

## Lecture 15: Many Lights

**CS 6620, Spring 2009**

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### Many Lights

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- Most techniques work for a single light source
- Many light sources
  - For environment maps
  - For indirect illumination
- Treat it as a single integration domain
  - Importance sample lights
  - Importance sampling (with visibility) still hard problem

## Research on many lights

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- Ward '91
- Shirley, Wang, Zimmerman '94
- Fernandez, Bala, Greenberg '02
  - Donikian, Fernandez.. '06
- Lightcuts '05

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## Shirley, Wang, Zimmerman '94

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- Try to avoid linear cost of evaluating lights
- Separate lights into
  - Set of important lights (a small set)
  - Set of “dim” lights (large set)
- Construct pdf using:
  - all important lights
  - 1 out of all the dim lights
- Importance sample these lights

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## Shirley, Wang, Zimmerman '94

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- Region of influence for important lights
  - Octree cells in region of influence have light in important set
- However, the partitioning into important and dim sets remains hard
- Also, still are not taking visibility into account

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## Lightcuts [SIGGRAPH '05,'06]

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- Walter, Fernandez, Arbree, Bala
- Efficient, accurate complex illumination



Environment map lighting & indirect  
Time 111s



Textured area lights & indirect  
Time 98s

(640x480, Anti-aliased, Glossy materials)

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# Scalable

- Scalable solution for many point lights
  - Thousands to millions
  - Sub-linear cost

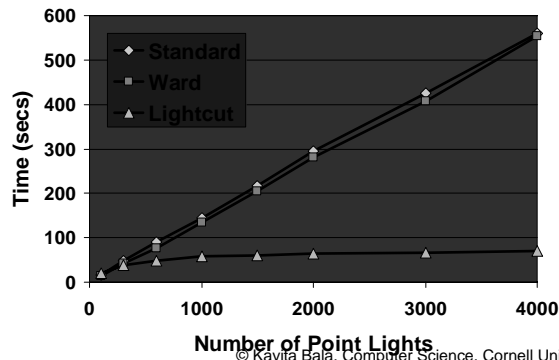


Tableau Scene

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# GI as many-point lights

- Approach: unify illumination
  - Area lights
  - HDR environment maps
  - Sun & sky light
  - Indirect illumination
- Convert to point lights



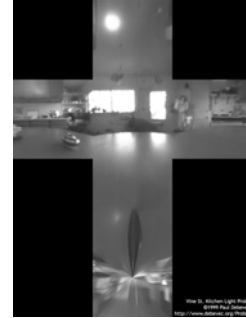
Kitchen light: area, sun/sky, indirect

$$P = \int_{\text{hemisphere}} (\text{indirect} + \text{direct})$$

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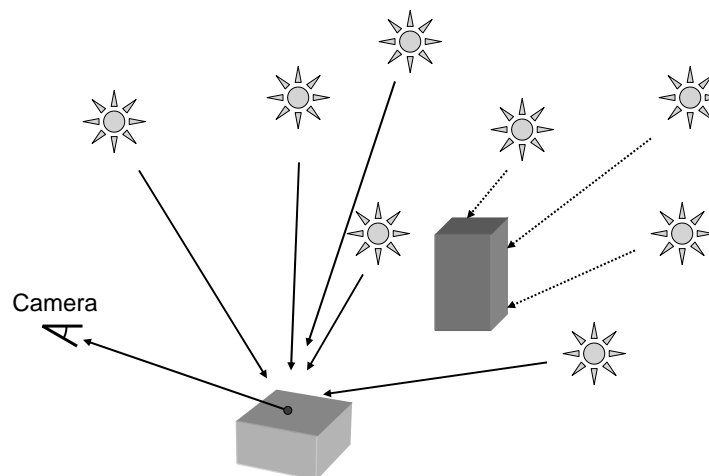
## Convert Illumination

- HDR environment map
  - Apply captured light to scene
  - Convert to directional point lights using [Agarwal et al. 2003]
- Indirect Illumination
  - Convert indirect to direct illumination using Instant Radiosity [Keller 97]
    - Caveats: no caustics, clamping, etc.
  - More lights = more indirect detail



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## Lightcuts Problem



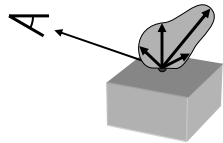
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# Illumination Equation

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$$\text{result} = \sum_{\text{lights}} M_i G_i V_i I_i$$

$M_i$  |  $G_i$  |  $V_i$  |  $I_i$   
Material term | Geometric term | Visibility term | Light intensity



Currently support diffuse, phong, and Ward

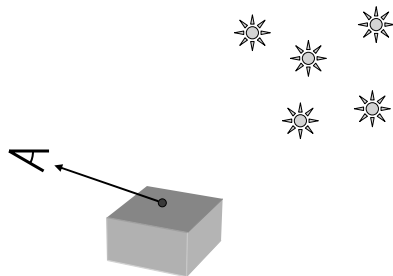
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# Illumination Equation

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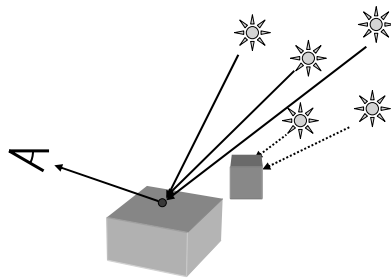


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# Illumination Equation

$$\text{result} = \sum_{\text{lights}} M_i G_i V_i I_i$$

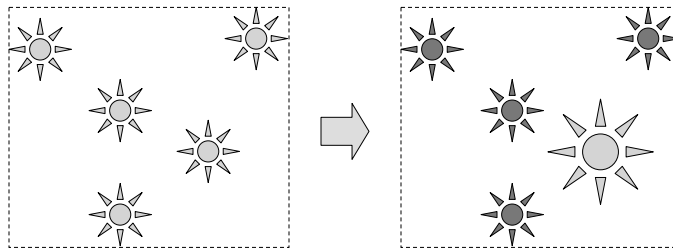
$M_i$  |  $G_i$  |  $V_i$  |  $I_i$   
Material term | Geometric term | Visibility term | Light intensity



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# Key Concepts

- Light Cluster
  - Approximate many lights by a single brighter light (the representative light)

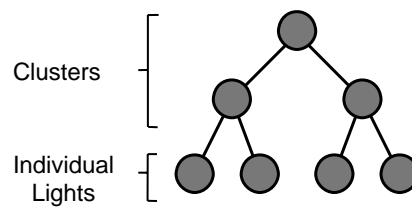


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## Key Concepts

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- Light Cluster
- Light Tree
  - Binary tree of lights and clusters

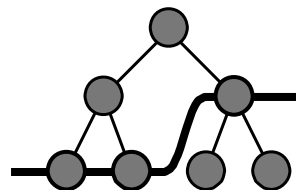


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## Key Concepts

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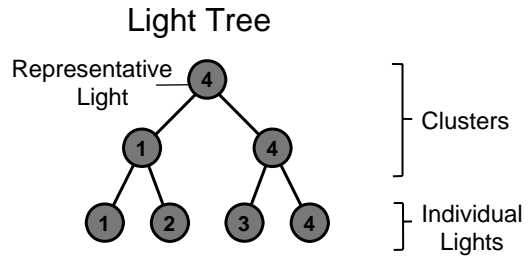
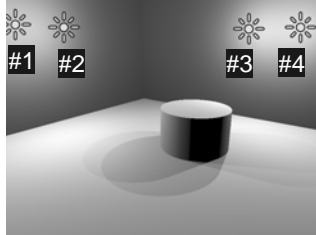
- Light Cluster
- Light Tree
- A Cut
  - A set of nodes that partitions the lights into clusters



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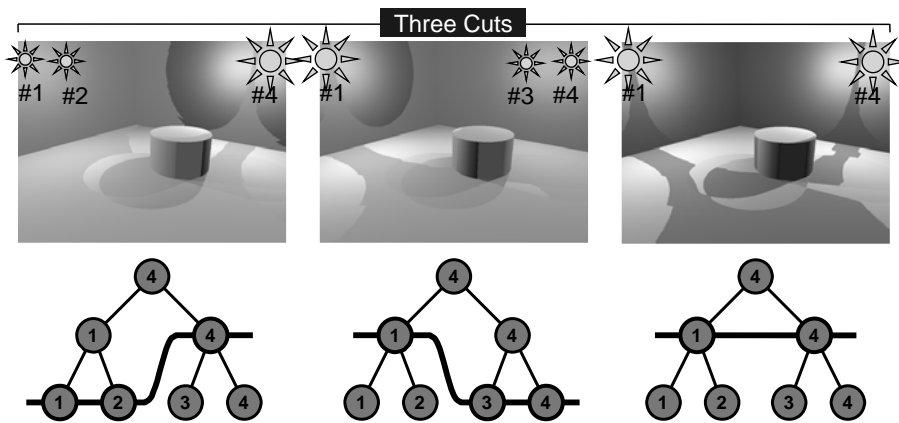


# Simple Example



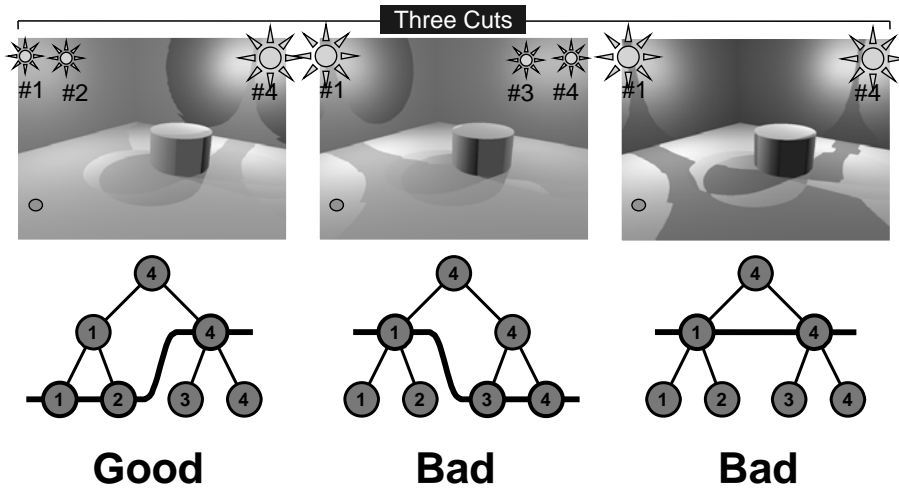
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# Three Example Cuts



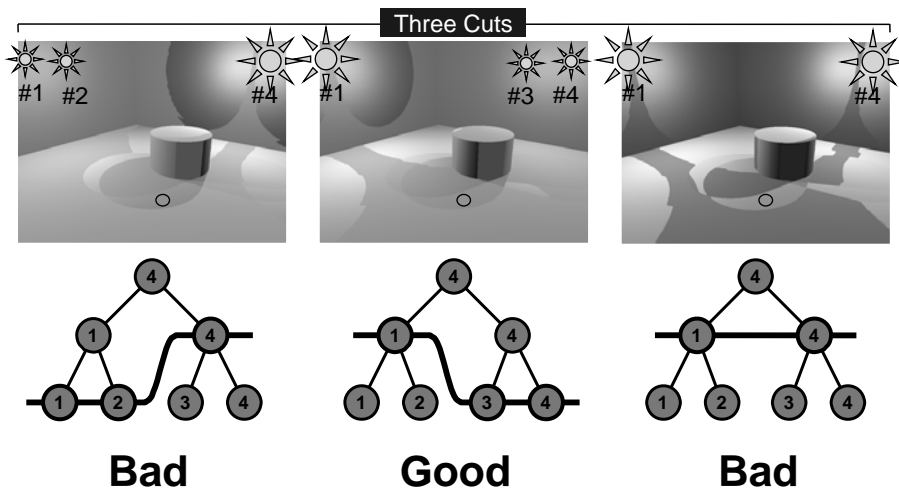
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## Three Example Cuts



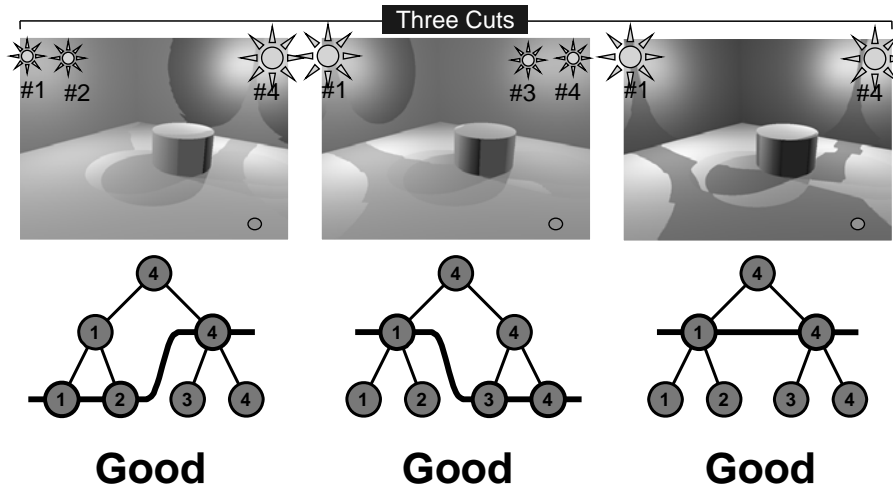
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## Three Example Cuts



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## Three Example Cuts



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## Algorithm Overview

- Pre-process
  - Convert illumination to point lights
  - Build light tree
- For each eye ray
  - Choose a cut to approximate the illumination

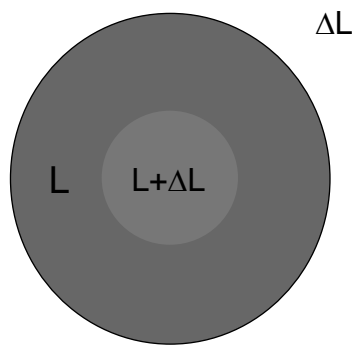
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## Algorithm Overview

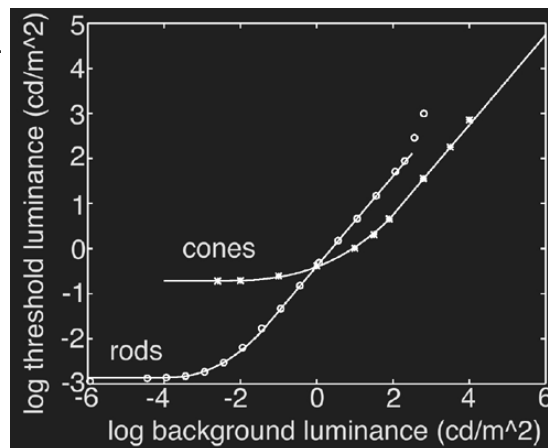
- Pre-process
  - Convert illumination to point lights
  - Build light tree
- For each eye ray
  - Choose a cut to approximate the local illumination
    - Cost vs. accuracy
    - Avoid visible transition artifacts

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## Threshold visibility



$\Delta L = kL$  Weber's law



TVI functions

L

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## Perceptual Metric

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- Weber's Law
  - Contrast visibility threshold is fixed percentage of signal
  - Used 2% in our results
- Ensure each cluster's error < visibility threshold
  - Transitions will not be visible
  - Used to select cut

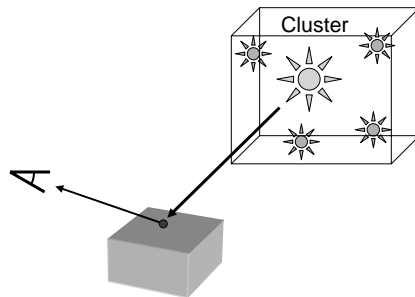
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## Cluster Approximation

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$$\text{result} \approx M_j G_j V_j \sum_{\text{lights}} I_i$$

j is the representative light



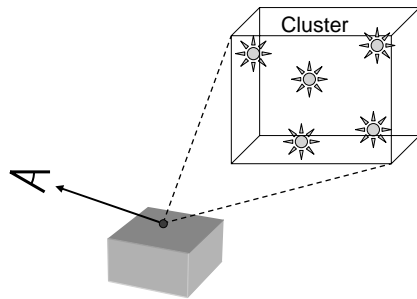
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## Cluster Error Bound

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$$\text{error} \leq M_{\text{ub}} G_{\text{ub}} V_{\text{ub}} \sum_{\text{lights}} I_i$$

- Bound each term
  - Visibility  $\leq 1$  (trivial)
  - Intensity is known
  - Bound material and geometric terms using cluster bounding volume



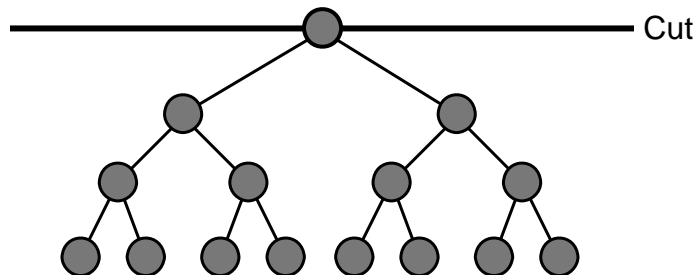
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ub == upper bound

## Cut Selection Algorithm

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- Start with coarse cut (eg, root node)

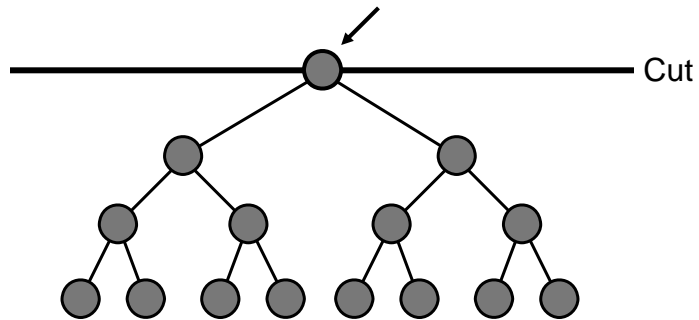


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## Cut Selection Algorithm

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- Select cluster with largest error bound

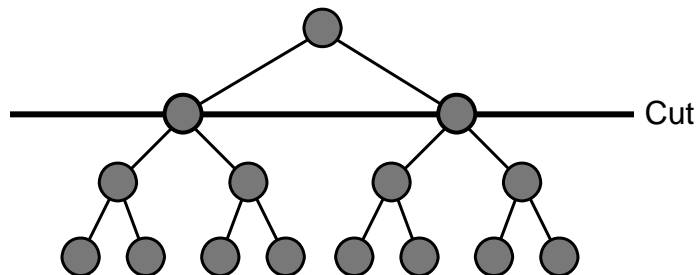


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## Cut Selection Algorithm

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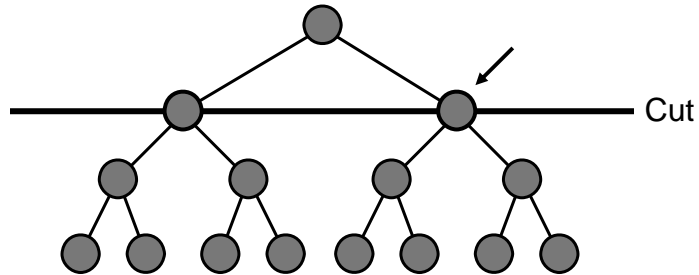
- Refine if error bound  $> 2\%$  of total



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## Cut Selection Algorithm

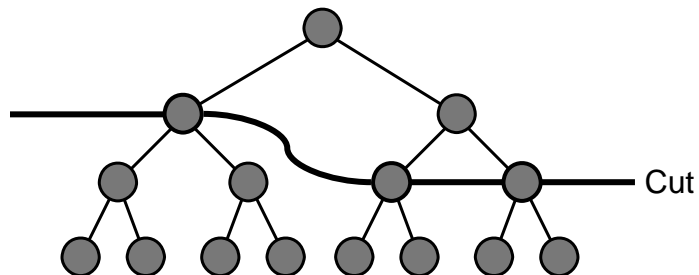
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## Cut Selection Algorithm

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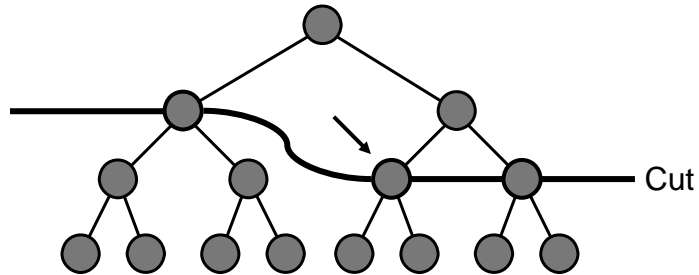


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## Cut Selection Algorithm

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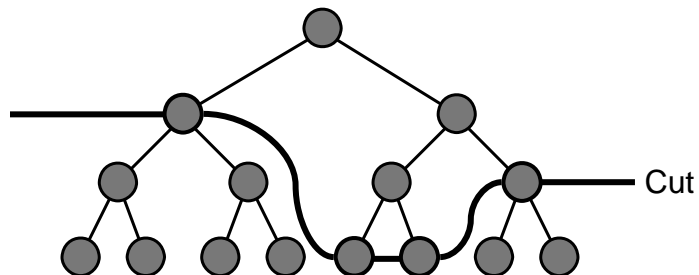


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## Cut Selection Algorithm

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- Repeat until cut obeys 2% threshold



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Kitchen, shadow ray false color

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## Combined Illumination



Lightcuts 128s

4 608 Lights  
(Area lights only)

Avg. 259 shadow rays / pixel



Lightcuts 290s

59 672 Lights  
(Area + Sun/sky + Indirect)

Avg. 478 shadow rays / pixel  
(only 54 to area lights)

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Avg. shadow rays per eye ray 46 (0.03%)  
Grand Central, 1.46M polygons, 143464 lights, (Area+Sun/sky+Indirect)

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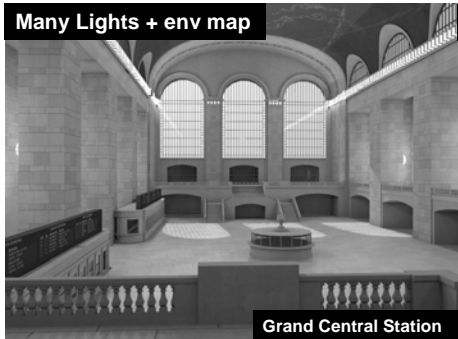
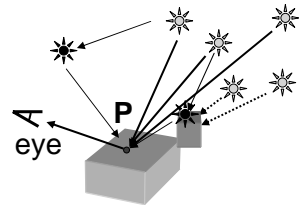
Avg. shadow rays per eye ray 17 (0.13%)  
Tableau, 630K polygons, 13000 lights, (EnvMap+Indirect)

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## Problem: Many Lights and GI

$$\int_{\text{hemisphere}(\text{indirect} + \text{direct})}$$



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# AA, Volumetric, Motion Blur, DOF

$$\text{Pixel} = \int_{\text{aperture}} \int_{\text{time}} \int_{\text{volume}}$$

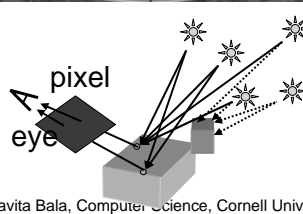
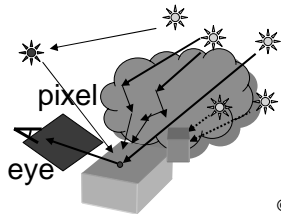
**Volumetric: Fog**



**Motion Blur**



**Depth-of-Field**



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# How to scale to complexity?



**If you can't see it,  
don't compute it**

Kalabsha temple, Egypt

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**More** complexity is **Less** visually salient



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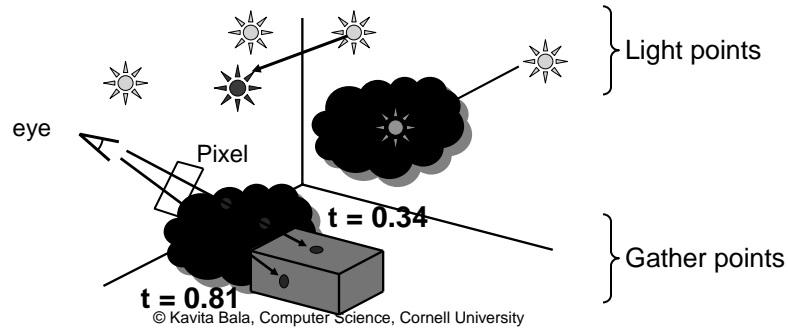
**More is Less**



# Multidimensional LC[SIG'06]

$$\text{Pixel} = \int_{\text{aperture}} \int_{\text{time}} \int_{\text{volume}}$$

- Discretize full integral into 2 point sets
  - Light points (**L**)
  - Gather points (**G**)

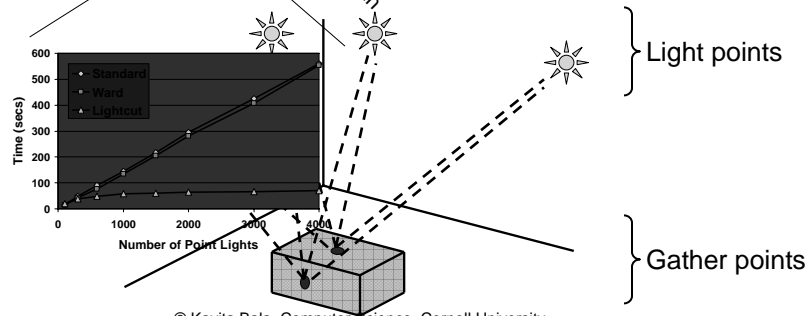


# Multidimensional problem

- Sum of all pairs of gather and light points

$$\text{Pixel} = \sum_{(j,i) \in \mathbf{G} \times \mathbf{L}} S_j k_{ji} I_i$$

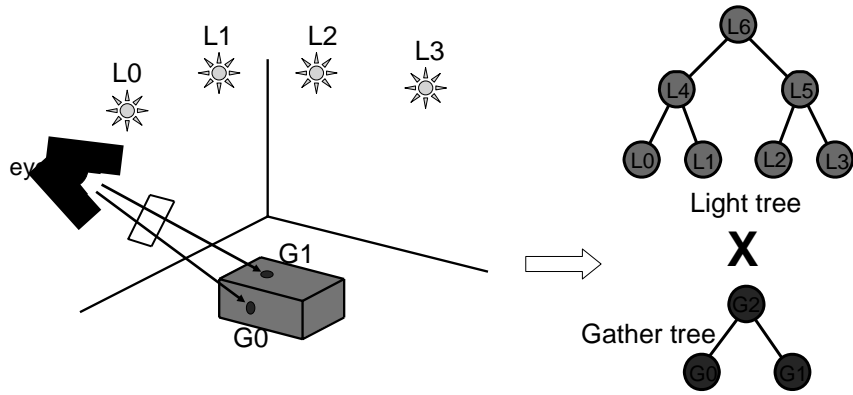
$S_j$  Gather strength      $k_{ji}$  Weight of ray      $I_i$  Light intensity





# Product Graph

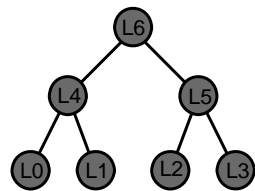
- Explicit hierarchy would be too expensive
- Use implicit hierarchy: product graph



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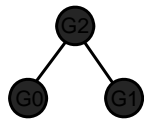
# Product Graph

Cartesian product of two trees (g)



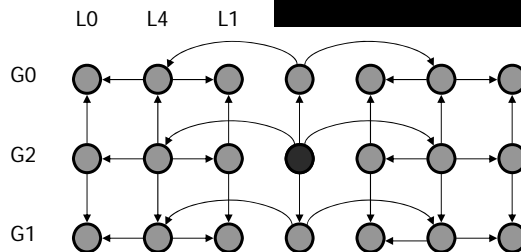
Light tree

**X**



Gather tree

=



Refine "cut" until perceptual threshold  
Generalize cut, representative, error bounds

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