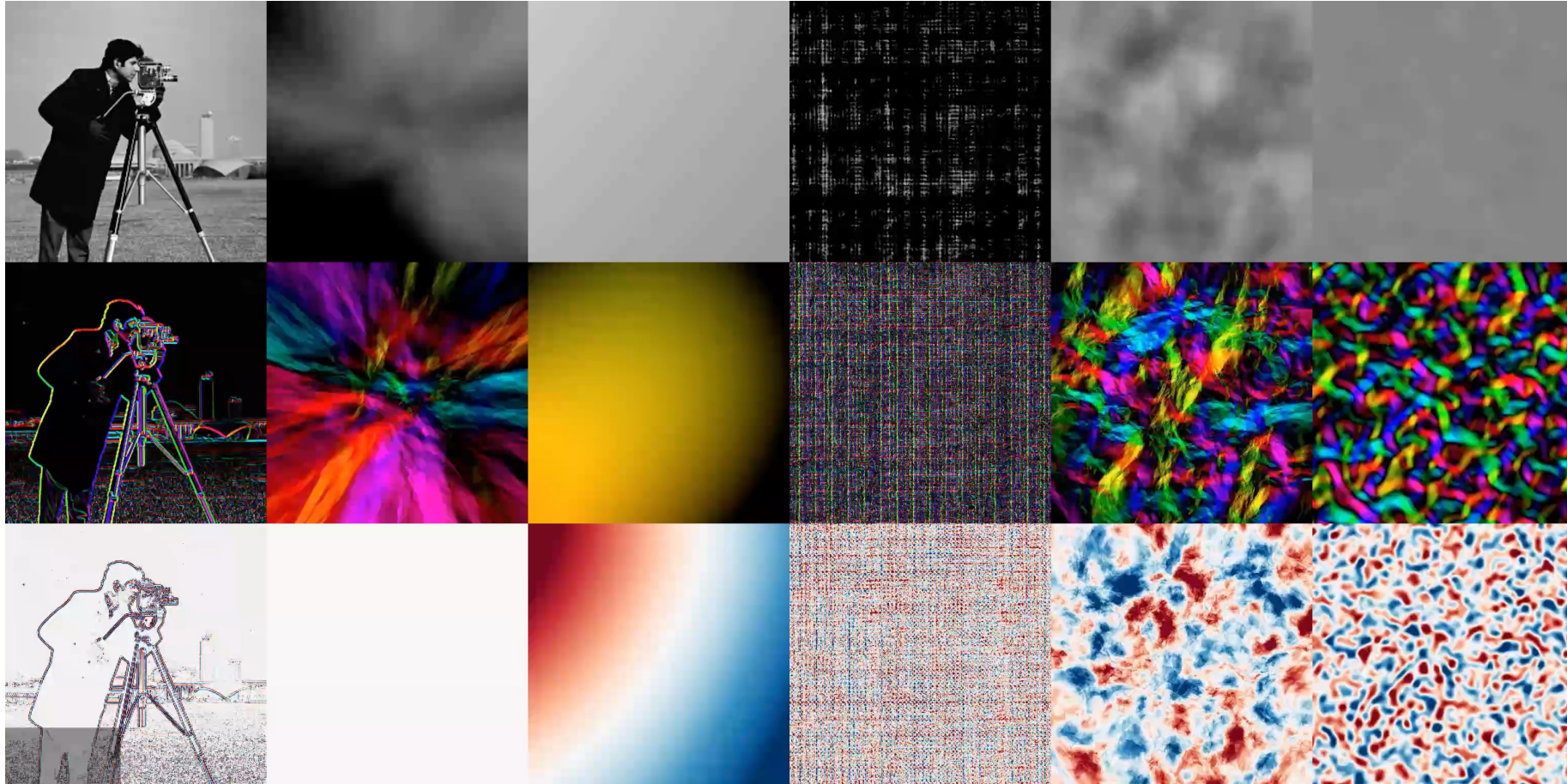
Tancik, Matthew, et al. "Fourier features let networks learn high frequency functions in low dimensional domains." *arXiv preprint arXiv:2006.10739* (2020).

# Representing high frequency details - SIREN

- Instead of ReLU activations use sinusoidal activation
- Side-effect – all derivatives exist and are themselves SIREN models
  - Allows to model both signal and derivative



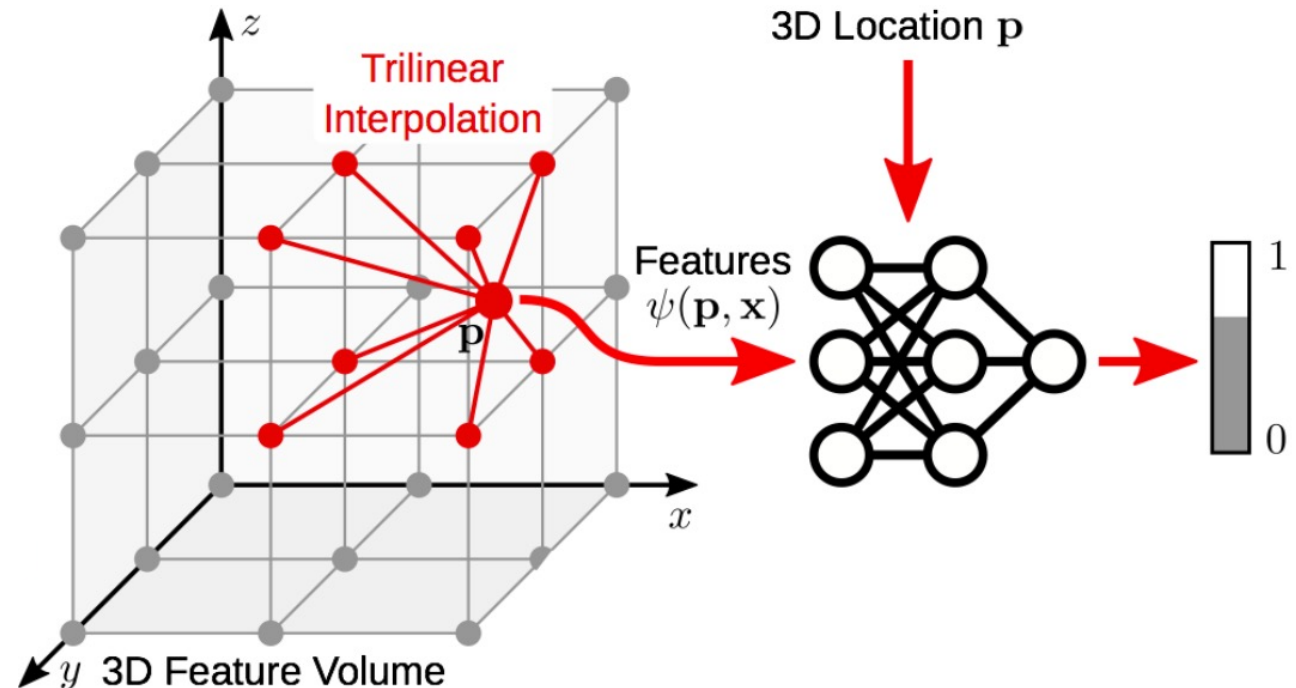
# Representing high frequency details



Sitzmann, Vincent, et al. "Implicit neural representations with periodic activation functions." *Advances in Neural Information Processing Systems* 33 (2020).

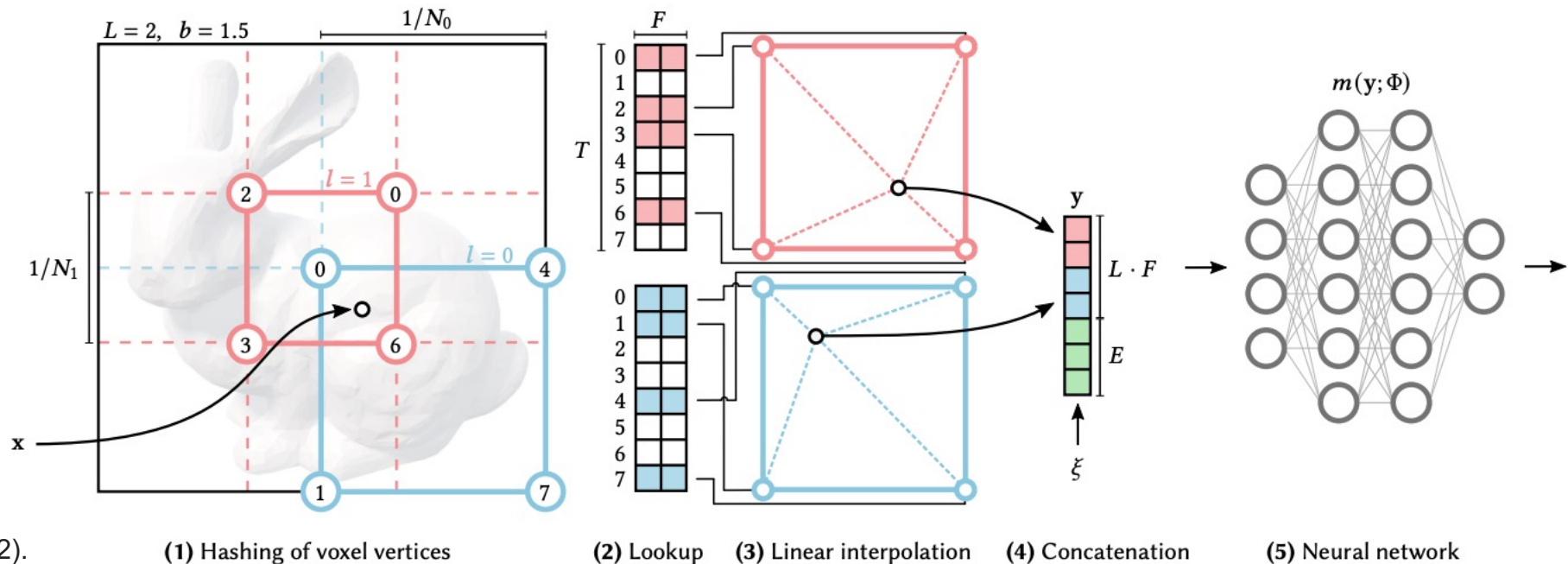
# Scene representations and detail – hybrid representations

- Use a voxelized feature volume
- For each 3D point, index into feature volume with interpolation
  - Location-dependent “latent code”!
- Use MLP to decode latent code into occupancy



# Scene representations and detail – hybrid representations

- Challenge: might need many many voxels
  - With multiple spatial resolutions
- Once again memory constraints
- Idea: maintain a smaller hash table of features
  - Hash voxel coordinates



# Generalizing neural fields through transfer learning

- Use meta-learning framework
- Learn *initialization for network*  $\theta_0$
- In each training iteration
  - Sample a shape
  - Perform SGD steps to update parameters to  $\theta_0 + \Delta\theta$
  - Backpropagate final loss to update  $\theta_0$
- Compared to latent code approach, allows greater fidelity/cheaper networks since new shapes can use different weights

# Using implicit fields for 3D reconstruction

Input

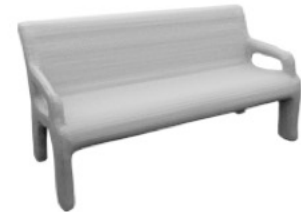
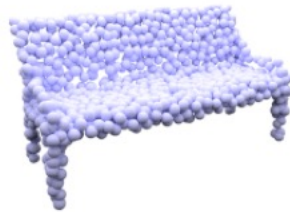
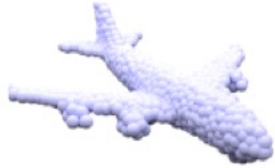
3D-R2N2

PSGN

Pix2Mesh

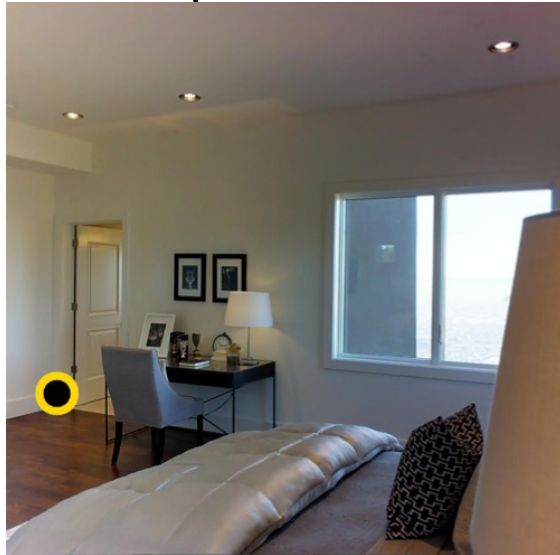
AtlasNet

Ours

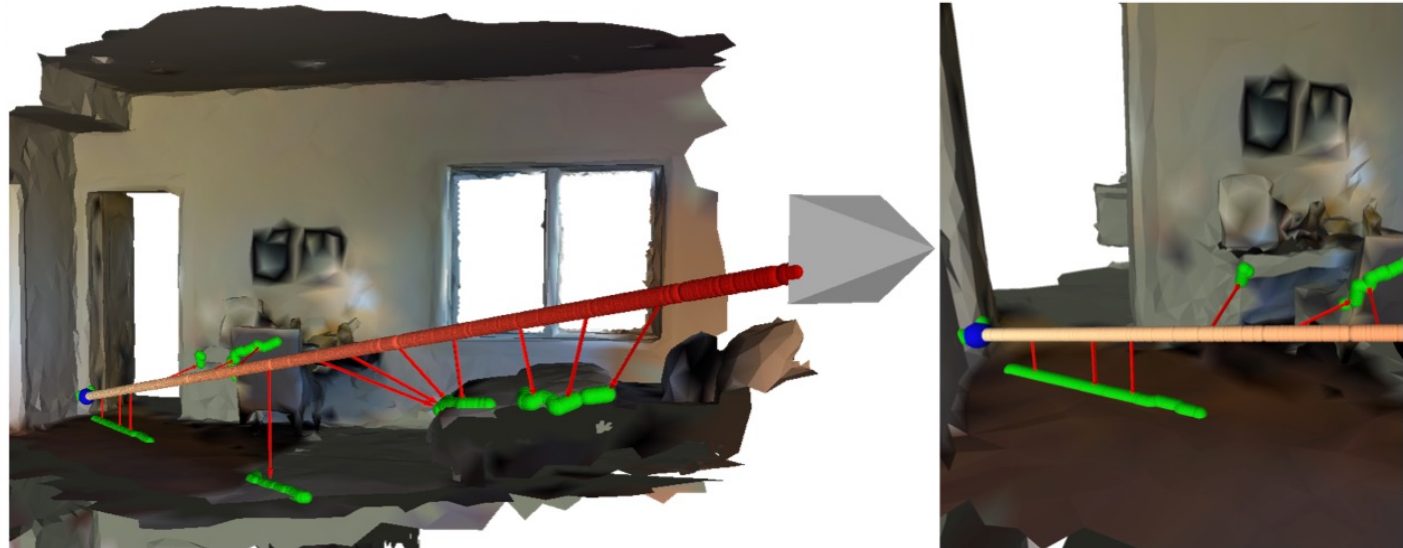


# From single objects to scenes – problems with distance fields

- Signed distance fields no longer meaningful
- Unsigned distance fields meaningful but hard to analyze
- One approach: ray distance
  - For each point on the ray, distance to nearest intersection of the ray
  - But dependent on view



(a) Image with ray center

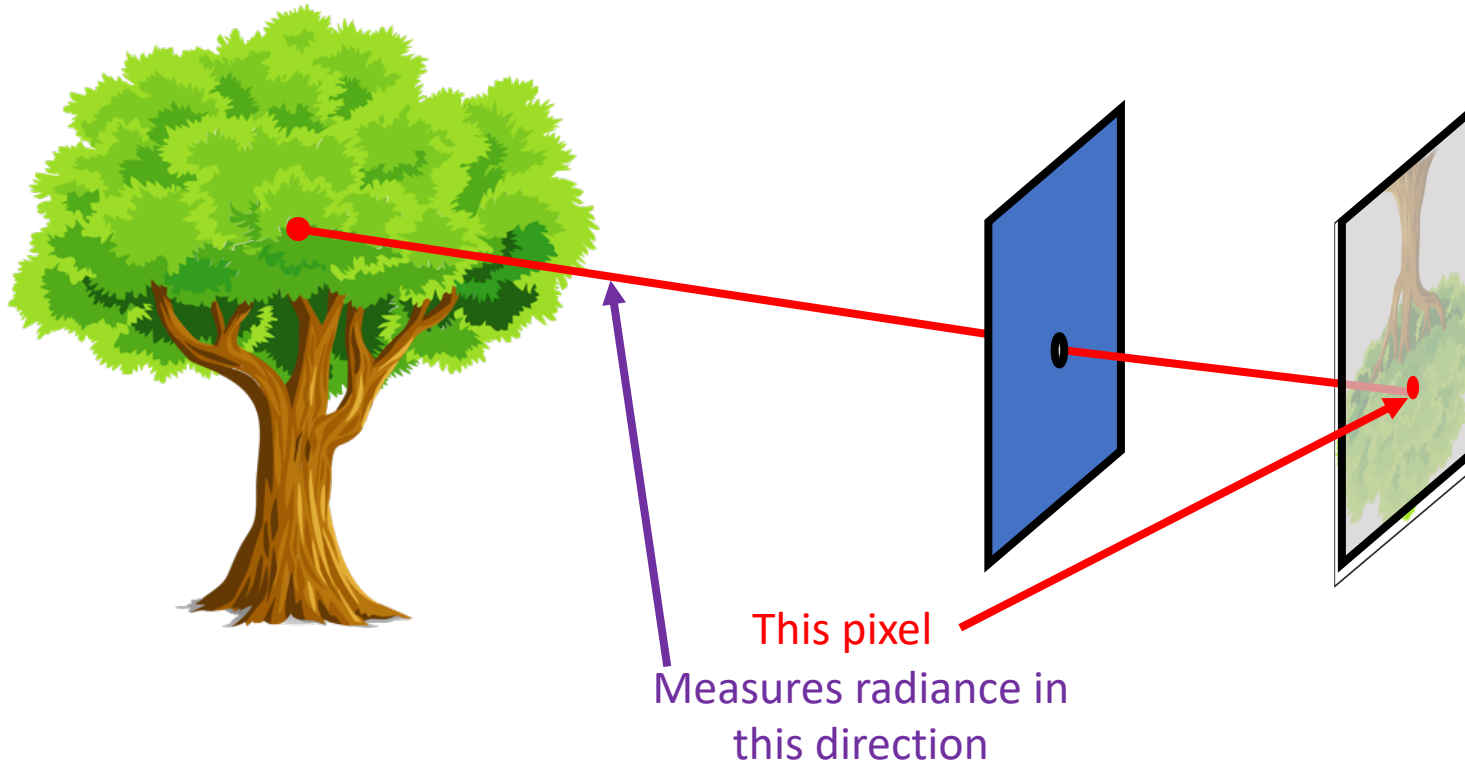


(b) Third person 3D views with the red ray and nearest points

Neural fields of radiance

# Radiance

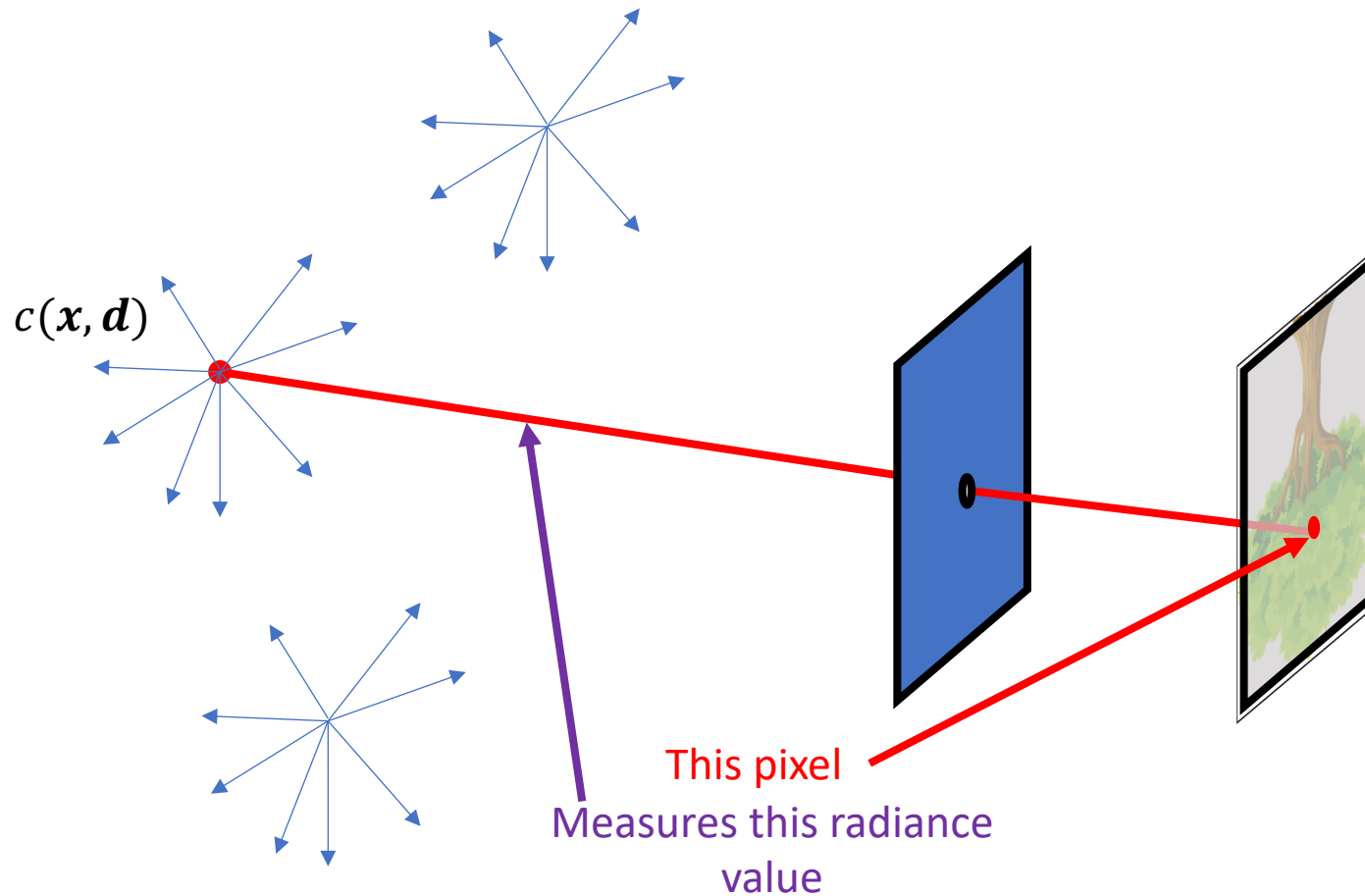
- Pixels measure *radiance*





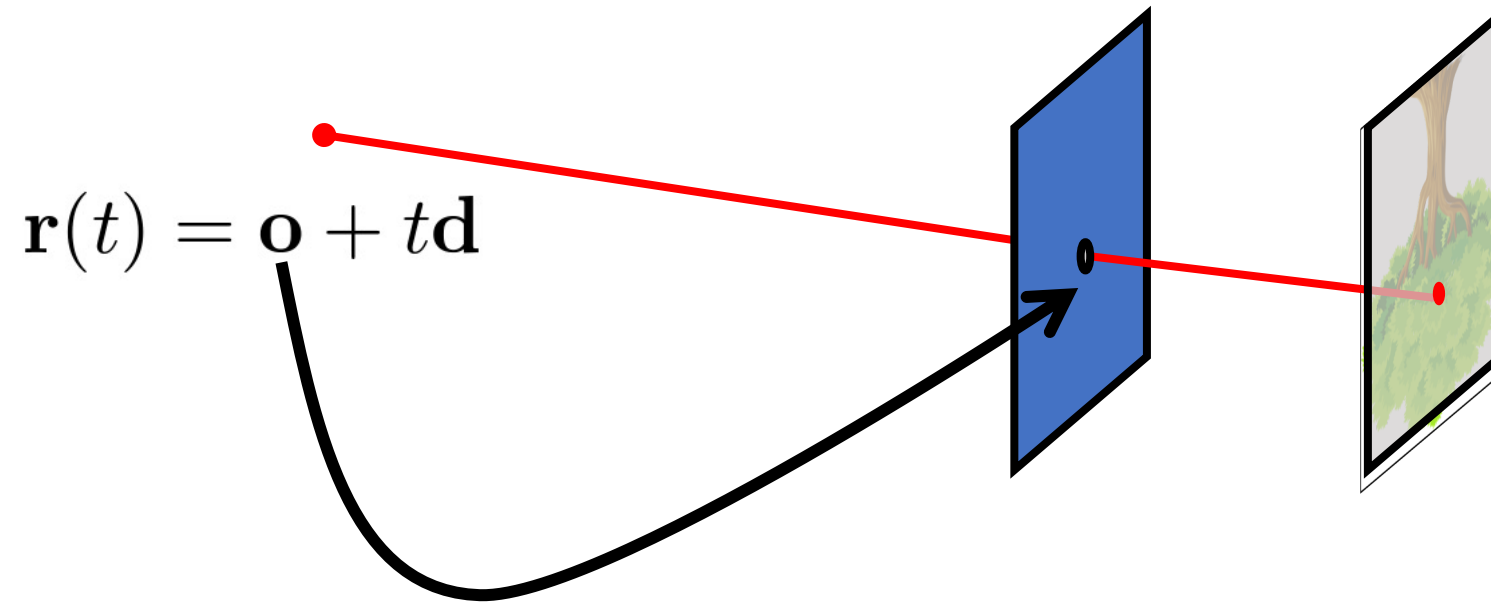
# Radiance fields

- Radiance field  $c(\mathbf{x}, \mathbf{d})$
- Also have density  $\sigma(\mathbf{x})$  : where are the surfaces?



# Volume rendering with radiance fields

- Pixels measure *radiance*



# Volume rendering with radiance fields

Integral along ray

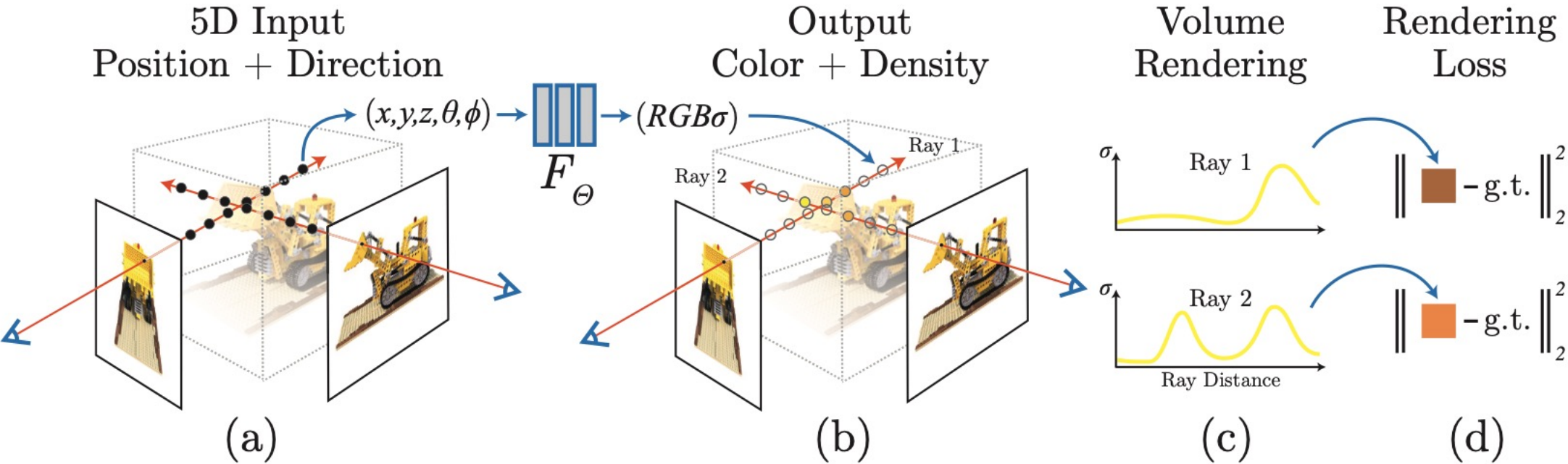
Observed color

$$C(\mathbf{r}) = \int_{t_n}^{t_f} T(t) \sigma(\mathbf{r}(t)) \mathbf{c}(\mathbf{r}(t), \mathbf{d}) dt$$

Soft visibility

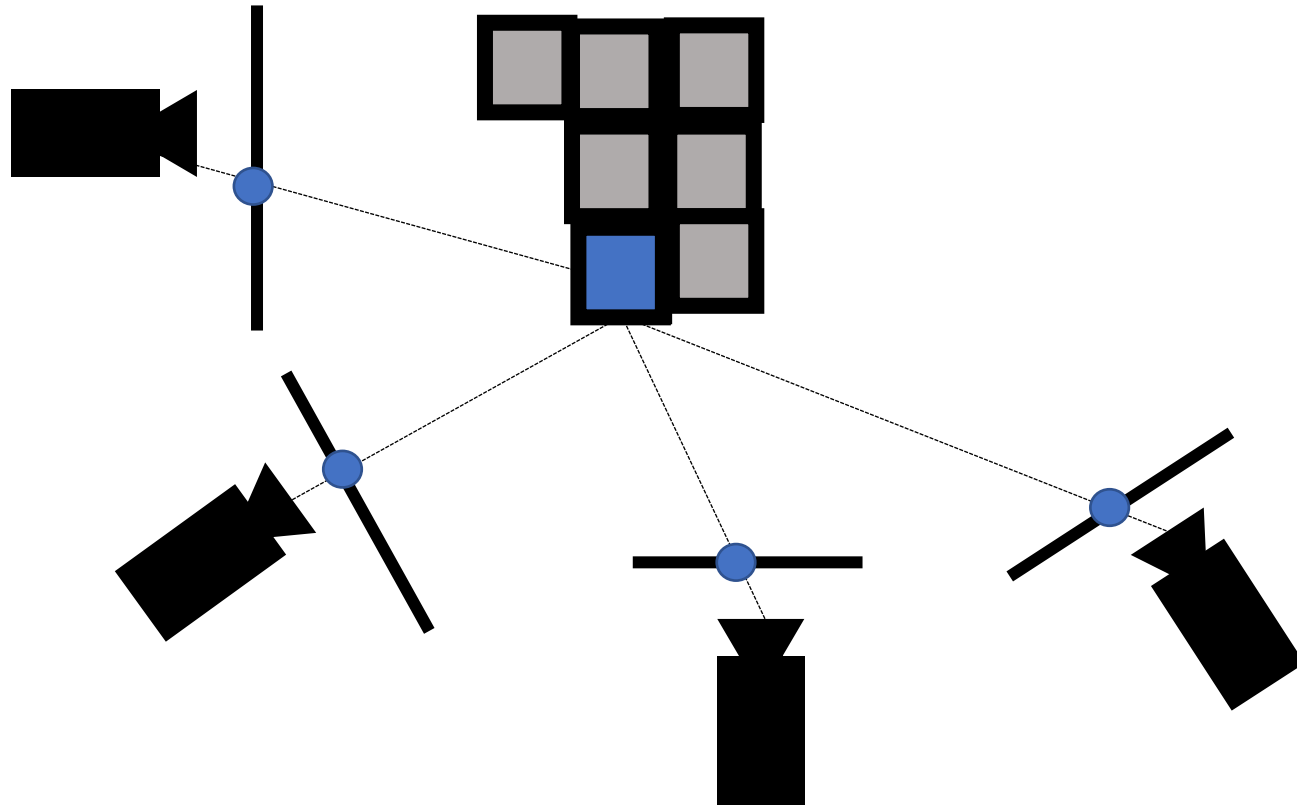
$$T(t) = \exp\left(-\int_{t_n}^t \sigma(\mathbf{r}(s)) ds\right)$$

# Neural radiance fields

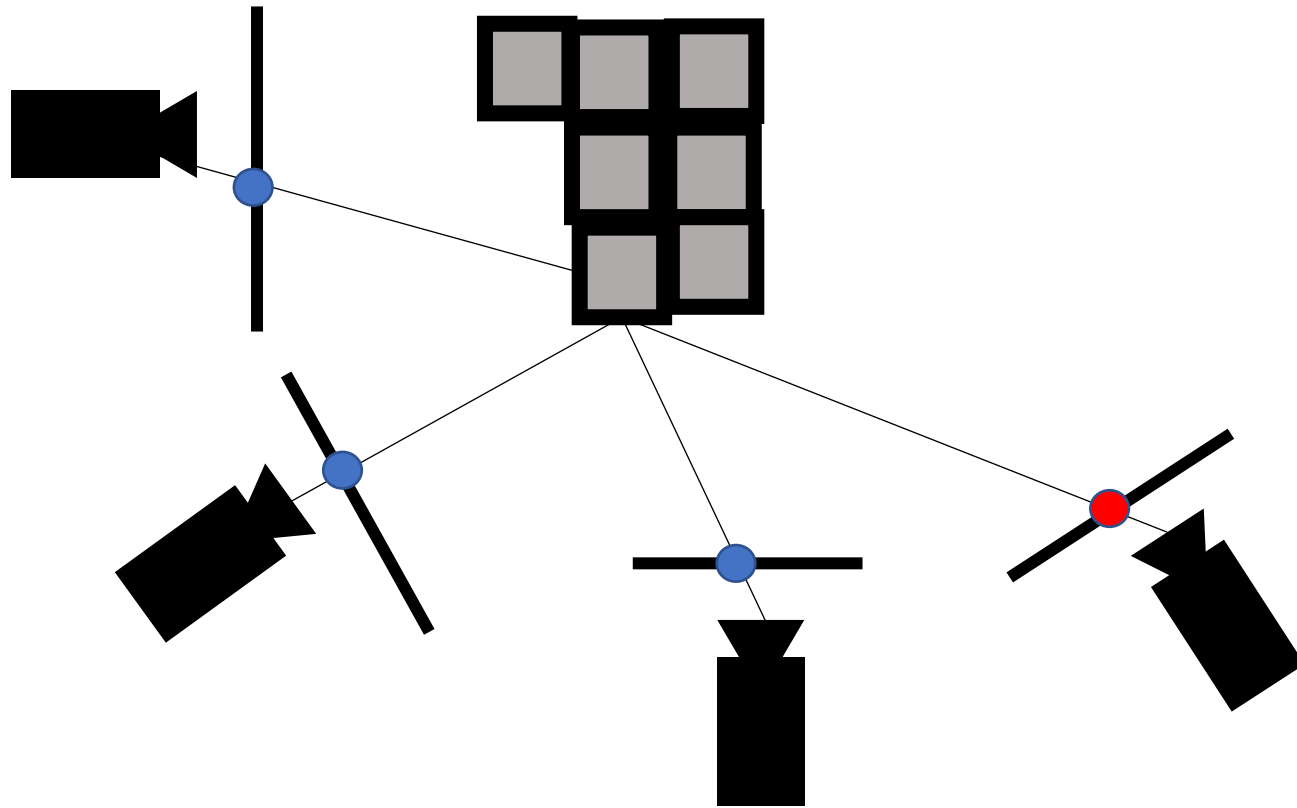


Mildenhall, Ben, et al. "Nerf: Representing scenes as neural radiance fields for view synthesis." *European conference on computer vision*. Springer, Cham, 2020.

# Connections to classical algorithms: Space carving



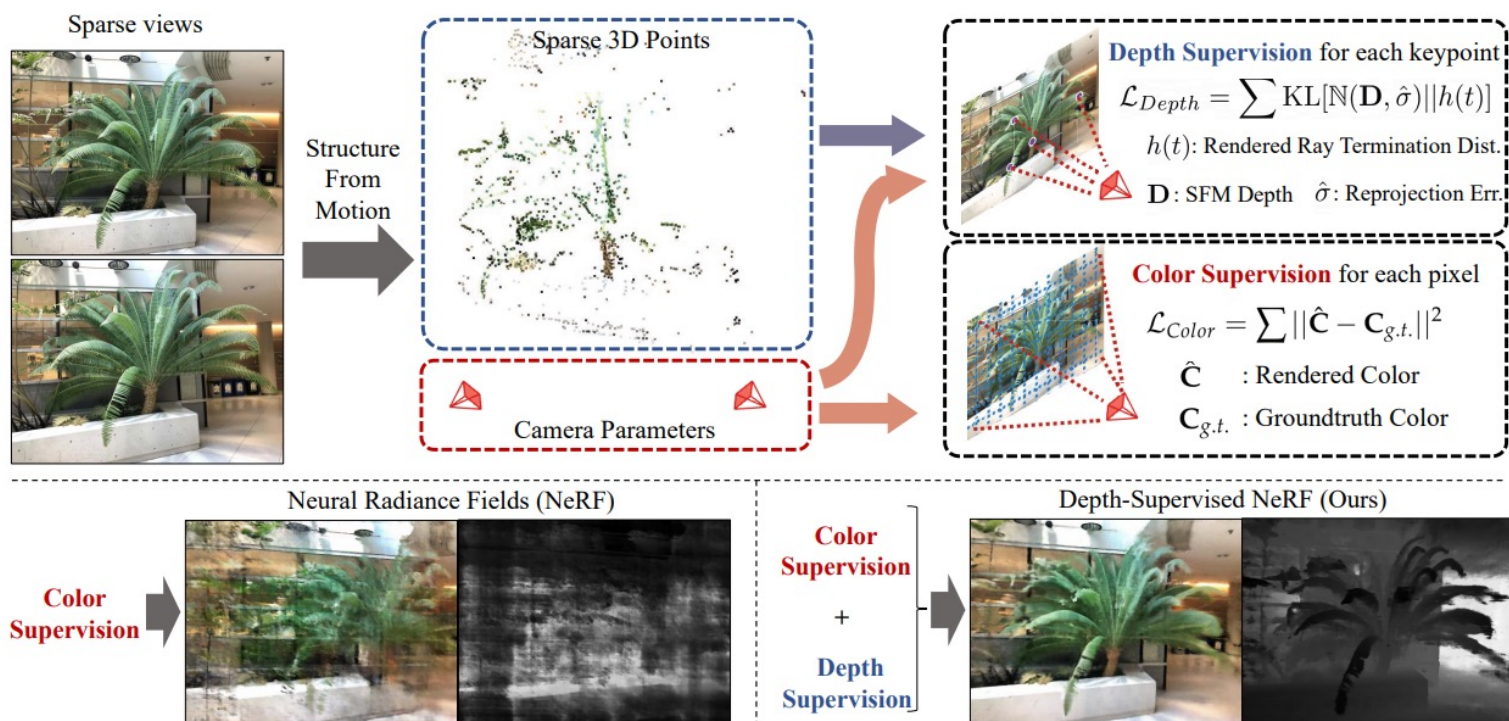
# Connections to classical algorithms: Space carving



# Leveraging classical 3D reconstruction

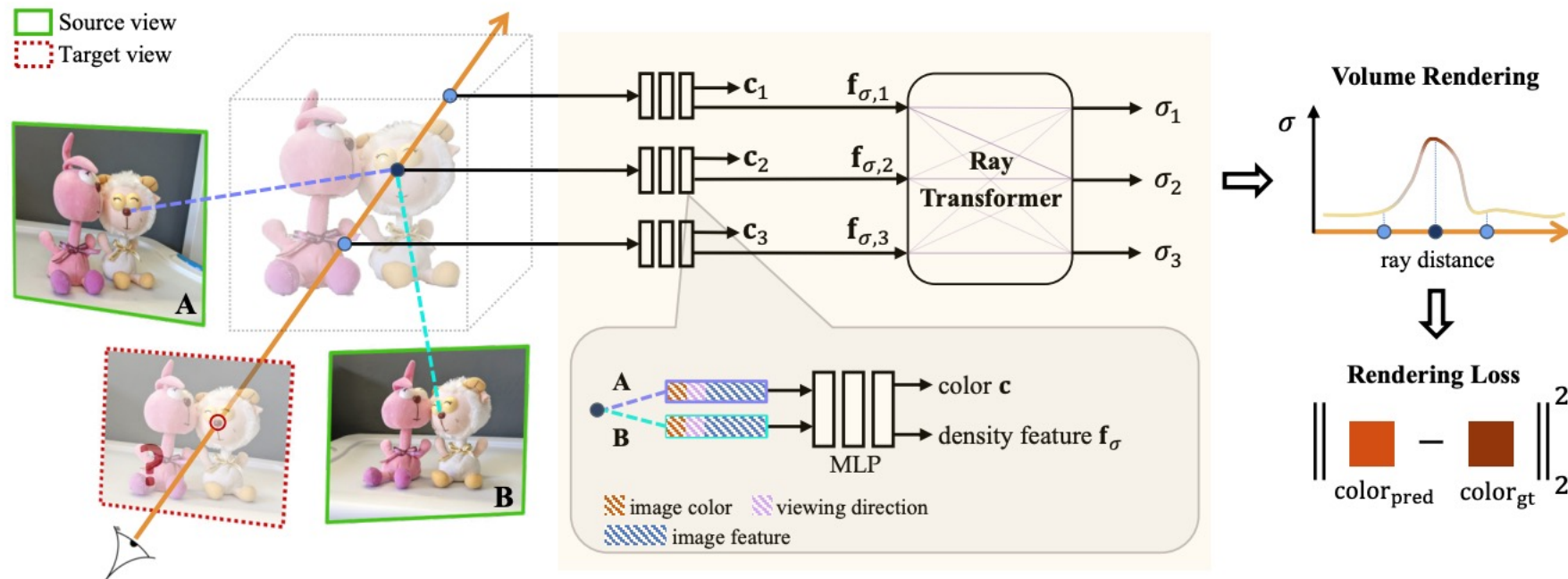
## Depth-supervised NeRF: Fewer Views and Faster Training for Free

Kangle Deng<sup>1</sup>   Andrew Liu<sup>2</sup>   Jun-Yan Zhu<sup>1</sup>   Deva Ramanan<sup>1,3</sup>  
<sup>1</sup>Carnegie Mellon University   <sup>2</sup>Google   <sup>3</sup>Argo AI



# Generalizing neural radiance fields across scenes

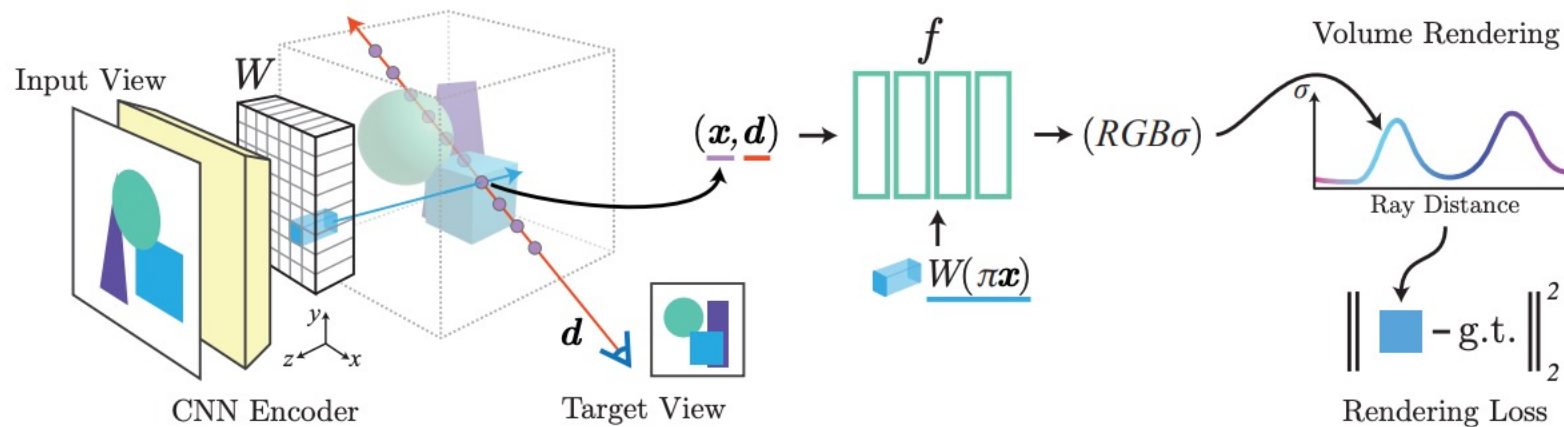
- Key idea: have neural network explicitly look up other views instead of storing radiance





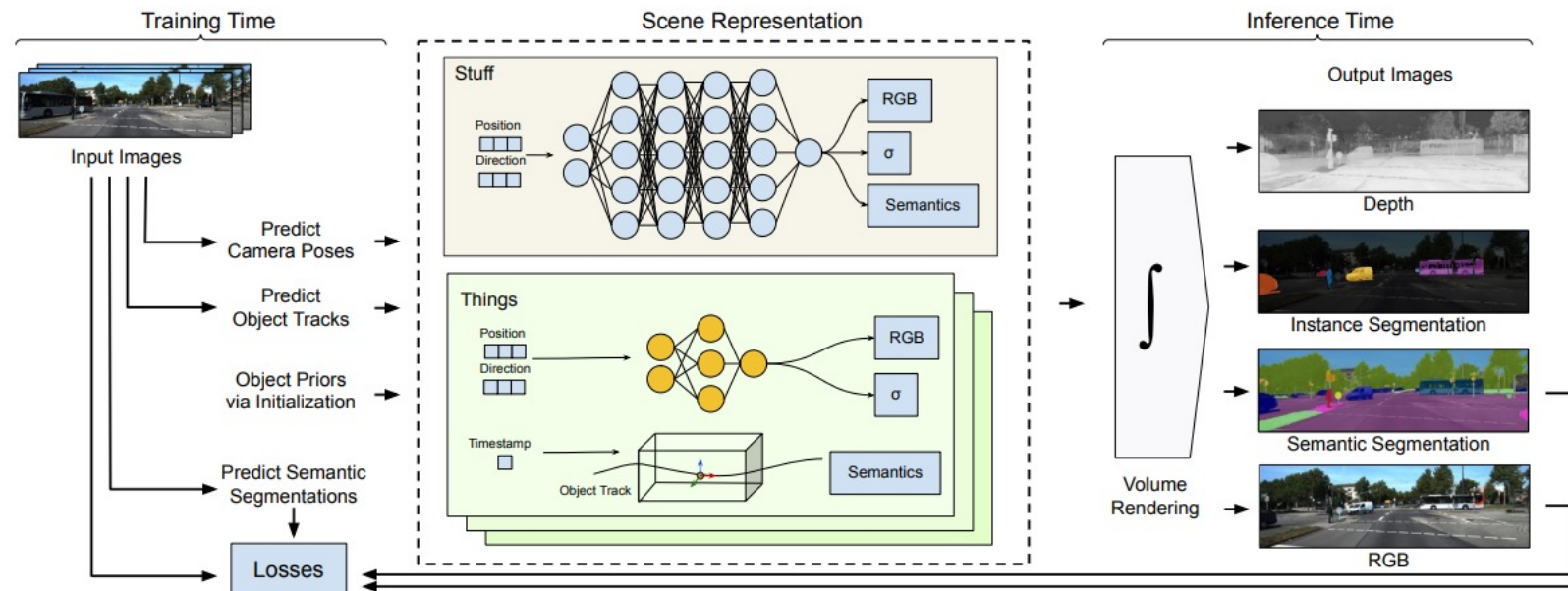
# Generalizing neural radiance fields across scenes

- Key idea: have neural network explicitly look up other views instead of storing radiance

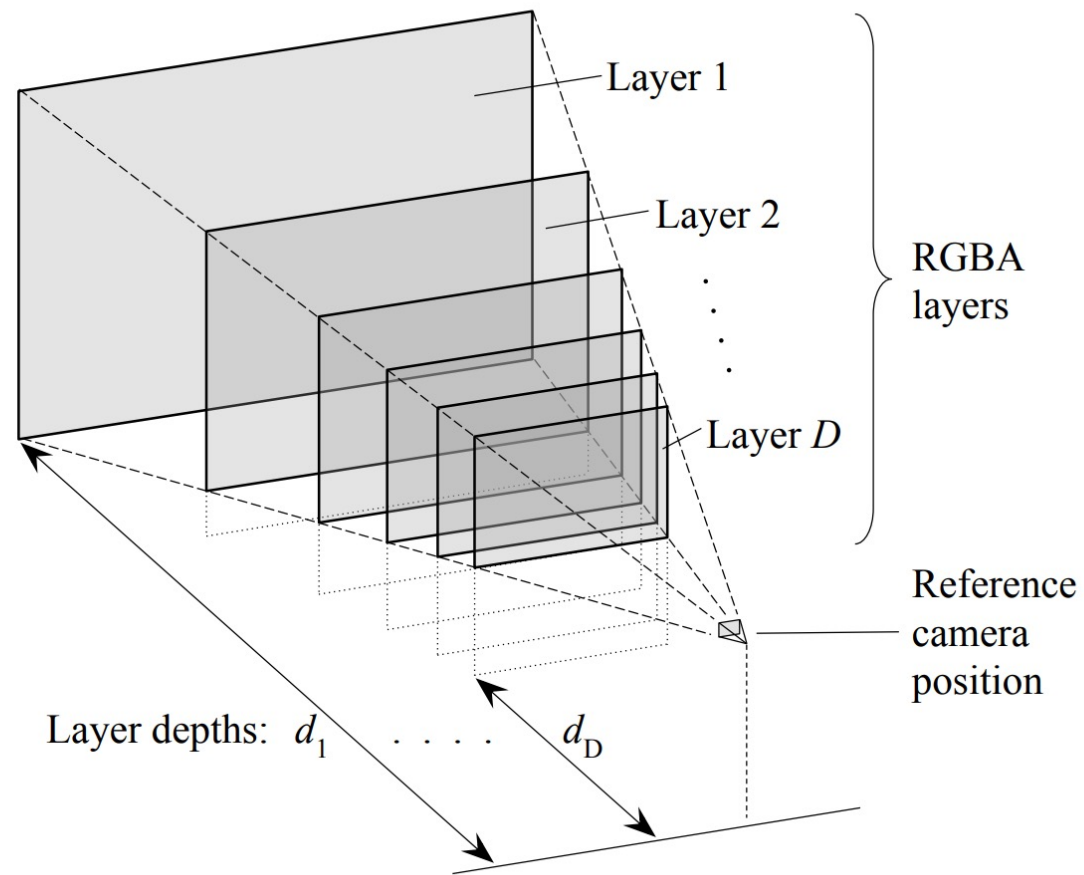


# Neural fields of semantics

- Can use neural fields to store not just color but also semantics
- Useful way to encode cross-view consistency of recognition



# Other representations of 3D structure: Multiplane images



# Challenges with neural fields

- Shape information is stored in neural network weights
  - Difficult to edit
- Appearance information entangled with shape and pose
- Generalization across complex scenes still work in progress