

CS 6620 Advanced Interactive Rendering

Spring 2009
Kavita Bala
Computer Science
Cornell University

Information

- Kavita Bala (kb@cs.cornell.edu)
 - Upson 5142
- AA: Melissa Totman (mtotman@cs.cornell.edu)
- Lectures: Mon and Wed, 1:25-2:40
 - UP 111

What is this course about?

- Practical state-of-the-art rendering algorithms
 - Industry: simulation, games, movies
- Assumptions
 - Exposure to ray tracing
 - 465/466
 - If not, talk to me

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Pre-req: Ray Tracing

- Introduced in 1980 by Turner Whitted
- Trace rays from eye into scene
 - Backward ray tracing

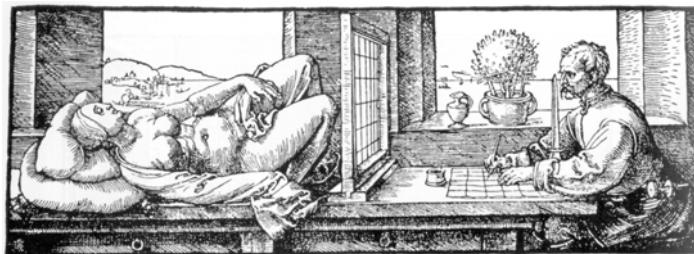
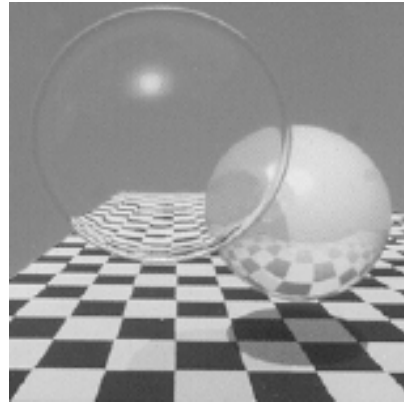


Fig. 6.9 Albrecht Dürer, illustration showing a 'veil' being used to draw a perspective image of a naked woman. From his *Underweysung der Messung mit dem Zirkel und Richtscheit* (Nuremberg, 1525), Book 3, Figure 67.

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Insights

- Find visible objects
- Shade visible points
 - Shadows
 - Reflections
 - Refractions



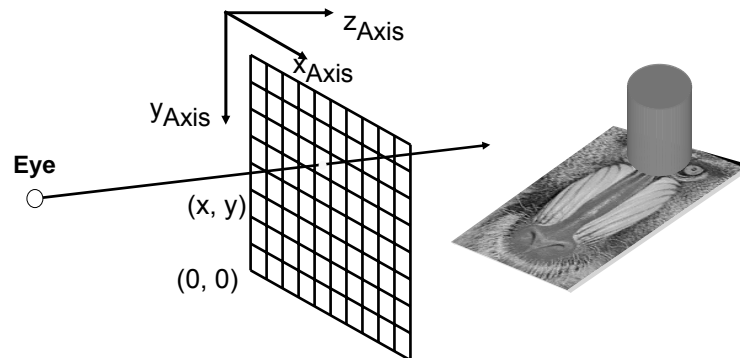
Whitted 1980: First ray traced image

- First global illumination algorithm!

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Basic Algorithm - View Rays

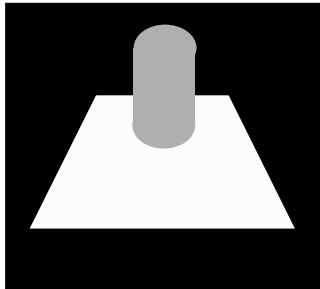
- Rays are cast from the eye point through each pixel in the image



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Visibility Determination

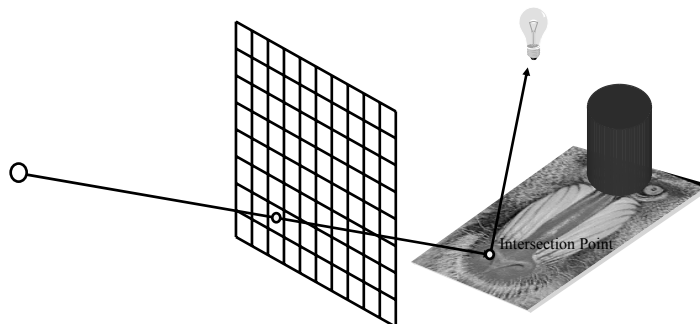
- Intersect eye ray with all objects in scene
 - Find closest object
 - Z-buffer was existing algorithm
- No intersection? Show background color



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Basic Algorithm - Shadows

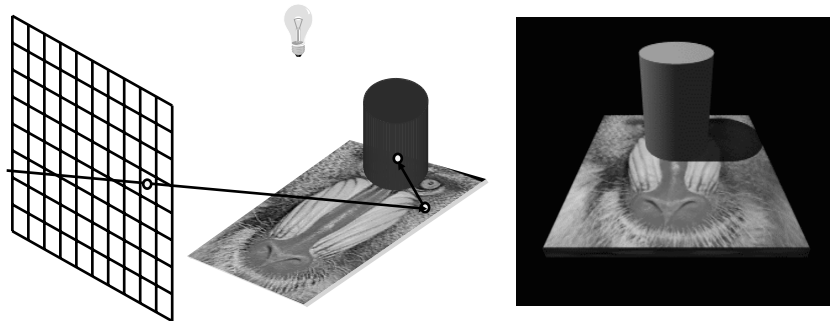
- Cast ray from the surface point to each light source: shadow rays



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Basic Algorithm - Shadows, cont.

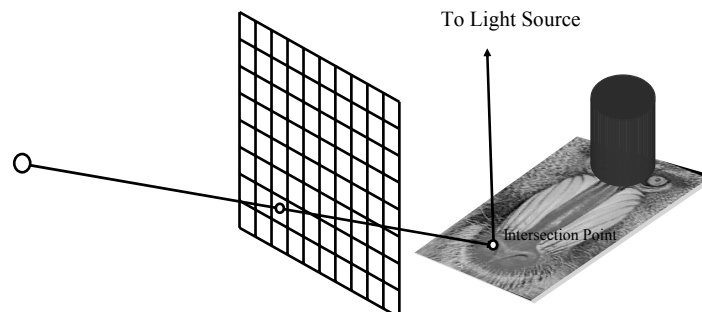
- Shadow ray is blocked = shadow



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Basic Algorithm – Shadow Rays

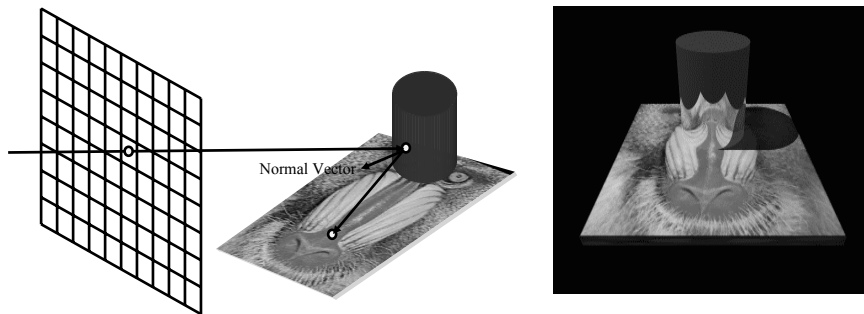
- If shadow ray not blocked, calculate color based on shading model



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Basic Algorithm - Reflections

- If object specular, shoot secondary reflected rays



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Ray Tracing



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Advanced State-of-the-Art Rendering

- Practical algorithms used in industry
- High-quality rendering

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Advanced State-of-the-Art Rendering

- High-quality rendering
 - Monte Carlo rendering
 - Photon mapping
 - Lightcuts
- Interactive rendering
 - Radiosity and variants
 - Shadow algorithms
 - GPU rendering and global illumination
 - Precomputed radiance transfer (PRT)

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Advanced State-of-the-Art Rendering

- Handling Complexity
 - Acceleration Structures
 - Scalable Rendering
 - Interactive Ray Tracing
- Rendering in movies
 - Final render
 - Cinematic relighting

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Advanced State-of-the-Art Rendering

- Trends in rendering research
 - Accuracy
 - Scalable rendering
 - Perceptually-Based rendering

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Administration

- 1 exam
- 1-2 assignments
- 1 paper presentations
 - Paper report
- Final project (in groups)
 - Project proposal
 - Final demonstration

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Groups or Alone

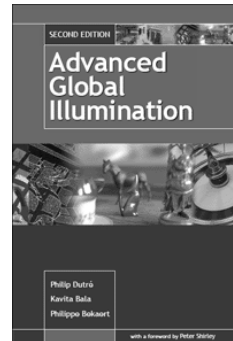
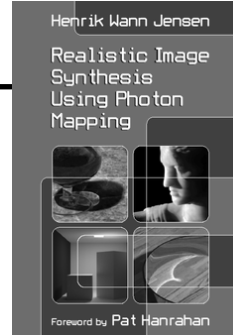
- Groups or work alone

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Book

- Photon Mapping book
 - Jensen

- Advanced Global Illumination
 - Dutre, Bala, Bekaert
 - 2nd Edition



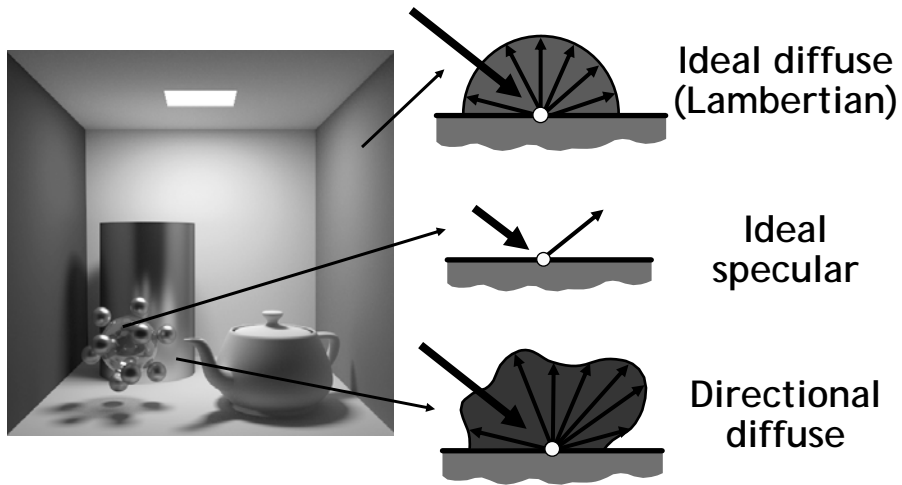
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Information

- www.cs.cornell.edu/courses/cs6620/2009sp/
 - Schedule
 - Information will be posted on CMS as well
 - Check for updates and announcements

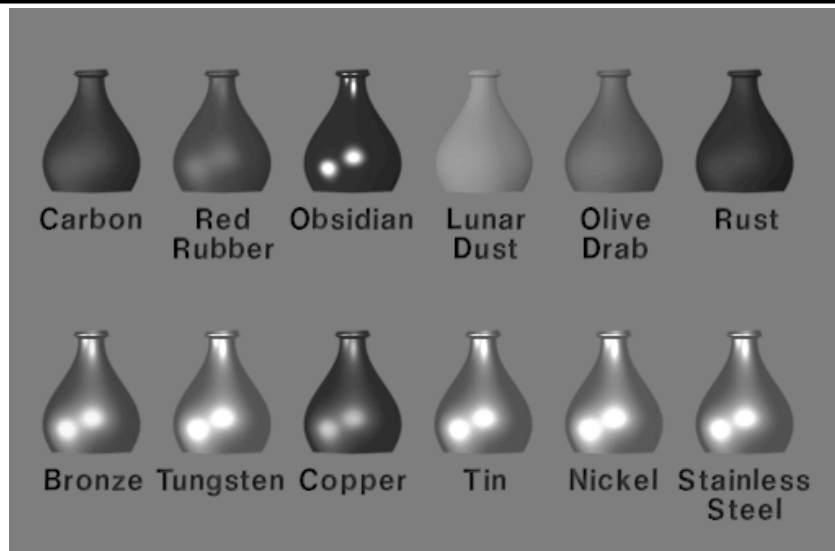
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Materials - Three Forms



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Rob Cook's vases



Source: Cook, Torrance 1981

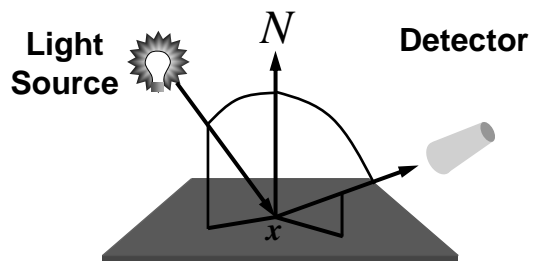
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Teapot



BRDF

- Bidirectional Reflectance Distribution Function

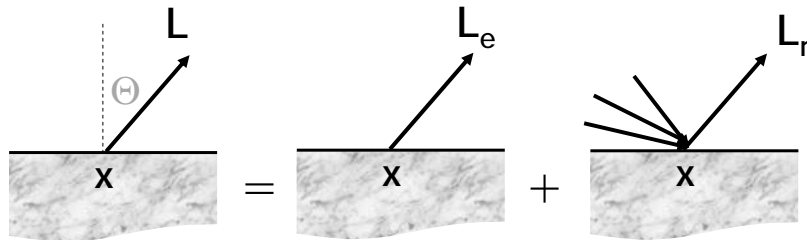


$$f_r(x, \Psi \rightarrow \Theta) = \frac{dL(x \rightarrow \Theta)}{dE(x \leftarrow \Psi)}$$

The equation is accompanied by arrows indicating the units of the terms. The numerator $dL(x \rightarrow \Theta)$ is associated with a large arrow pointing to the unit $\frac{W}{m^2 sr}$. The denominator $dE(x \leftarrow \Psi)$ is associated with a smaller arrow pointing to the unit $\frac{W}{m^2}$.

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Rendering Equation

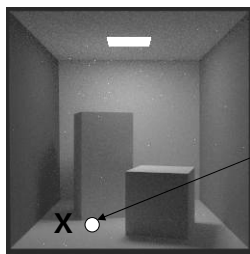


$$L(x \rightarrow \Theta) = L_e(x \rightarrow \Theta) + \int_{\text{hemisphere}} L(x \leftarrow \Psi) f_r(x, \Psi \leftrightarrow \Theta) \cos(\mathbf{N}_x, \Psi) d\omega_\Psi$$

- Applicable for each wavelength

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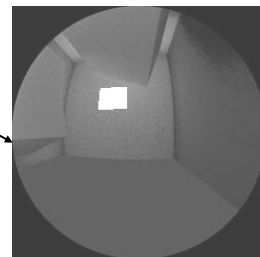
Rendering Equation



$$L(x \rightarrow \Theta) = L_e(x \rightarrow \Theta) +$$

$$\int_{\text{hemisphere}} L(x \leftarrow \Psi) f_r(x, \Psi \leftrightarrow \Theta) \cos(\mathbf{N}_x, \Psi) d\omega_\Psi$$

incoming radiance



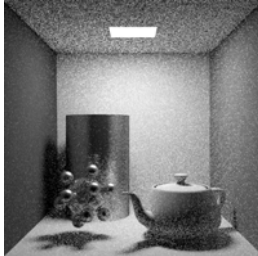
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Monte Carlo Sampling

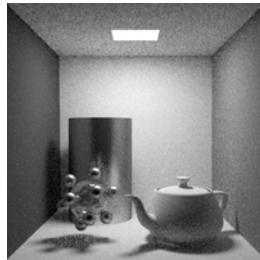
1 sample/
pixel



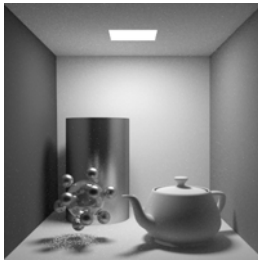
4 samples/
pixel



16 samples/
pixel

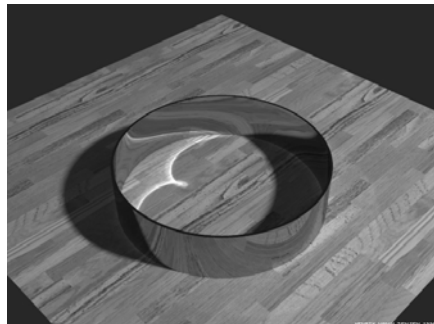


256 samples/
pixel



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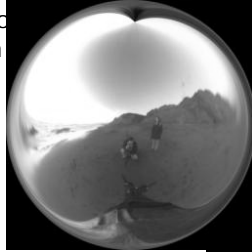
Photon Mapping



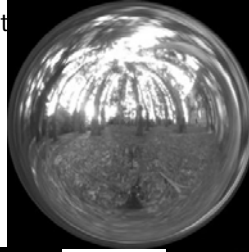
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Real-World HDR Lighting Environments

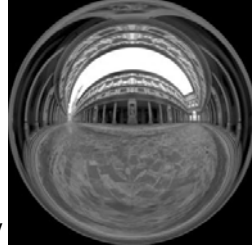
Funston
Beach



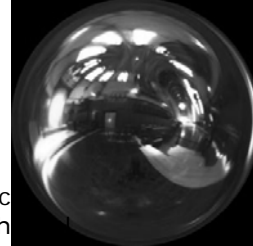
Eucalypt
Grove



Uffizi
Gallery



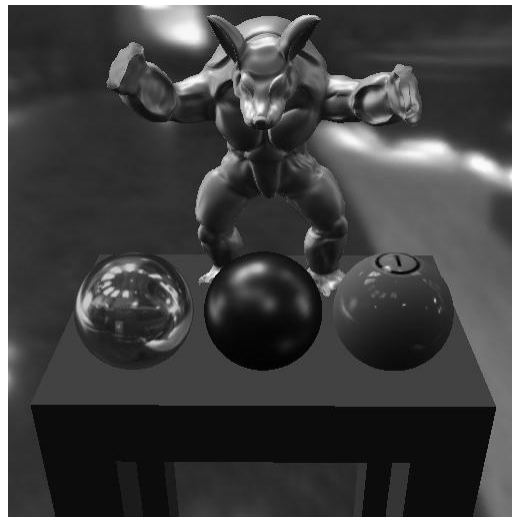
Grace
Cathedral



Lighting Environments from the Light Probe Image Gallery:
<http://www.debevec.org/Probes/>

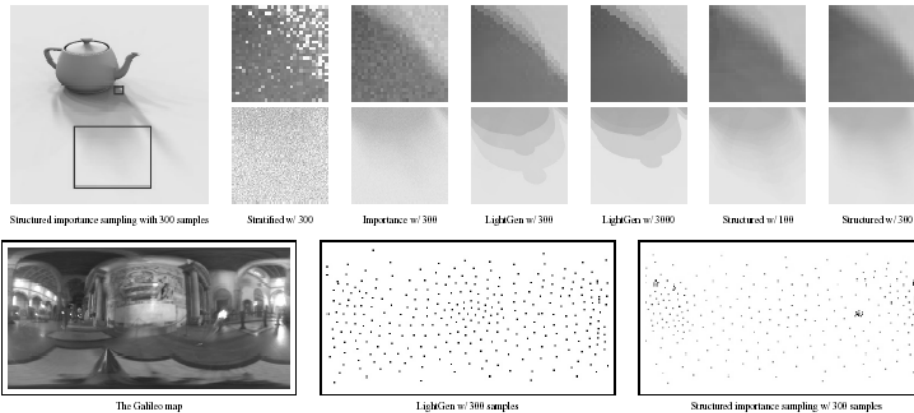
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Environment Map Rendering



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Environment Maps



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Advanced State-of-the-Art Rendering

- Interactive rendering
 - Radiosity and variants
 - Shadow algorithms
 - Shadow maps, shadow volumes, percentage closer filtering, soft shadows
 - GPU rendering and global illumination
 - Instant radiosity
 - Antiradiance
 - Precomputed radiance transfer (PRT)

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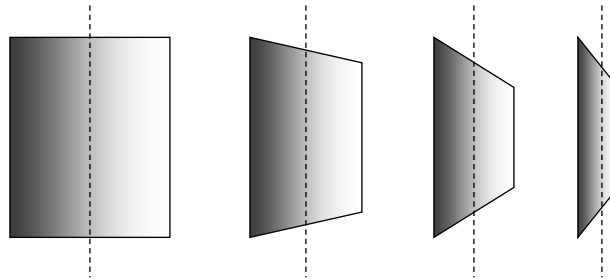
Radiosity

- Introduced in 1984
- Diffuse inter-reflections



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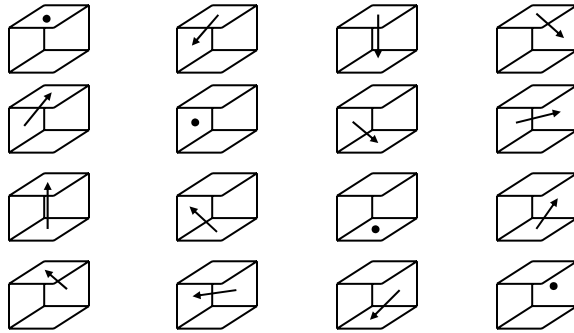
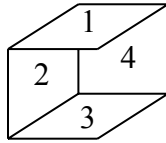
Key Idea #1: diffuse only



- Radiance independent of direction
- Surface looks the same from any viewpoint
- No specular reflections

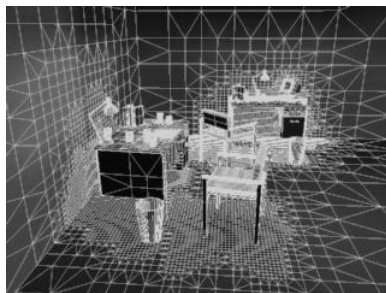
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Linear System



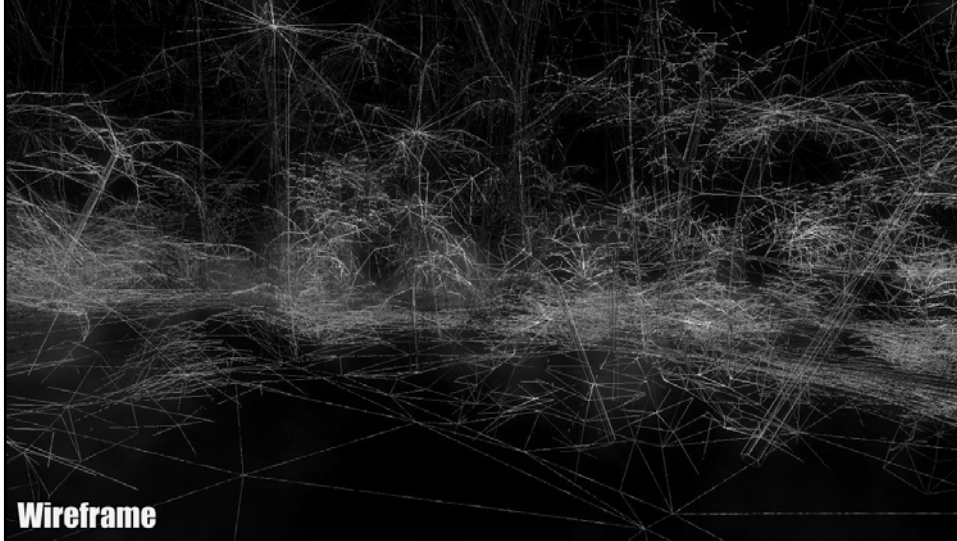
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Algorithm



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Radiosity in Games



Wireframe

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Radiosity in Games



Diffuse Colour

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Radiosity in Games



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Radiosity in Games



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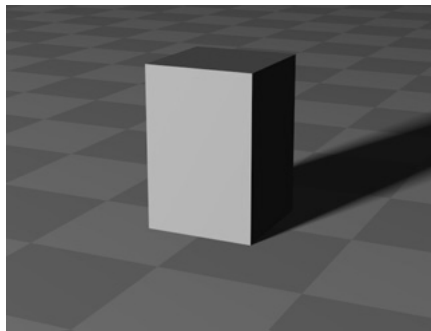
Radiosity in Games



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Why Shadows?

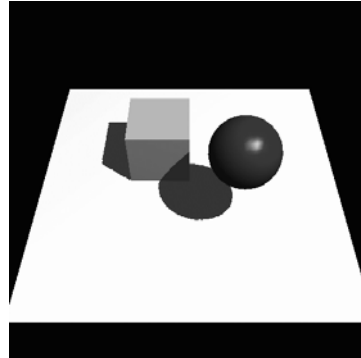
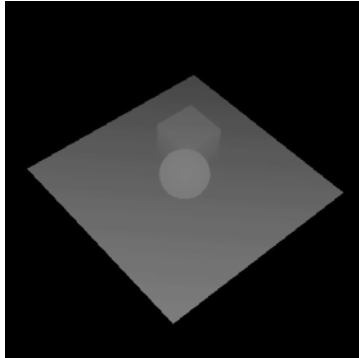
- Crucial for spatial and depth perception



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Shadow Maps

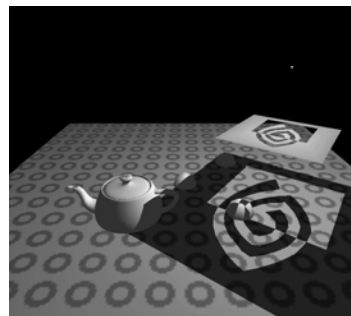
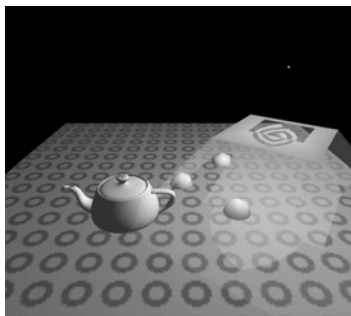
- Introduced by Lance Williams (SIGGRAPH 1978)
- Render scene from light's view
 - black is close, white is far



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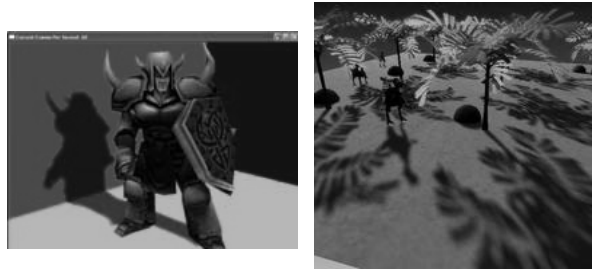
Shadow Volumes

- Clever counting method using stencil buffer
- Can cast shadows onto curved surfaces



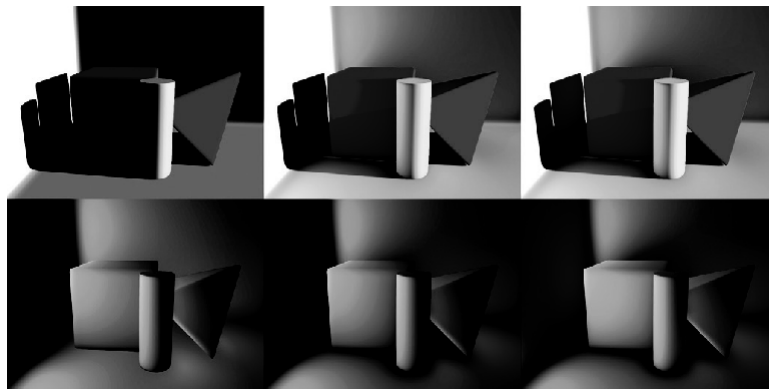
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Percentage Closer Filtering



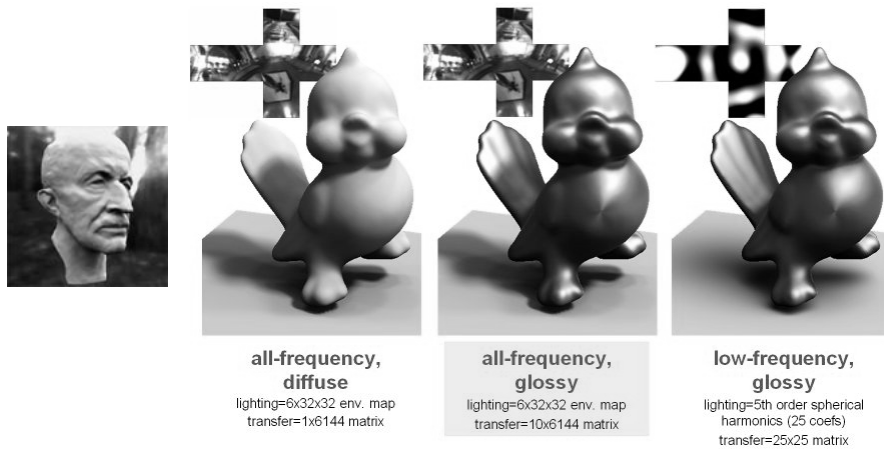
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Instant Radiosity/Dynamic Ambient Occlusion



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Precomputed Radiance Transfer



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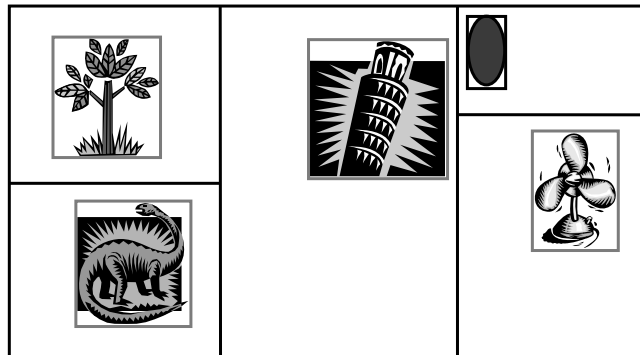
Advanced State-of-the-Art Rendering

- Handling Complexity
 - Acceleration Structures
 - Scalable Rendering
 - Interactive Ray Tracing

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K-dimensional (kd) Tree

- Spatial subdivision



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Interactive Ray Tracing



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Advanced State-of-the-Art Rendering

- Rendering in movies
 - Final render
 - PDI (Shrek)
 - Cinematic relighting
 - Pixar, Cornell
 - ILM (Lightspeed)
- Trends in rendering research
 - Scalable rendering
 - Perceptually-Based Rendering
 - Depiction

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GI for Movies



(a) direct and indirect lighting

(b) direct lighting only

Figure 1: Example of a character in outside lighting conditions. (a) and (b) were rendered respectively with and without indirect lighting.

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Rendering in Movies



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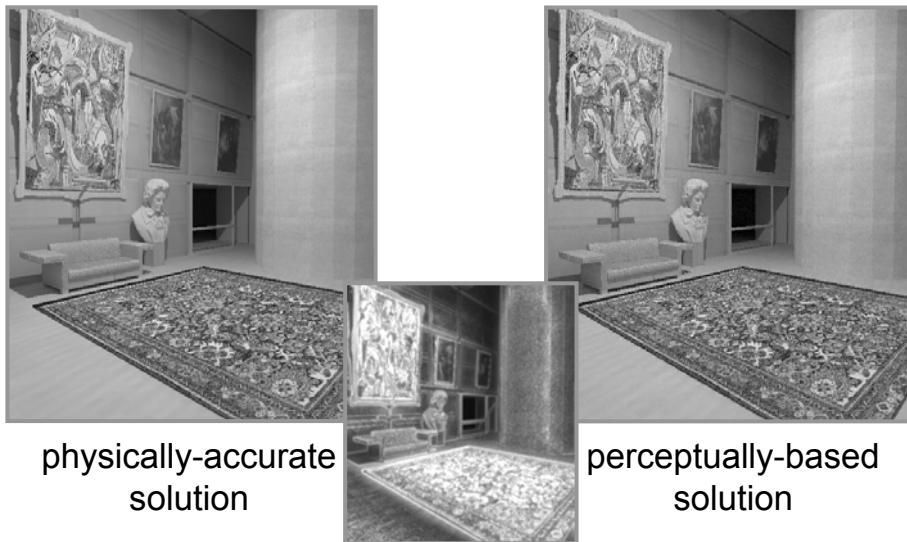
Lightspeed



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Perceptually-Based Rendering

5% effort

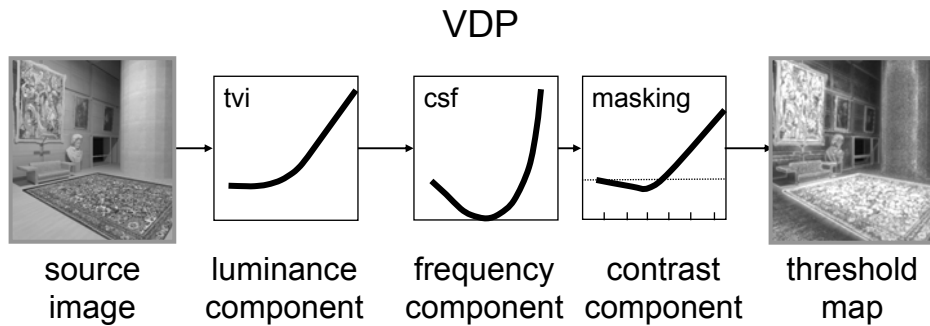


physically-accurate
solution

perceptually-based
solution

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Perceptually-driven rendering



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By the end of the course...

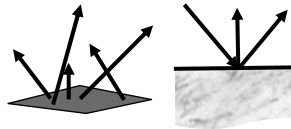
Fundamental understanding of:

- State-of-the-art practical rendering algorithms
 - For games, movies, simulation
 - Complex scene management
 - Lighting
 - Materials
 - Illumination
 - Geometry

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What is the behavior of light?

- Physics of light



- Radiometry

- Material properties

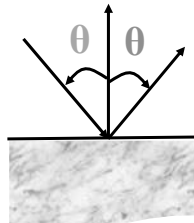


- **Rendering Equation**

Brief history of Optics: 350 B.C.

- Greek philosophers (350 B.C.)
 - Pythagoras, Plato, Aristotle
 - Light emanated from the eye
- By 300 B.C.,
 - Understood rectilinear propagation of light
 - Euclid described law of reflection

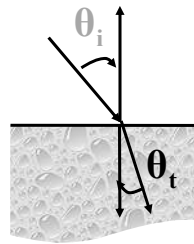
reflection



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Brief history of Optics: Dark Ages

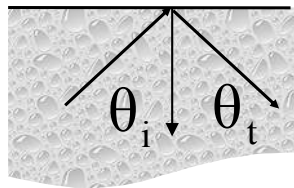
- Ptolemy (130 A.D.)
 - Refraction
- Not much in Dark Ages except for Alhazen (elaborated law of reflection)
 - Angles of incidence and reflection in the same plane as normal N



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Brief history of Optics: 17th century

- 17th century: telescopes, microscopes
- Kepler (1611)
 - Total internal reflection

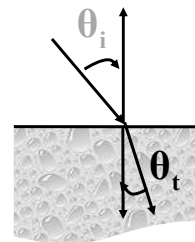


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Brief history of Optics: 17th century

- Snell (1621): Law of refraction

$$\frac{\sin \theta_i}{\sin \theta_t} = \frac{\eta_t}{\eta_i}$$
$$\eta_i \sin \theta_i = \eta_t \sin \theta_t$$

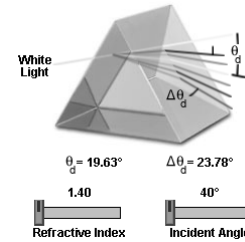


- Descartes published the sine form of law of refraction
- Fermat (1657)
 - Law of refraction from *principle of least time*

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Brief history of Optics: 17th century

- Newton (1642-1727)
 - Dispersion
 - Light splits into component colors
 - Corpuscular/emission theory

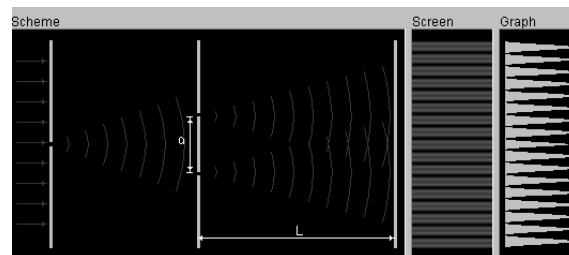


- Huygens (1629-1695)
 - Developed wave theory of light
 - Discovered polarization
- Two conflicting theories: wave vs. emission

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Brief history of Optics (contd.)

- Young (1801)
 - Principle of interference
 - Double-slit experiment



- Fresnel
 - 1816: Diffraction and interference
 - 1821: Fresnel equations for reflection and refraction

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Brief history of Optics (contd.)

- Maxwell (1831-1879)
 - Electricity and magnetism
 - Maxwell's equations
$$\nabla \cdot \mathbf{E} = 0$$
$$\nabla \cdot \mathbf{B} = 0$$
$$\nabla \times \mathbf{E} = -\partial \mathbf{B} / \partial t$$
$$\nabla \times \mathbf{B} = \mu_0 \epsilon_0 \partial \mathbf{E} / \partial t$$
 - Theoretical validation of measured speed of light
- Light is electromagnetic radiation

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Brief history of Optics (contd.)

- Hertz (1887)
 - Discovered the photoelectric effect
 - The process whereby electrons are liberated from materials under the action of radiant energy*
- Einstein (1905)
 - Explained photoelectric effect
 - Light is a stream of quantized energy packets called quanta (photons)
 - $E = h \nu$

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Brief history of Optics (contd.)

- Particle and wave theory seemingly mutually exclusive
- Quantum Mechanics
 - Bohr, Born, Heisenberg, Schrodinger, Pauli
 - Sub-microscopic phenomena
 - Unite particle and wave behavior of light
 - QED by Feynman

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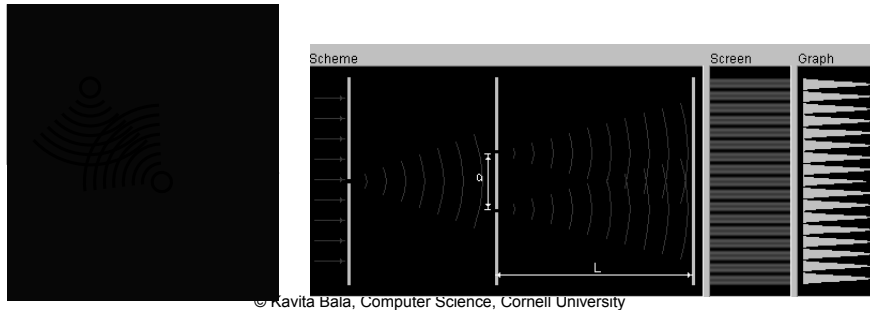
Models of Light

- Geometric Optics
 - Emission
 - Reflection / Refraction
 - Absorption
- Simplest model
- Size of objects $>$ wavelength of light

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Models of light

- Wave Model
 - Maxwell's Equations
 - Object size comparable to wavelength
 - Diffraction, Interference, Polarization



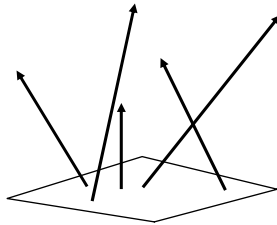
Models of light

- Quantum Model
 - Fluorescence
 - Phosphorescence
 - Relativistic effects
- Most complete model

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Geometric Optics: Properties

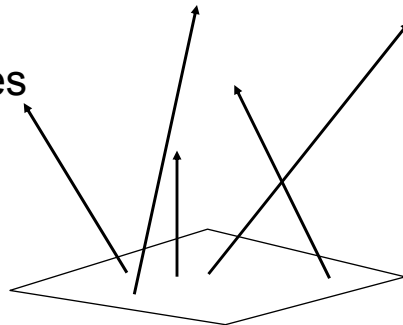
- Light travels in straight lines
- Rays do not interact with each other
- Rays have color(wavelength), intensity



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Emission

- New rays due to:
 - chemical
 - electrical
 - nuclear processes

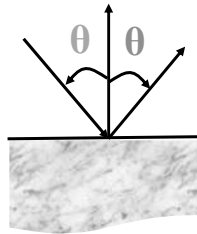


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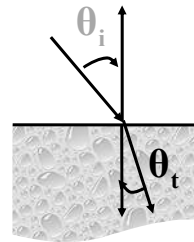
Reflections/Refractions

- Interface between 2 materials

reflection



refraction

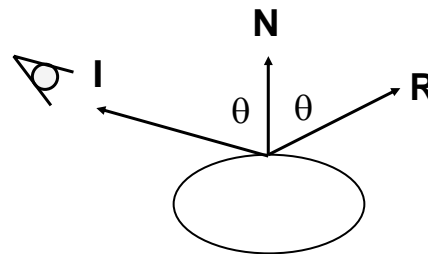


- Specular reflections and refractions
 - One direction

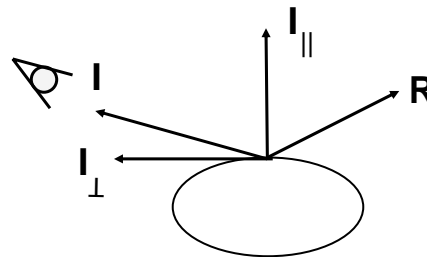
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Specular Reflections

Reflected ray R



$$\begin{aligned}
 I_{\parallel} &= (I \cdot N) N \\
 I_{\perp} &= I - (I \cdot N) N \\
 R &= I_{\parallel} + (-I_{\perp}) \\
 &= 2 (I \cdot N) N - I
 \end{aligned}$$



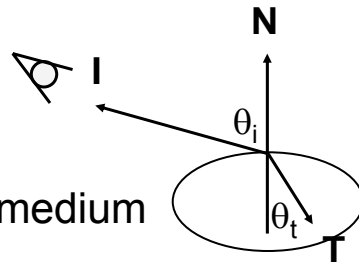
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Specular Refractions

- Compute refracted ray T
- Index of refraction: $\eta = c_{\text{vacuum}} / c_{\text{material}}$
- Snell's law:

$$\frac{\sin \theta_i}{\sin \theta_t} = \frac{\eta_t}{\eta_i}$$

$$\eta_i \sin \theta_i = \eta_t \sin \theta_t$$

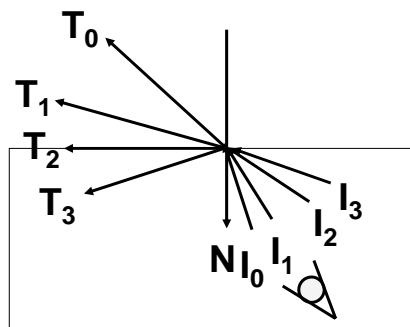


- Ray from rare to dense medium

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Total Internal Reflection

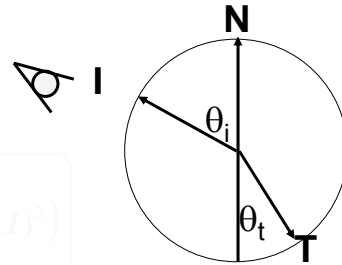
- Consider ray from dense to rare



$$\frac{\sin \theta_i}{1} = \frac{\eta_t}{\eta_i}$$

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Transmitted Ray



$$T = -\frac{\eta_i}{\eta_t} I + N \left(\frac{\eta_i}{\eta_t} (N \cdot I) - \sqrt{1 - \left(\frac{\eta_i}{\eta_t}\right)^2 (1 - (N \cdot I)^2)} \right)$$

$$T = -\eta I + N \left(\eta \cos \theta_i - \sqrt{1 - \eta^2 \sin^2 \theta_i} \right)$$

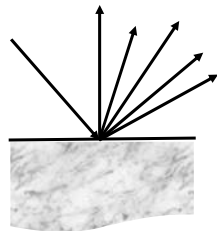
$$\cos \theta_t = (N \cdot I)$$

$$\eta = \frac{\eta_i}{\eta_t}$$

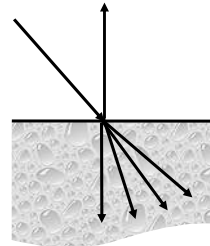
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Realistic Reflections/Refractions

reflection

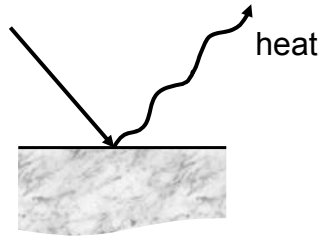


refraction



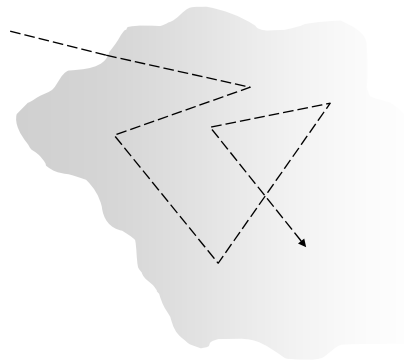
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Absorption



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Interaction with matter



participating medium

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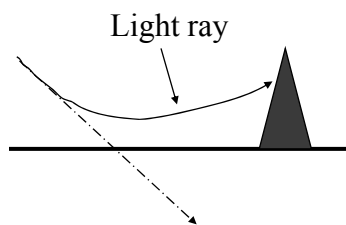
Interaction with matter



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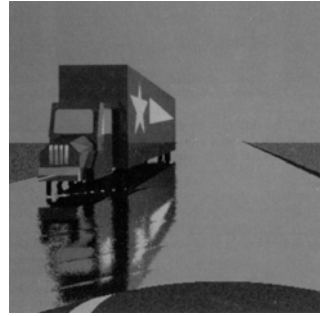
Interaction with matter

- Continuously varying refractive index



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Interaction with matter



(Berger)

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