# **CS5670: Computer Vision**

Image Classification



Some Slides from Fei-Fei Li, Justin Johnson, Serena Yeung <u>http://vision.stanford.edu/teaching/cs231n/</u>

# References

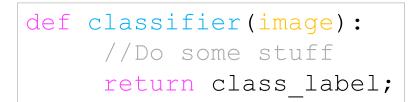
• Stanford CS231N

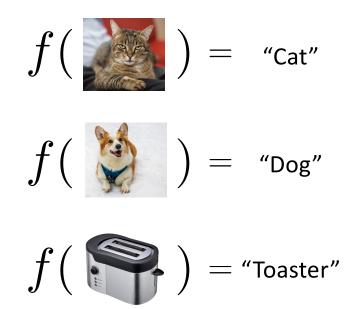
<u>http://cs231n.stanford.edu/</u>

• Many slides courtesy of Abe Davis

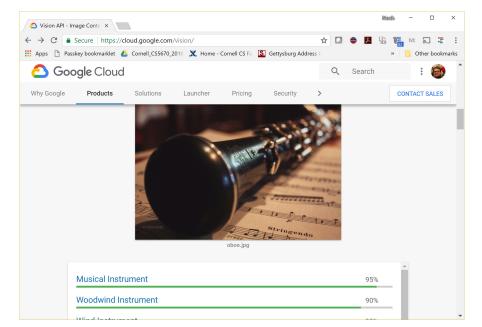
## Image classifiers in a nutshell

- Input: an image
- Output: the class label for that image
- Label is generally one or more of the discrete labels used in training
  - e.g. {cat, dog, cow, toaster, apple, tomato, truck, ... }





#### Image classification demo



#### https://cloud.google.com/vision/docs/drag-and-drop

See also:

https://aws.amazon.com/rekognition/

https://www.clarifai.com/

https://azure.microsoft.com/en-us/services/cognitive-services/computer-vision/

•••

#### **The Semantic Gap**



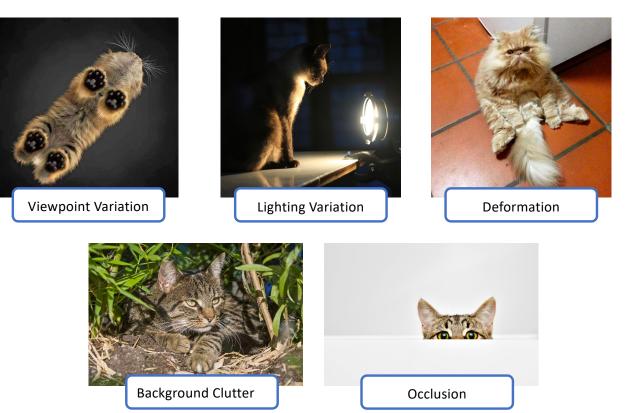
What we see

JTTTO TTTOTOOTOTTT r oroor rrrororrr( J0707077770777077( PICOTITICOI I OI I( POT TITOT TOOTOOTO] 10077777 700077700] ]07007007007770007] 10000 J000JJ70JJ70( 0770000007777 7 ][ ) JOJJOOJ OJOOJJ ][ PT TOOOT TTTT 101] JTTT TOTOTO TOTTT ]00070707070707070] 1007 7777000070 77( JOTTTTOOOOTTTT TTO]

What the computer sees

#### **Variation Makes Recognition Hard**

• The same class of object can appear *very* differently in different images



## The Problem is Under-constrained

- Distinct realities can produce the same image...
- We generally can't compute the "right" answer, but we can compute the most likely one...
- We need some kind of prior to condition on. We can learn this prior from data:

$$f(x) = \underset{\ell_x}{\operatorname{argmax}} P(\ell_x | data)$$

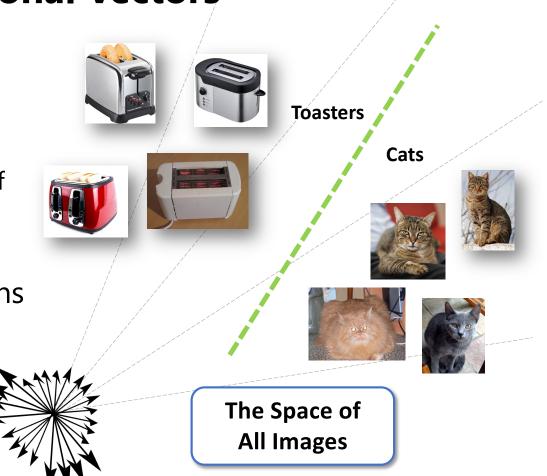




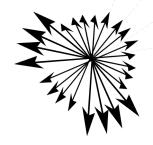
- An image is just a bunch of numbers
- Let's stack them up into a vector
  - Our training data is just a bunch of high-dimensional points now



- An image is just a bunch of numbers
- Let's stack them up into a vector
  - Our training data is just a bunch of high-dimensional points now
- Divide space into different regions for different classes



- An image is just a bunch of numbers
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- Divide space into different regions for different classes



The Space of All Images

**TOASTER CAT** 

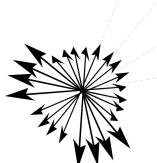
YOUR ARGUMENT IS INVALID

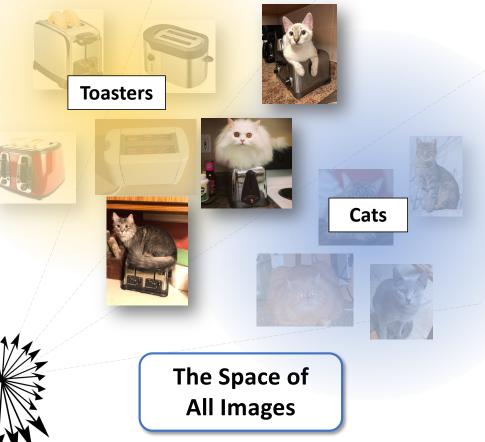


- An image is just a bunch of numbers
- Let's stack them up into a vector
  - Our training data is just a bunch of high-dimensional points now
- Divide space into different regions for different classes

#### or

 Define a distribution over space for each class





### Image Features and Dimensionality Reduction

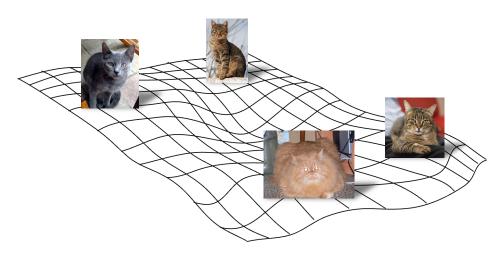
- How high-dimensional is an image?
  - Let's consider an iPhone X photo:
    - 4032 x 3024 pixels
    - Every pixel has 3 colors
    - 36,578,304 pixels (36.5 Mega pixels)
- In practice, images sit on a lowerdimensional manifold
- Think of image features and dimensionality reduction as ways to represent images by their location on such manifolds



The Space of All Images

#### **Image Features and Dimensionality Reduction**

- How high-dimensional is an image?
  - Let's consider an iPhone X photo:
    - 4032 x 3024 pixels
    - Every pixel has 3 colors
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- In practice, images sit on a lowerdimensional manifold
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Side Note: This also lets us deal with images of different sizes, crops, etc.

## **Training & Testing a Classifier**

- Collect a database of images with labels
- Use ML to train an image classifier
- Evaluate the classifier on test images

catdogmughatImage: Image: Image:

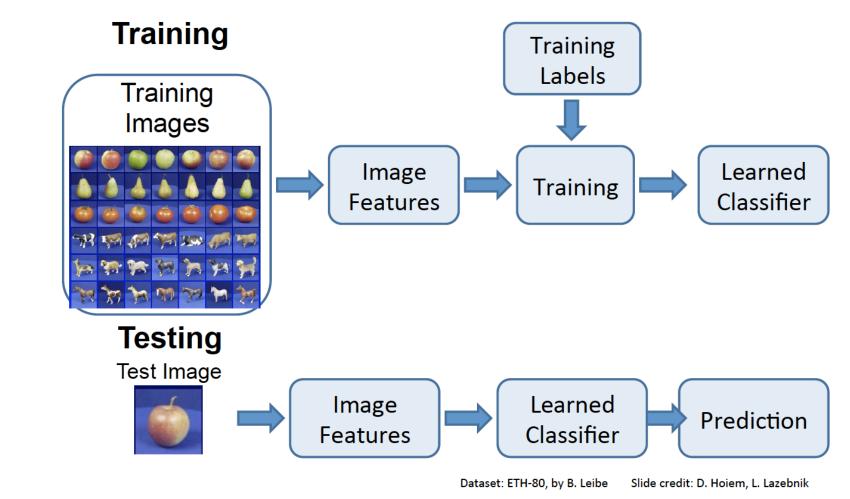
Example training set

#### Training Images Image Image Features Image Features Image Im

#### **Training & Testing a Classifier**

Dataset: ETH-80, by B. Leibe S

Slide credit: D. Hoiem, L. Lazebnik



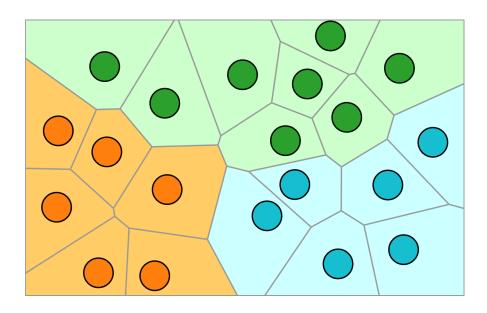
#### **Training & Testing a Classifier**

## Classifiers

- Nearest Neighbor
- kNN ("k-Nearest Neighbors")
- Linear Classifier
- Neural Network
- Deep Neural Network
- Transformers
- ...

## First idea: Nearest Neighbor (NN) Classifier

- Train
  - Remember all training images and their labels
- Predict
  - Find the closest (most similar) training image
  - Predict its label as the true label



#### **CIFAR-10 and NN results**

Example dataset: CIFAR-10 10 labels 50,000 training images 10,000 test images.

| airplane   | 🛁 🐹 🌉 📈 🍬 = 🛃 🎆 🛶 😂                      |
|------------|--|
| automobile | an 😂 🚵 💁 🔤 🜌 🚔 🐝                         |
| bird       | S 🗾 🖉 🕺 🚑 S 😵 🔛 🐙                        |
| cat        | Ni N |
| deer       | M M M M M M M M M M M M M M M M M M M    |
| dog        | N 🔊 🐔 🐘 🎘 🏹 🧑 🚺 🌋                        |
| frog       |  |
| horse      | 📲 🗶 🕸 🚵 🕅 📷 🖙 🛣 🌋 🐲                      |
| ship       | 🗃 😼 🚈 📥 🚔 🕪 💋 🖉 🙇                        |
| truck      | 🛁 🍱 🚛 🌉 👹 🔤 📷 🖓                          |

#### **CIFAR-10 and NN results**

Example dataset: CIFAR-10 10 labels 50,000 training images 10,000 test images.

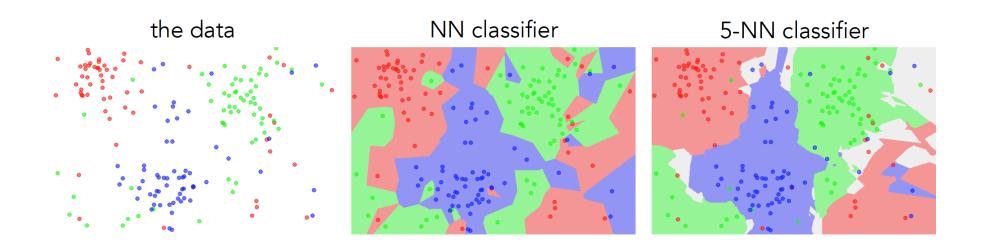
| airplane   | 🚧 🐹 🚒 📈 🏏 = 🛃 🔐 🛶 😂                      |
|------------|--|
| automobile | an 😂 🧱 🤮 🕹 🔛 🐝 🛸 🐝                       |
| bird       | S 🖬 🖉 🕺 🚑 🔨 🌮 🔄 📐 🐖                      |
| cat        | in i |
| deer       | M M M M M M M M M M M M M M M M M M M    |
| dog        | N 🕼 🦔 🦳 🎘 🏹 🔊 🛣                          |
| frog       | Se S |
| horse      | 🕋 🗶 🔯 🔛 👘 📷 🖙 🐼 🐞                        |
| ship       | 🗃 😼 🚈 📥 📥 🥩 🖉 🚈 🙇                        |
| truck      | i i i i i i i i i i i i i i i i i i i    |

# For every test image (first column), examples of nearest neighbors in rows

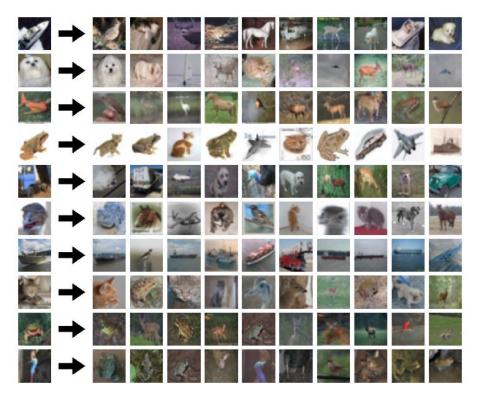


#### k-nearest neighbor

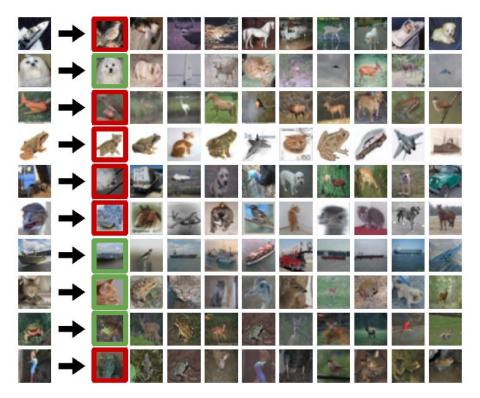
- Find the k closest points from training data
- Take **majority vote** from K closest points



What does this look like?



What does this look like?



#### **How to Define Distance Between Images**

L1 distance:

$$d_1(I_1,I_2) = \sum_p |I_1^p - I_2^p|$$

Where  $I_1$  denotes image 1, and p denotes each pixel

| ĺ., | test image |    |     |     |  |  |
|-----|------------|----|-----|-----|--|--|
|     | 56         | 32 | 10  | 18  |  |  |
|     | 90         | 23 | 128 | 133 |  |  |
|     | 24         | 26 | 178 | 200 |  |  |
|     | 2          | 0  | 255 | 220 |  |  |

| training image |    |     |     |  |  |  |
|----------------|----|-----|-----|--|--|--|
| 10             | 20 | 24  | 17  |  |  |  |
| 8              | 10 | 89  | 100 |  |  |  |
| 12             | 16 | 178 | 170 |  |  |  |
| 4              | 32 | 233 | 112 |  |  |  |

pixel-wise absolute value differences

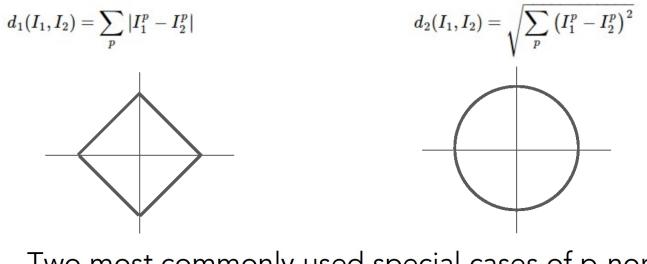
|   | 46 | 12 | 14 | 1   |       |
|---|----|----|----|-----|-------|
|   | 82 | 13 | 39 | 33  | 450   |
| - | 12 | 10 | 0  | 30  | → 456 |
|   | 2  | 32 | 22 | 108 |       |
|   |    |    |    |     |       |

#### **Choice of distance metric**

• Hyperparameter

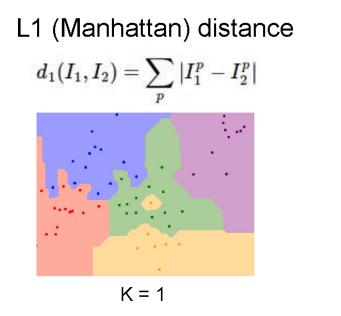
L1 (Manhattan) distance

L2 (Euclidean) distance

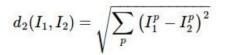


- Two most commonly used special cases of p-norm  $||x||_p = \left(|x_1|^p + \dots + |x_n|^p\right)^{\frac{1}{p}} \quad p \ge 1, x \in \mathbb{R}^n$ 

#### K-Nearest Neighbors: Distance Metric



L2 (Euclidean) distance





Demo: http://vision.stanford.edu/teaching/cs231n-demos/knn/

#### Hyperparameters

- What is the **best distance** to use?
- What is the **best value of k** to use?
- These are **hyperparameters**: choices about the algorithm that we set rather than learn
- How do we set them?
  - One option: try them all and see what works best

Idea #1: Choose hyperparameters that work best on the data

Your Dataset

Idea #1: Choose hyperparameters that work best on the data

**BAD**: K = 1 always works perfectly on training data

Your Dataset

**Idea #1**: Choose hyperparameters that work best on the data

**BAD**: K = 1 always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, choose hyperparameters that work best on test data

| train test |  |
|------------|--|
|------------|--|

|              | <b>D</b> : K = 1 always works<br>rfectly on training data |
|--------------|---|
| Your Dataset |   |
|              | <b>D</b> : No idea how algorithm<br>I perform on new data |
| train        | test  |

| Idea #1: Choose hyperparameters that work best on the data   |                                | = 1 always wor<br>on training dat |  |  |
|--|--------------------------------|-----------------------------------|--|--|
| Your Dataset   |                                |                                   |  |  |
| Idea #2: Split data into <b>train</b> and <b>test</b> , choose hyperparameters that work best on test data | idea how algo<br>rm on new dat |                                   |  |  |
| train  | test                           |                                   |  |  |
| Idea #3: Split data into train, val, and test; choose Better!  |                                |                                   |  |  |
| train  | test                           |                                   |  |  |

Your Dataset

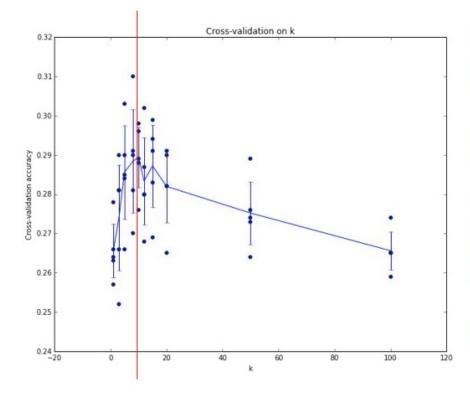
#### Idea #4: Cross-Validation: Split data into folds,

try each fold as validation and average the results

| fold 1 | fold 2 | fold 3 | fold 4 | fold 5 | test |
|--------|--------|--------|--------|--------|------|
| fold 1 | fold 2 | fold 3 | fold 4 | fold 5 | test |
| fold 1 | fold 2 | fold 3 | fold 4 | fold 5 | test |

Useful for small datasets, but not used too frequently in deep learning

#### **Hyperparameter Tuning**



Example of 5-fold cross-validation for the value of **k**.

Each point: single outcome.

The line goes through the mean, bars indicated standard deviation

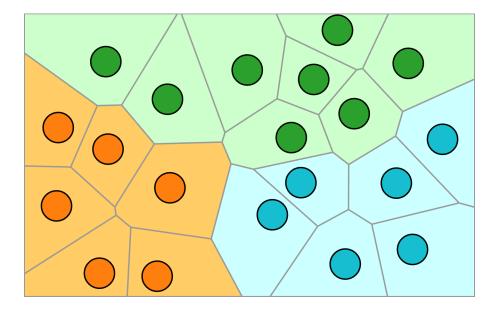
(Seems that k ~= 7 works best for this data)

## **Recap: How to pick hyperparameters?**

- Methodology
  - Train and test
  - Train, validate, test
- Train an initial model
- Validate to find hyperparameters
- Test to understand generalizability

## kNN – Complexity and Storage

- N training images, M test images
- Training: O(1)
- Testing: O(MN)
- We often need the opposite:
  - Slow training is ok
  - Fast testing is necessary

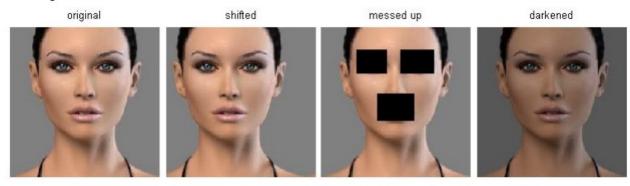


# k-Nearest Neighbors: Summary

- In **image classification** we start with a **training set** of images and labels, and must predict labels on the **test set**
- The **K-Nearest Neighbors** classifier predicts labels based on nearest training examples
- Distance metric and K are **hyperparameters**
- Choose hyperparameters using the validation set; only run on the test set once at the very end!

### **Problems with KNN: Distance Metrics**

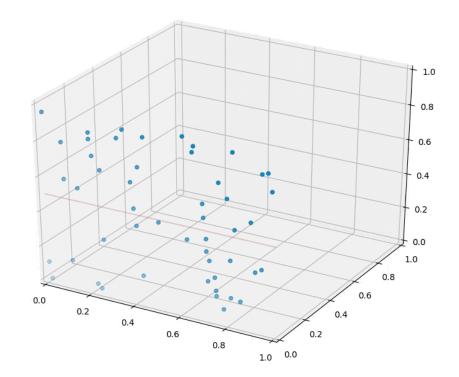
- terrible performance at test time
- distance metrics on level of whole images can be very unintuitive



(all 3 images have same L2 distance to the one on the left)

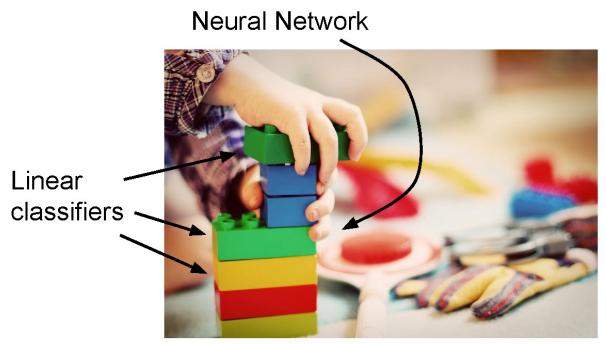
# **Problems with KNN: The Curse of Dimensionality**

- As the number of dimensions increases, the same amount of data becomes more sparse.
- Amount of data we need ends up being exponential in the number of dimensions



Animation from https://www.cs.cornell.edu/courses/cs4780/2018fa/lectures/lecturenote02 kNN.html

# **Linear Classifiers**

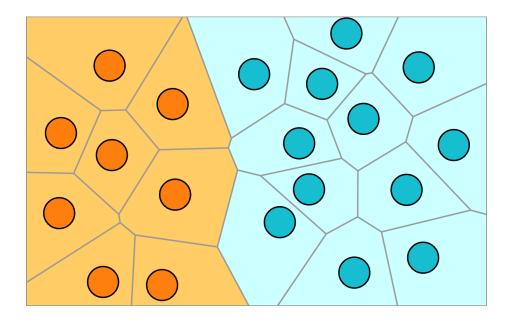


This image is <u>CC0 1.0</u> public domain

# Linear Classification vs. Nearest Neighbors

#### • Nearest Neighbors

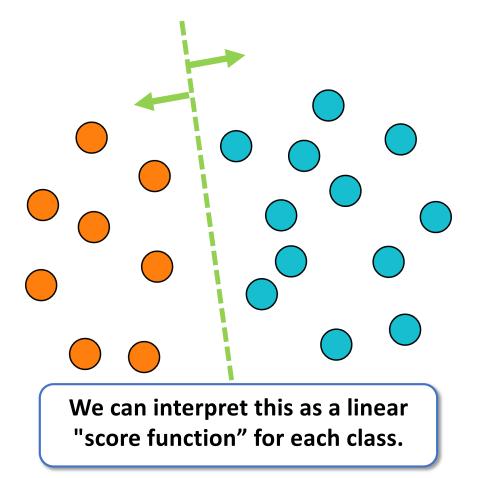
- Store every image
- Find nearest neighbors at test time, and assign same class



# **Linear Classification vs. Nearest Neighbors**

#### • Nearest Neighbors

- Store every image
- Find nearest neighbors at test time, and assign same class
- Linear Classifier
  - Store hyperplanes that best separate different classes
  - We can compute continuous class score by calculating (signed) distance from hyperplane



### **Score functions**



#### class scores

### **Parametric Approach**

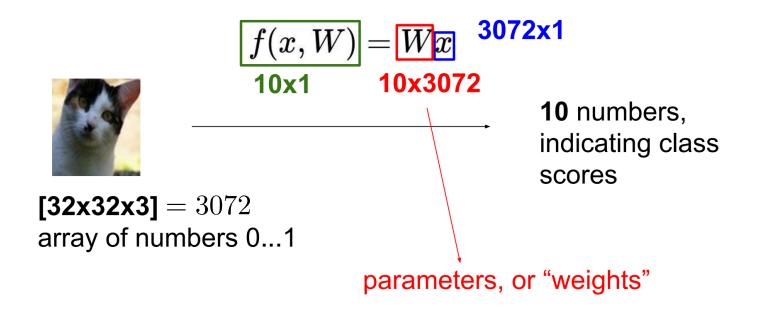


image parameters
f(x,W)

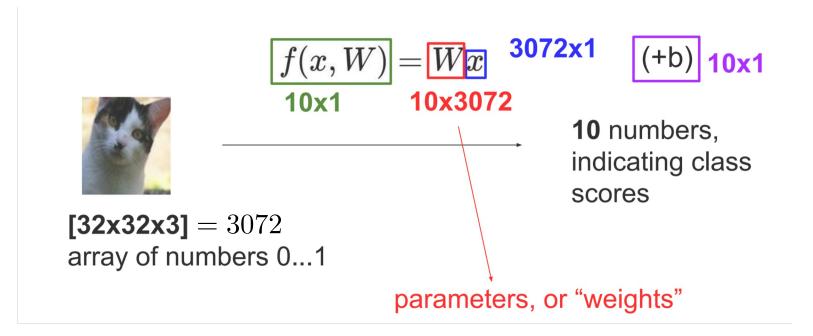
**10** numbers, indicating class scores

[32x32x3] = 3072array of numbers 0...1 (3072 numbers total)

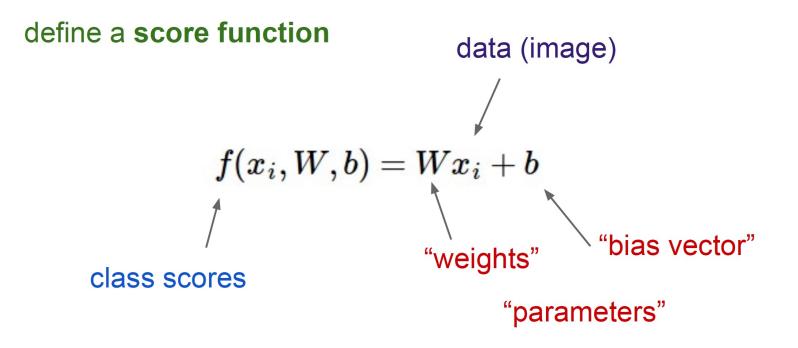
### **Parametric Approach: Linear Classifier**



### **Parametric Approach: Linear Classifier**

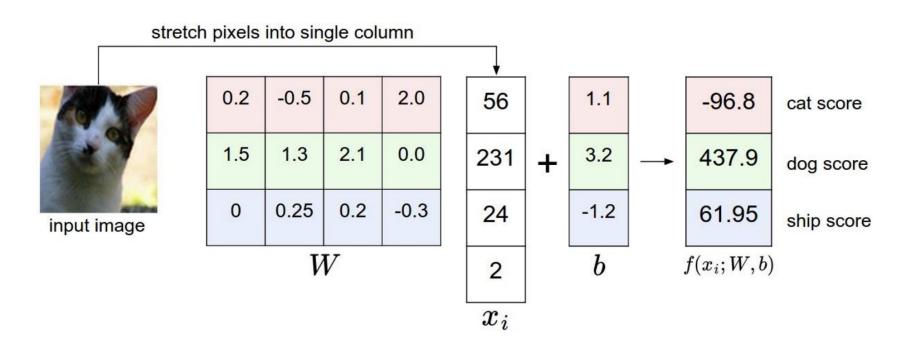


### **Linear Classifier**



#### **Interpretation: Algebraic**

Example with an image with 4 pixels, and 3 classes (cat/dog/ship)

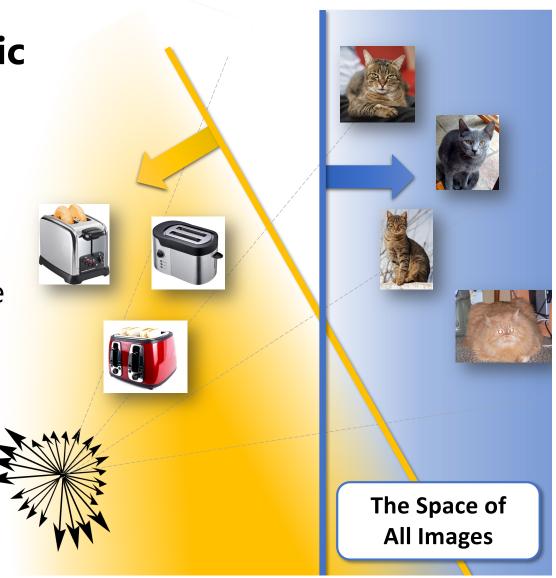


# **Interpretation: Geometric**

• Parameters define a hyperplane for each class:

 $f(x_i, W, b) = Wx_i + b$ 

 We can think of each class score as defining a distribution that is proportional to distance from the corresponding hyperplane



# Hard Cases for a Linear Classifier

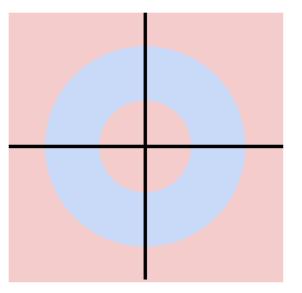
Class 1: First and third quadrants

#### Class 2:

Second and fourth quadrants

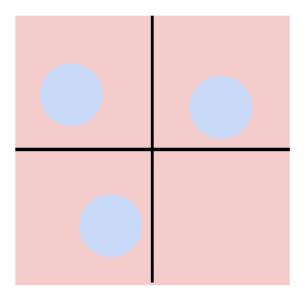
Class 1: 1 <= L2 norm <= 2

Class 2: Everything else



Class 1: Three modes

Class 2: Everything else



### **Interpretation: Template matching**

• We can think of the rows in  $\!W\!$  as templates for each class

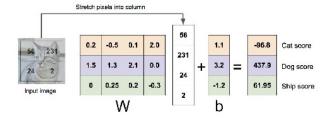


Rows of W in  $f(x_i, W, b) = Wx_i + b$ 

### Linear Classifier: Three Viewpoints

Algebraic Viewpoint

f(x,W) = Wx



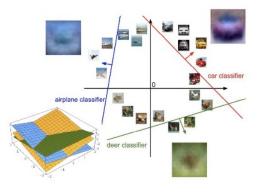
Visual Viewpoint

One template per class



Geometric Viewpoint

Hyperplanes cutting up space



# **So far**: Defined a (linear) <u>score function</u> f(x,W) = Wx + b

Example class scores for 3 images for some W:

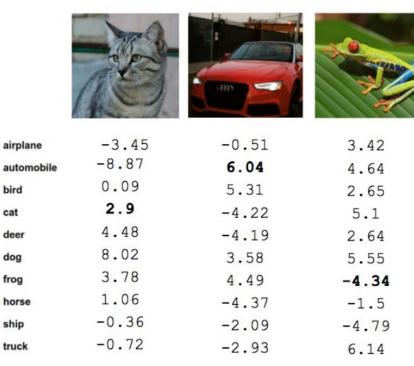
How can we tell whether this W is good or bad?

Cat image by <u>Nikita</u> is licensed under <u>CC-BY 2.0</u> Car image is <u>CC0 1.0</u> public domain <u>Frod image</u> is in the public domain



| airplane   | -3.45 | -0.51 | 3.42  |
|------------|-------|-------|-------|
| automobile | -8.87 | 6.04  | 4.64  |
| bird       | 0.09  | 5.31  | 2.65  |
| cat        | 2.9   | -4.22 | 5.1   |
| deer       | 4.48  | -4.19 | 2.64  |
| dog        | 8.02  | 3.58  | 5.55  |
| frog       | 3.78  | 4.49  | -4.34 |
| horse      | 1.06  | -4.37 | -1.5  |
| ship       | -0.36 | -2.09 | -4.79 |
| truck      | -0.72 | -2.93 | 6.14  |

### **Linear classification**



Cat image by Nikita is licensed under CC-BY 2.0; Car image is CC0 1.0 public domain; Frog image is in the public domain

#### Output scores

#### TODO:

- Define a loss function that quantifies our unhappiness with the scores across the training data.
- Come up with a way of efficiently finding the parameters that minimize the loss function. (optimization)

#### Loss functions

Suppose: 3 training examples, 3 classes. With some W the scores f(x, W) = Wx are:



2.2

2.5

1.3 3.2 cat 5.1 4.9 car -3.1 -1.7 2.0 frog

A loss function tells how good our current classifier is

Given a dataset of examples  $\{(x_i, y_i)\}_{i=1}^N$ 

Where  $x_i$  is image and  $y_i$  is (integer) label

Loss over the dataset is a sum of loss over examples:

$$L = \frac{1}{N} \sum_{i} L_i(f(x_i, W), y_i)$$

# Loss function, cost/objective function

- Given ground truth labels ( $y_i$ ), scores  $f(x_i, \mathbf{W})$ 
  - how unhappy are we with the scores?
- Loss function or objective/cost function measures unhappiness
- During training, want to find the parameters W that minimize the loss function

# Simpler example: binary classification

- Two classes (e.g., "cat" and "not cat")
  - AKA "positive" and "negative" classes





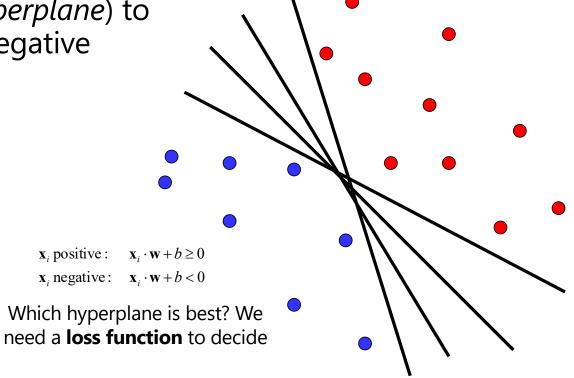




not cat

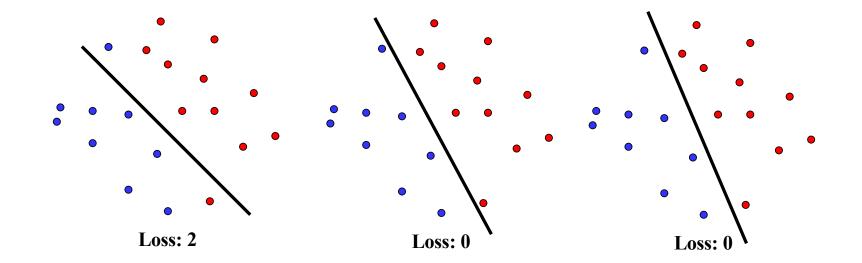
# **Linear classifiers**

• Find linear function (*hyperplane*) to separate positive and negative examples



# What is a good loss function?

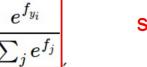
- One possibility: Number of misclassified examples
  - Problems: discrete, can't break ties
  - We want the loss to lead to good generalization
  - We want the loss to work for more than 2 classes



### **Softmax classifier**

 Interpret Scores as unnormalized log probabilities of classes

$$f(x_i, W) = Wx_i$$
 (score function)



softmax function

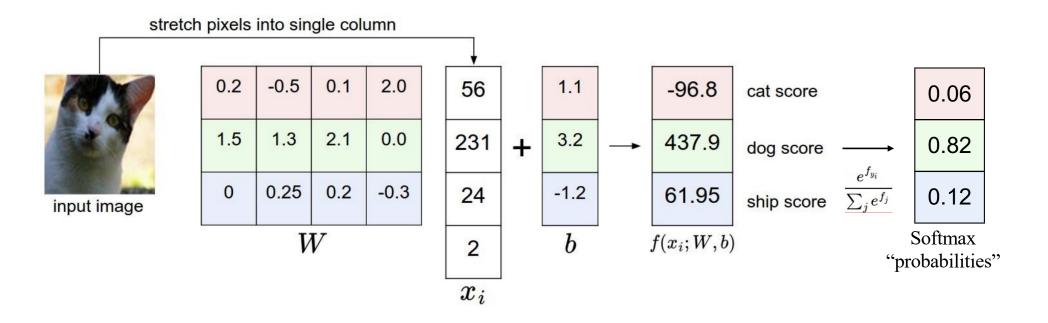
Squashes values into probabilities  $P(y_i \mid x_i; W)$ ranging from 0 to 1

Example with three classes:

 $[1,-2,0] 
ightarrow [e^1,e^{-2},e^0] = [2.71,0.14,1] 
ightarrow [0.7,0.04,0.26]$ 

# **Softmax classifier**

#### Example with an image with 4 pixels, and 3 classes (cat/dog/ship)



**Cross-entropy loss** 

 $f(x_i, W) = W x_i$  (score function)

#### **Cross-entropy loss**

 $f(x_i, W) = W x_i$  (score function)  $L_i = -\log\left(\frac{e^{f_{y_i}}}{\sum_j e^{f_j}}\right)^{f_{y_i}: \text{ score of correct class}}$  $L_i = -f_{y_i} + \log\sum_j e^{f_j}$  We call  $L_i$  crossentropy loss

#### **Cross-entropy loss**

 $f(x_i, W) = Wx_i$  (score function)

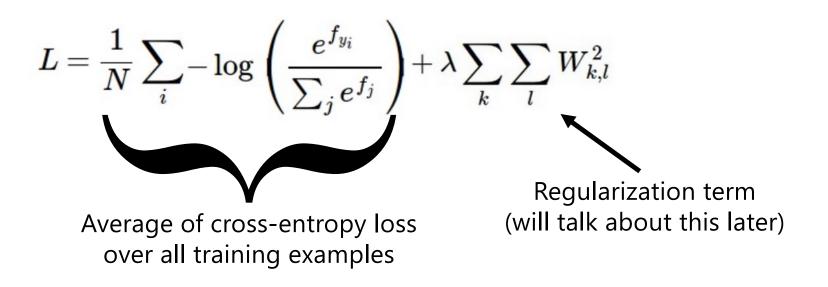
$$\begin{split} L_{i} = -\log\left(\frac{e^{f_{y_{i}}}}{\sum_{j}e^{f_{j}}}\right) & L_{i} = -f_{y_{i}} + \log\sum_{j}e^{f_{j}} & \text{We call } L_{i} \, cross-entropy \, loss \\ & \bullet & \bullet & \bullet \\ P(y_{i} \mid x_{i}; W) & \text{i.e. we're minimizing} \\ & \text{the negative log} \\ & \text{likelihood.} \end{split}$$

#### Losses

- Cross-entropy loss is just one possible loss function
  - One nice property is that it reinterprets scores as probabilities, which have a natural meaning
- SVM (max-margin) loss functions also used to be popular
  - But currently, cross-entropy is the most common classification loss

# Summary

- Have score function and loss function
  - Currently, score function is based on linear classifier
  - Next, will generalize to convolutional neural networks
- Find W and b to minimize loss



# **Questions?**