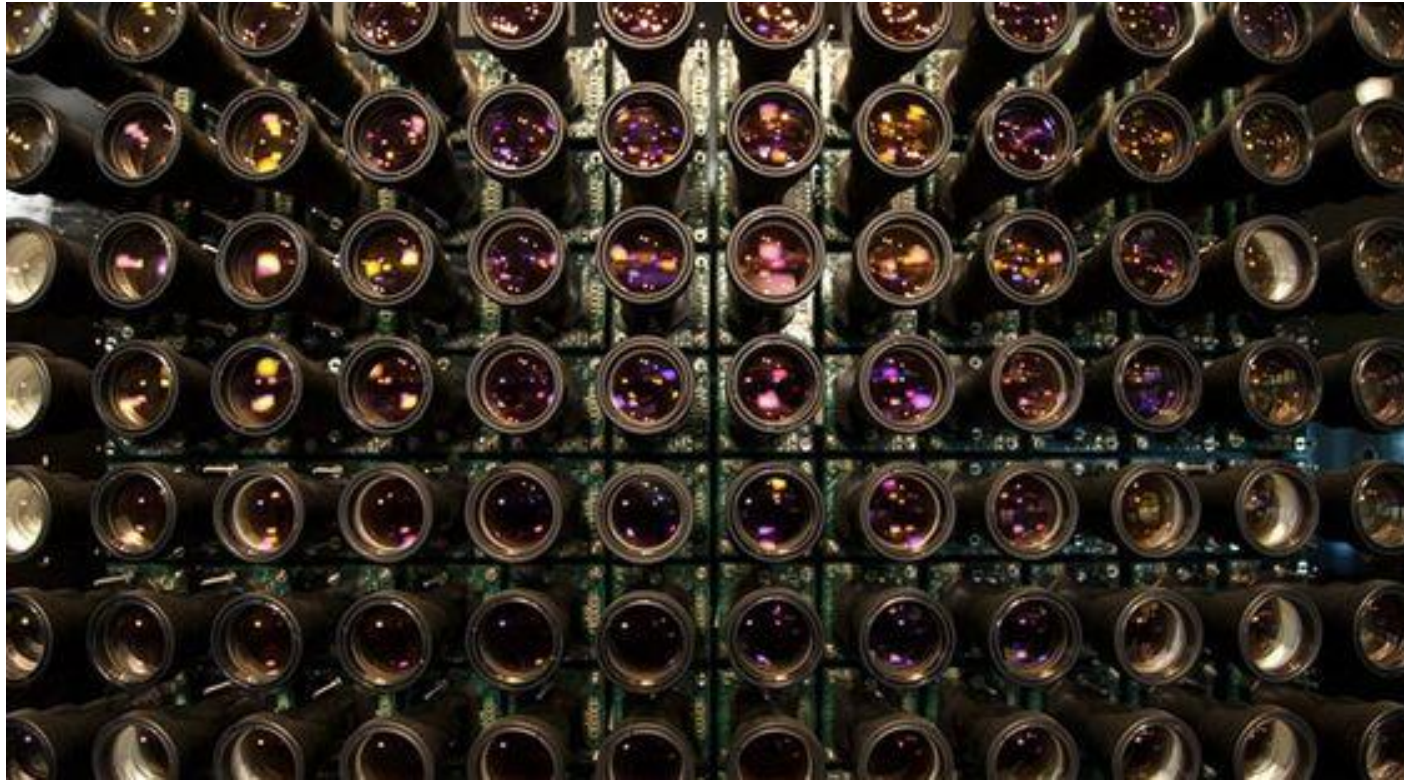


# CS5670: Computer Vision

## Multi-view stereo



Stanford Multi-Camera Array

<http://graphics.stanford.edu/projects/array/>

# Announcements

- Project 3 due this Friday, April 2 at 7pm (code), Monday, April 5 at 7pm (artifact)
- Project 4 (Stereo) to be released next Wednesday, April 7, due Tuesday, April 20, by 7pm
  - To be done in groups of two
- Please file midterm regrade requests in Gradescope

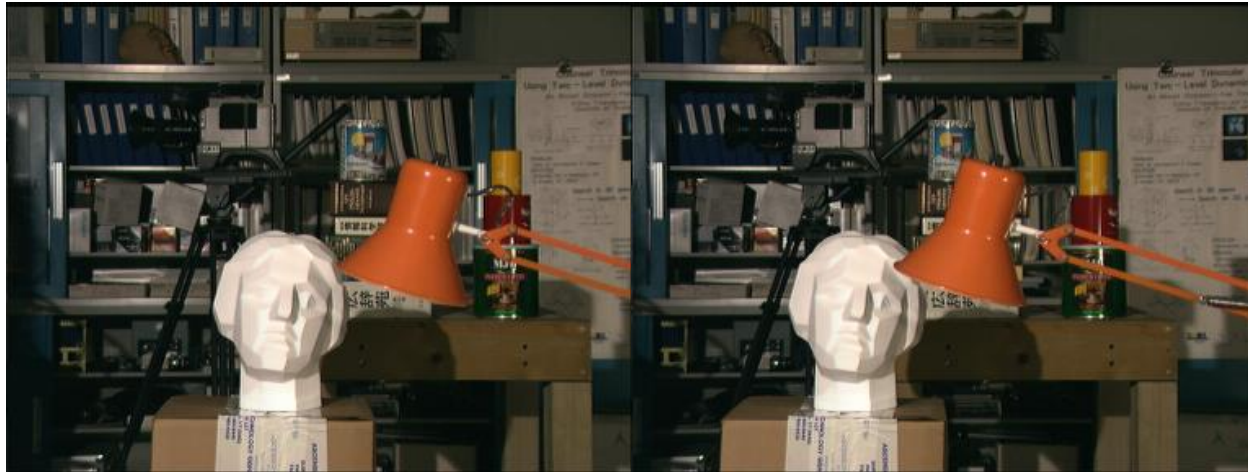
# Questions?

- Go to [sli.do](https://sli.do) and enter code `cs5670`

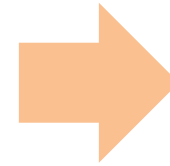
# Recommended Reading

- Szeliski (1<sup>st</sup> Edition) Chapter 11.6
- *Multi-View Stereo: A Tutorial*, Furukawa and Hernandez, 2015
  - [http://carlos-hernandez.org/papers/fnt\\_mvs\\_2015.pdf](http://carlos-hernandez.org/papers/fnt_mvs_2015.pdf)

# Last time: Binocular (Two-View) Stereo



Left-right (rectified) stereo pair

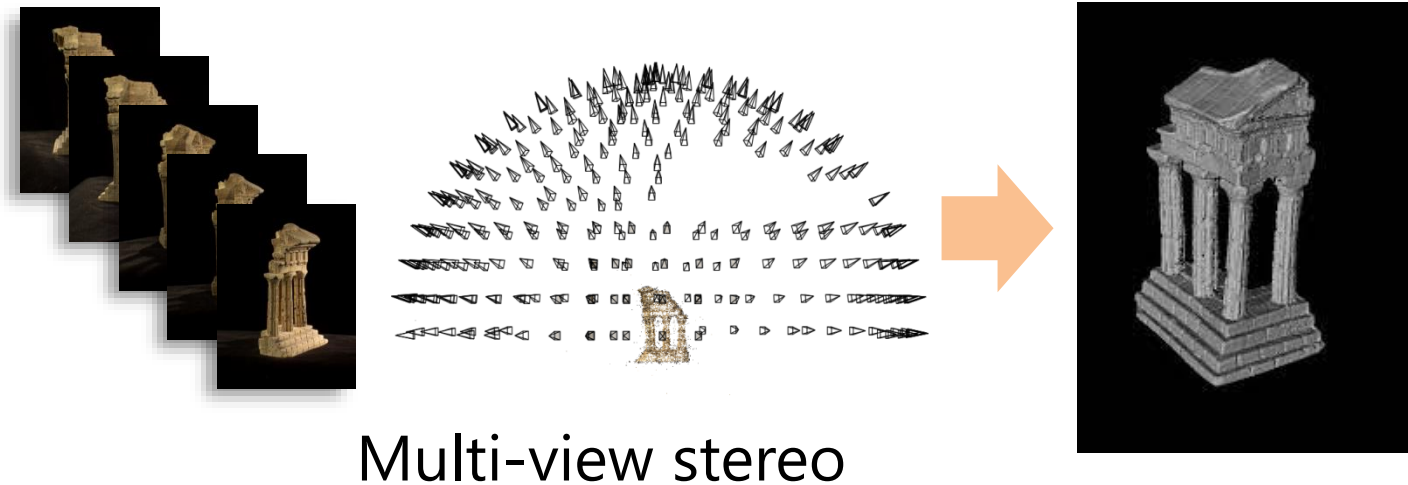


Computed disparity map

Useful for robot perception and navigation, video effects, etc.

# Multi-view Stereo

**Problem formulation:** given several images of the same object or scene, compute a representation of its 3D shape



# Multi-view Stereo



[Point Grey's Bumblebee XB3](#)



[Point Grey's ProFusion 25](#)

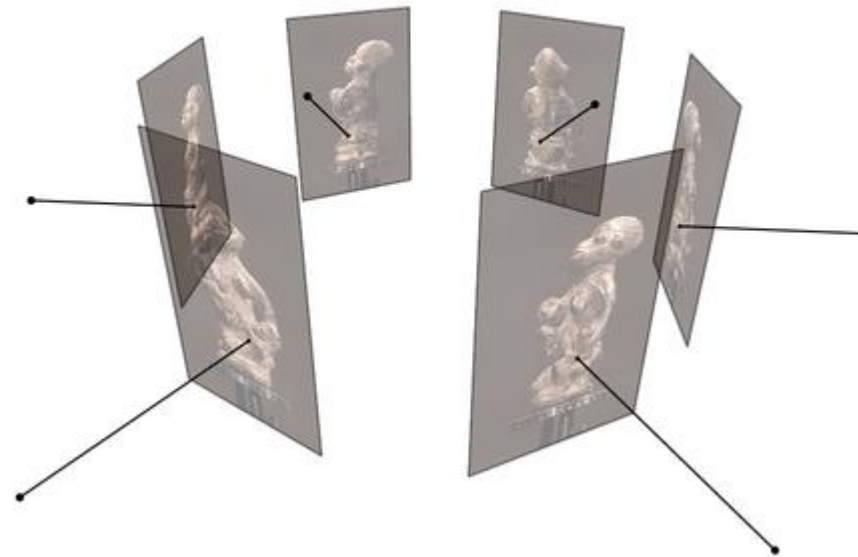


CMU's [Panoptic Studio](#)

# Multi-view Stereo

**Input:** calibrated images from several viewpoints (known intrinsics and extrinsics / projection matrices)

**Output:** 3D object model



Figures by Carlos Hernandez

We'll talk more about how to calibrate multiple cameras soon



# Applications



Data SIO, NOAA, U.S. Navy, NGA, GEBCO

Google earth

# Whistle in the Form of Female Figure *600 AD - 900 AD*



Details Los Angeles County Museum of Art



Los Angeles County Museum of Art



Sculpture



Mexico

Share



Compare



Saved <sup>0</sup>



Discover



Google



THE RENDERPEOPLE MISSION

**IMPROVING  
THE QUALITY**

**TY  
LE**

<https://renderpeople.com/about-us/>



# Virtual Reality Video



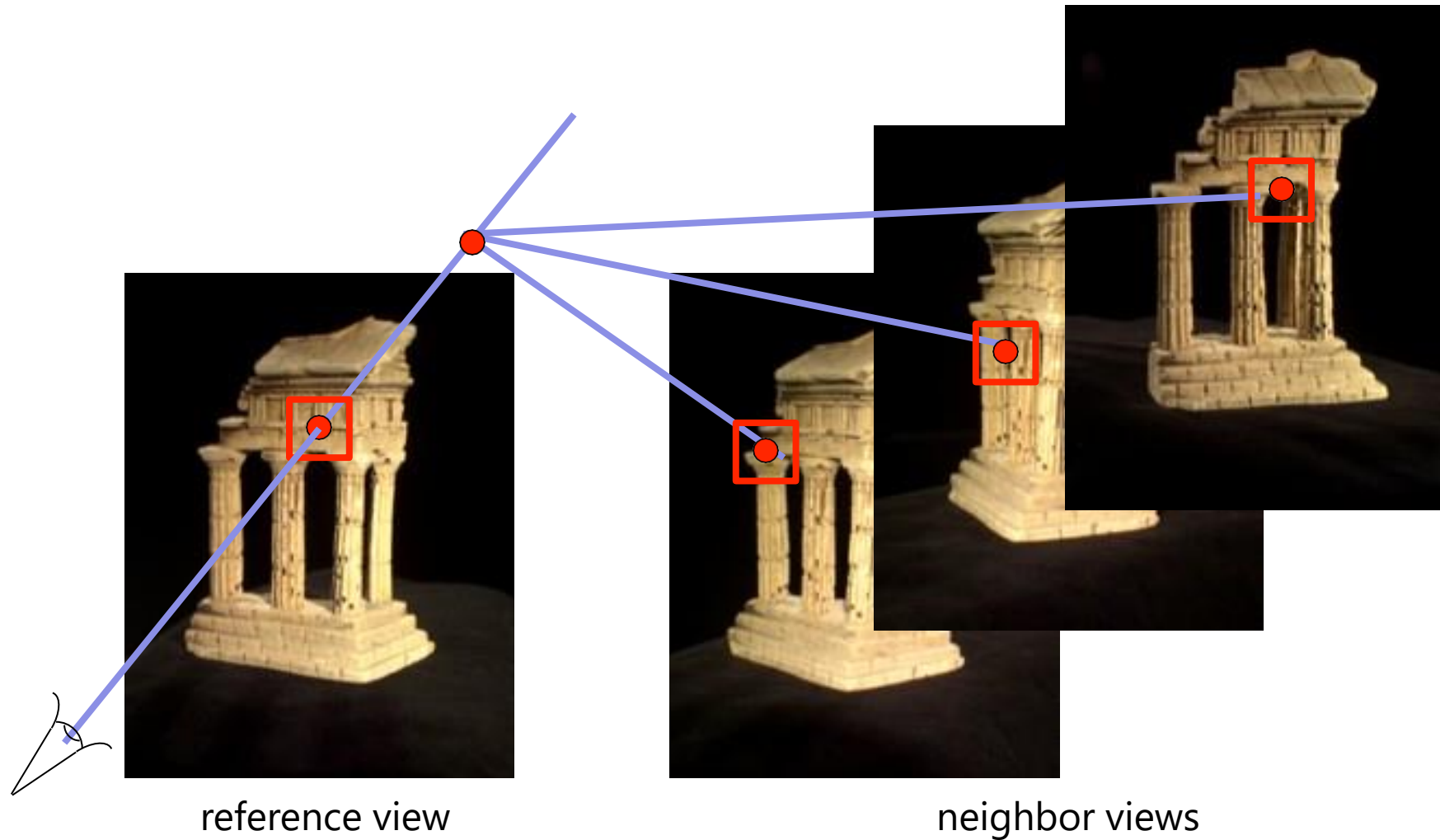
Anderson, et al. *Jump: Virtual Reality Video*. SIGGRAPH Asia 2016.



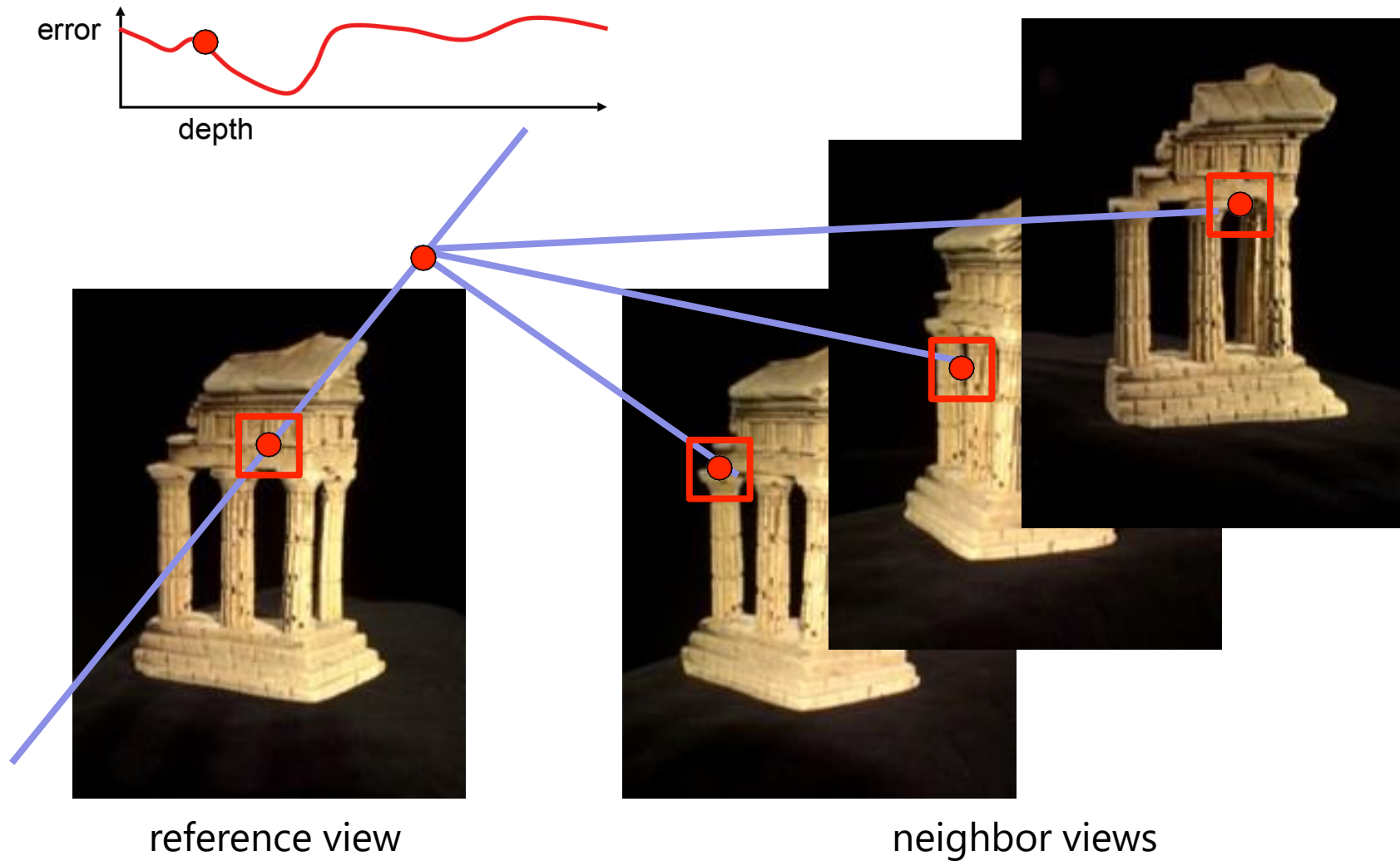
Broxton, et al. *Immersive Light Field Video with a Layered Mesh Representation*. SIGGRAPH 2020.



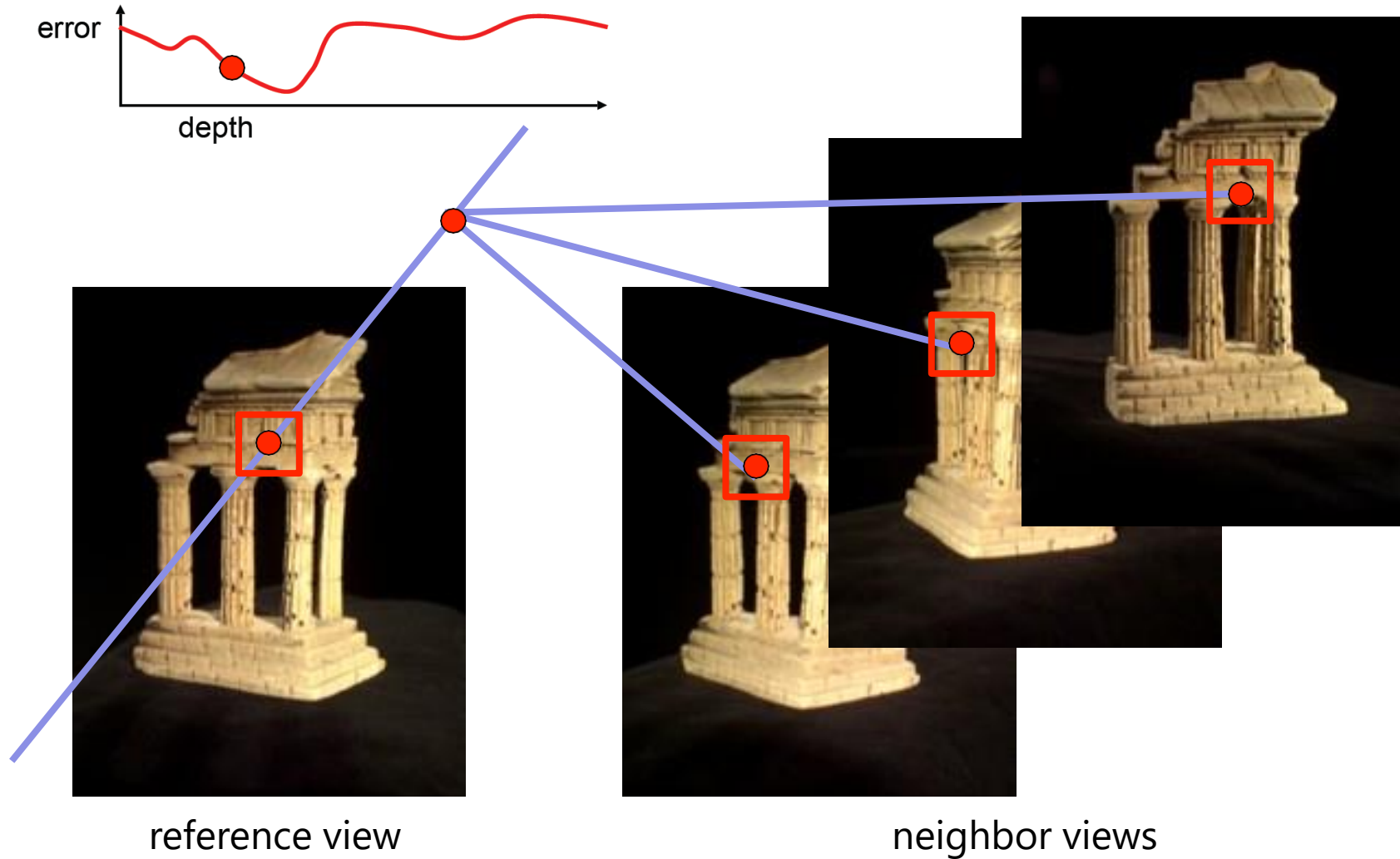
# Multi-view stereo: Basic idea



# Multi-view stereo: Basic idea

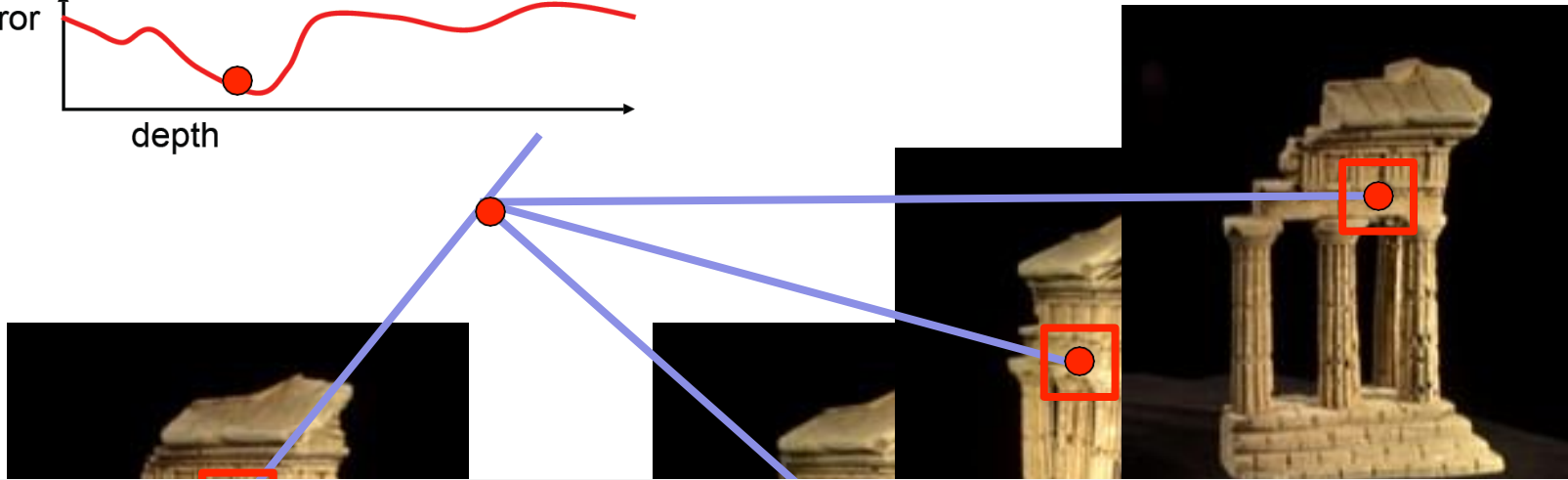
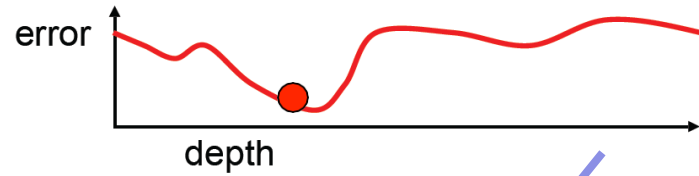


# Multi-view stereo: Basic idea





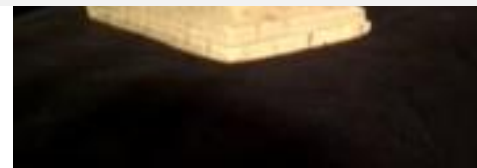
# Multi-view stereo: Basic idea



**In this manner, solve for a depth map over the whole reference view**



reference view

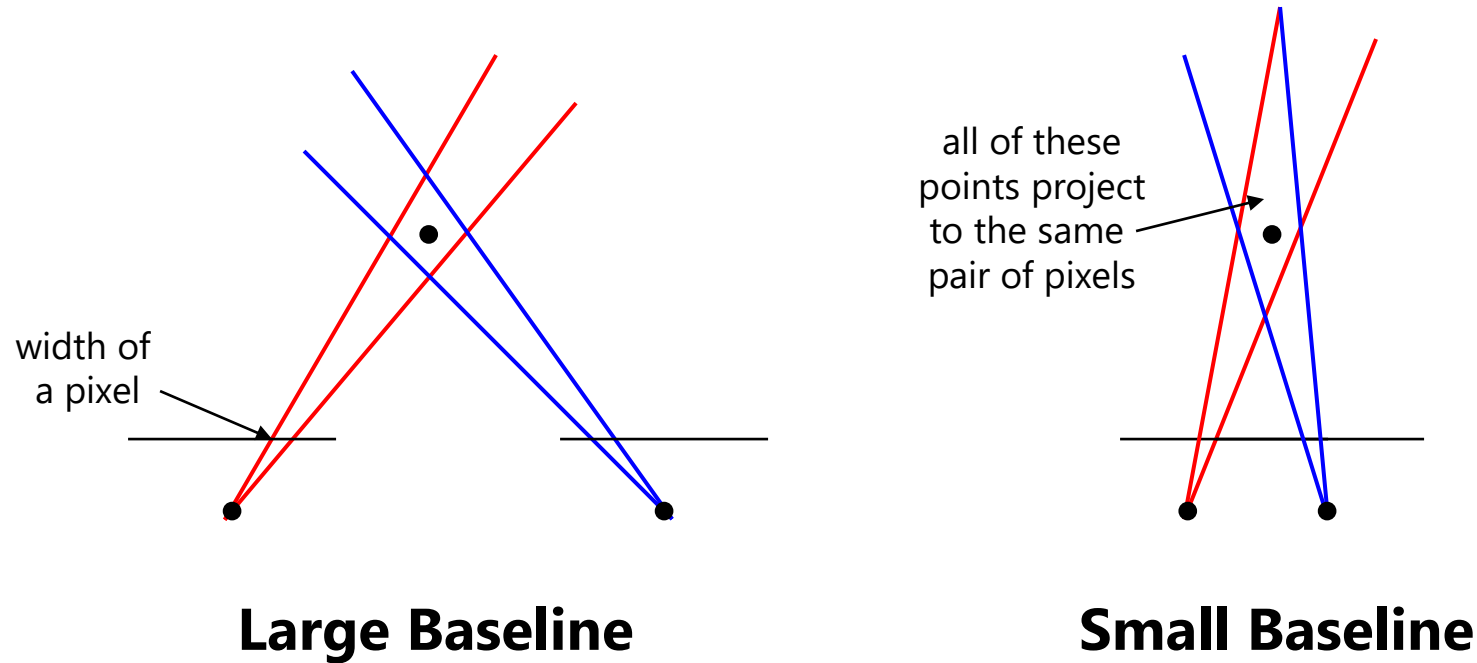


neighbor views

# Multi-view stereo: advantages

- Can match windows using more than 1 neighbor, giving a **stronger match signal**
- If you have lots of potential neighbors, can **choose the best subset** of neighbors to match per reference image
- Can reconstruct a depth map for each reference frame, and then merge into a **complete 3D model**

# Choosing the stereo baseline



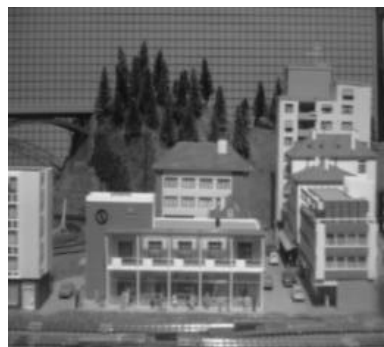
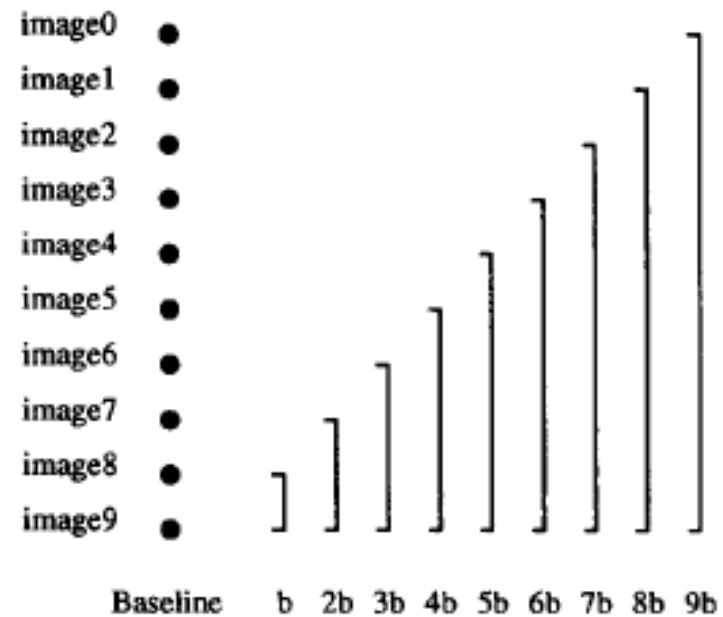
What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

# The Effect of Baseline on Depth Estimation



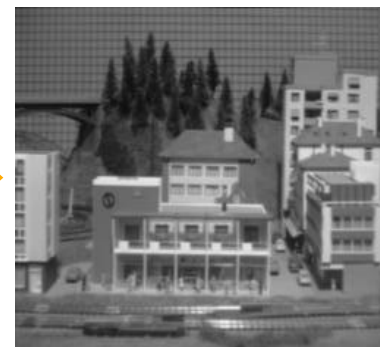
Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.



$I_1$

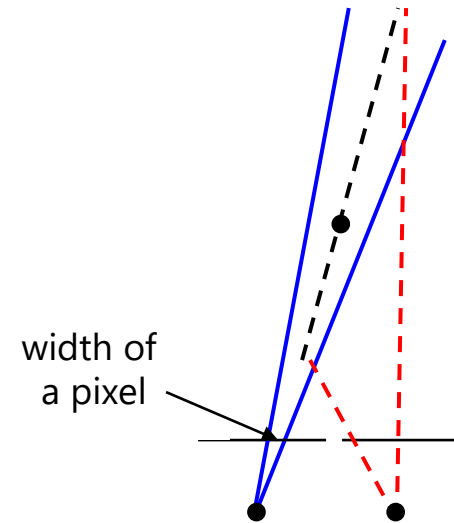
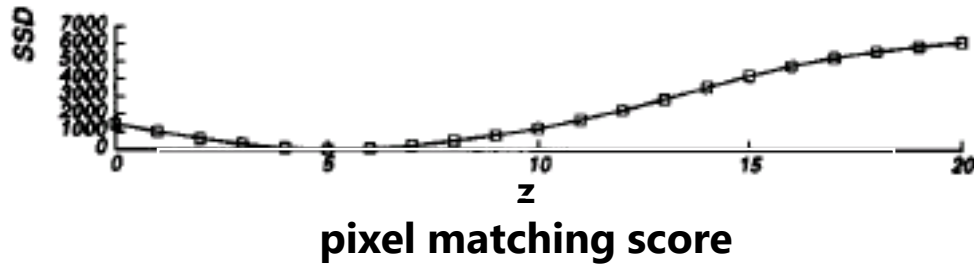


$I_2$

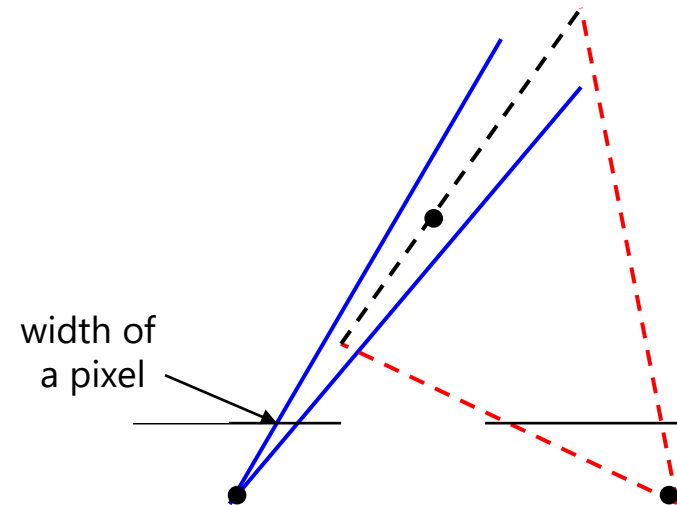
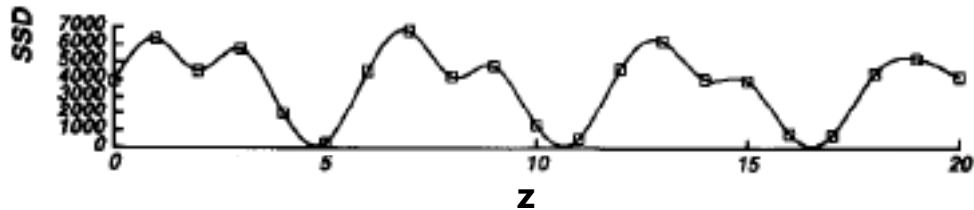


$I_{10}$

# Multiple-baseline stereo



- For short baselines, estimated depth will be less precise due to narrow triangulation



- For larger baselines, must search larger area in second image

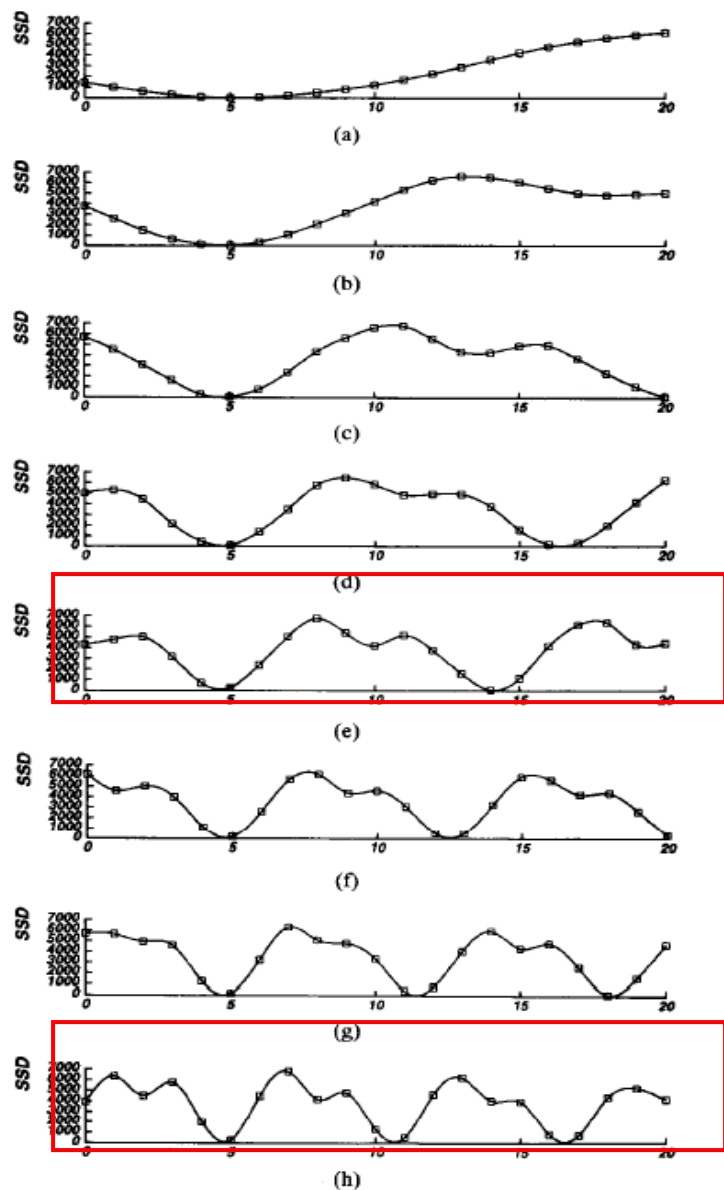


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

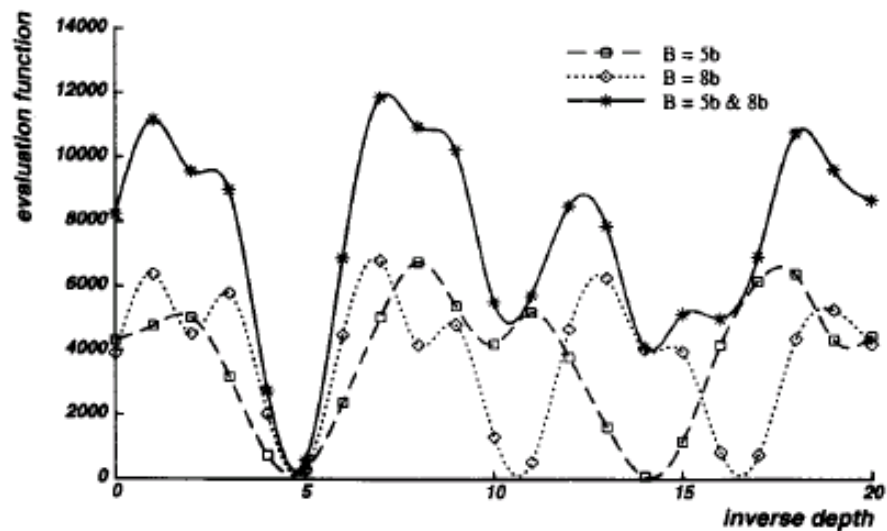


Fig. 6. Combining two stereo pairs with different baselines.

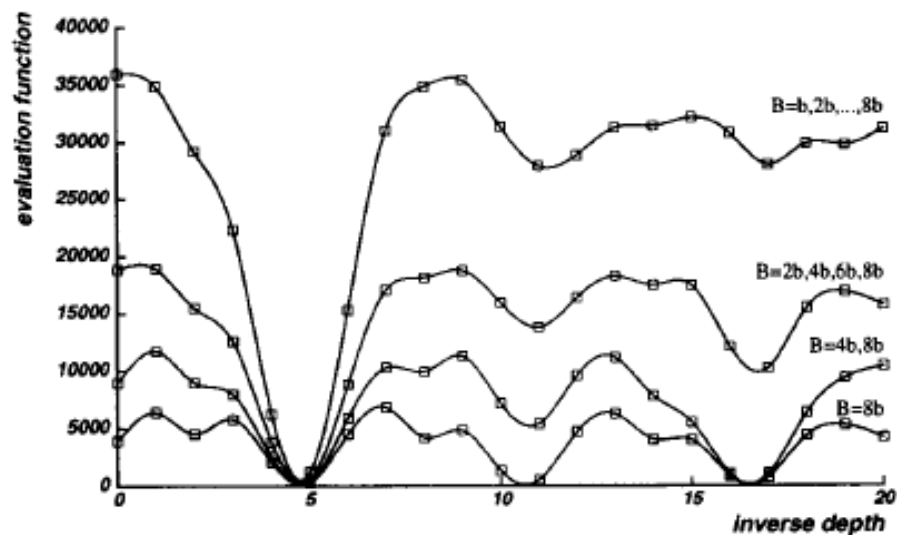
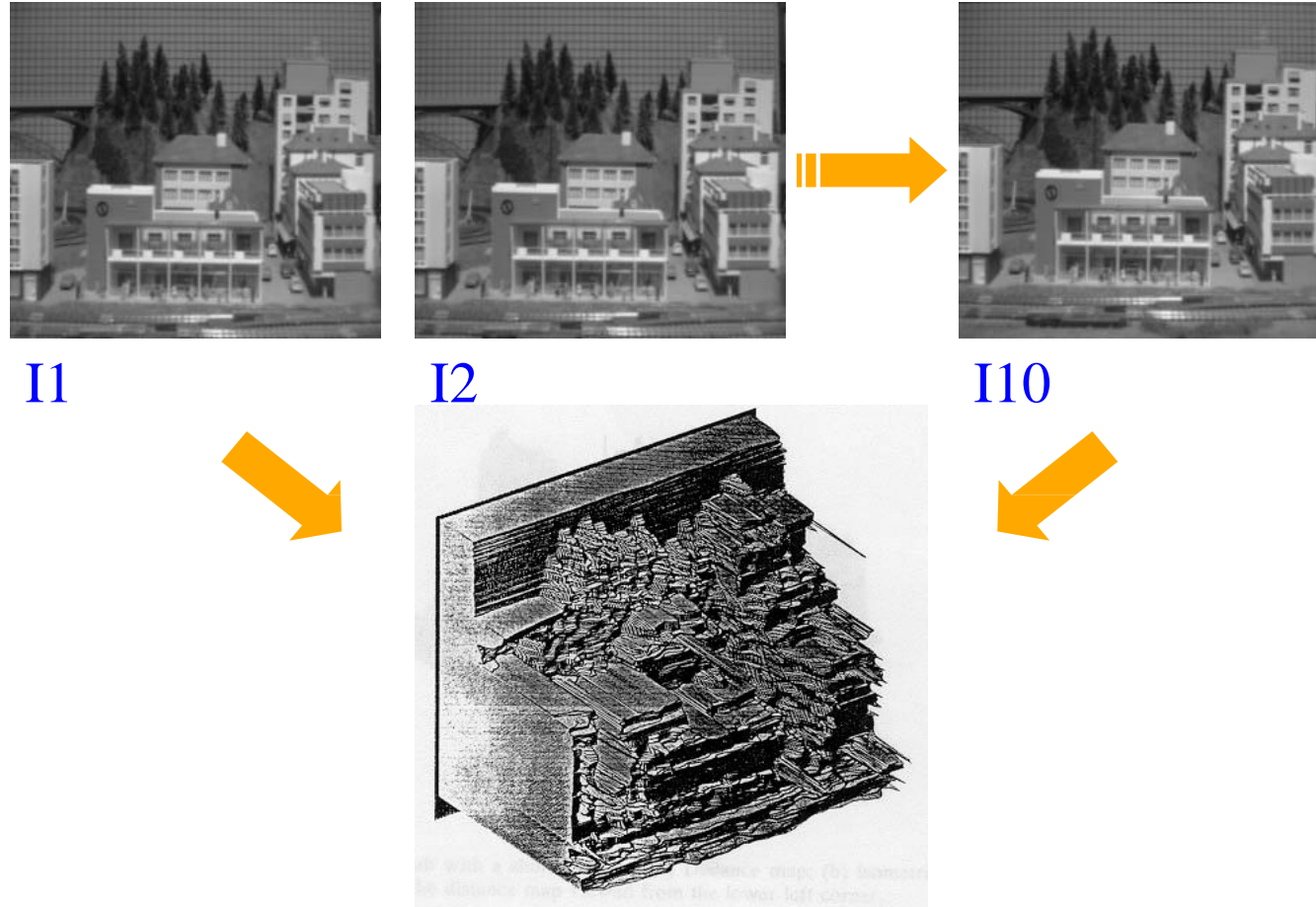


Fig. 7. Combining multiple baseline stereo pairs.

# Multiple-baseline stereo results



M. Okutomi and T. Kanade, *A Multiple-Baseline Stereo System*, IEEE Trans. on Pattern Analysis and Machine Intelligence, 15(4):353-363 (1993).

# Multibaseline Stereo

## Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - replace two-view SSD with **SSSD** over all baselines
  - **SSSD**: the SSD values are computed first for each pair of stereo images, and then add all together from multiple stereo pairs.

## Limitations

- Only gives a depth map (not an “object model”)
- Won't work for widely distributed views.



# Problem: *visibility*

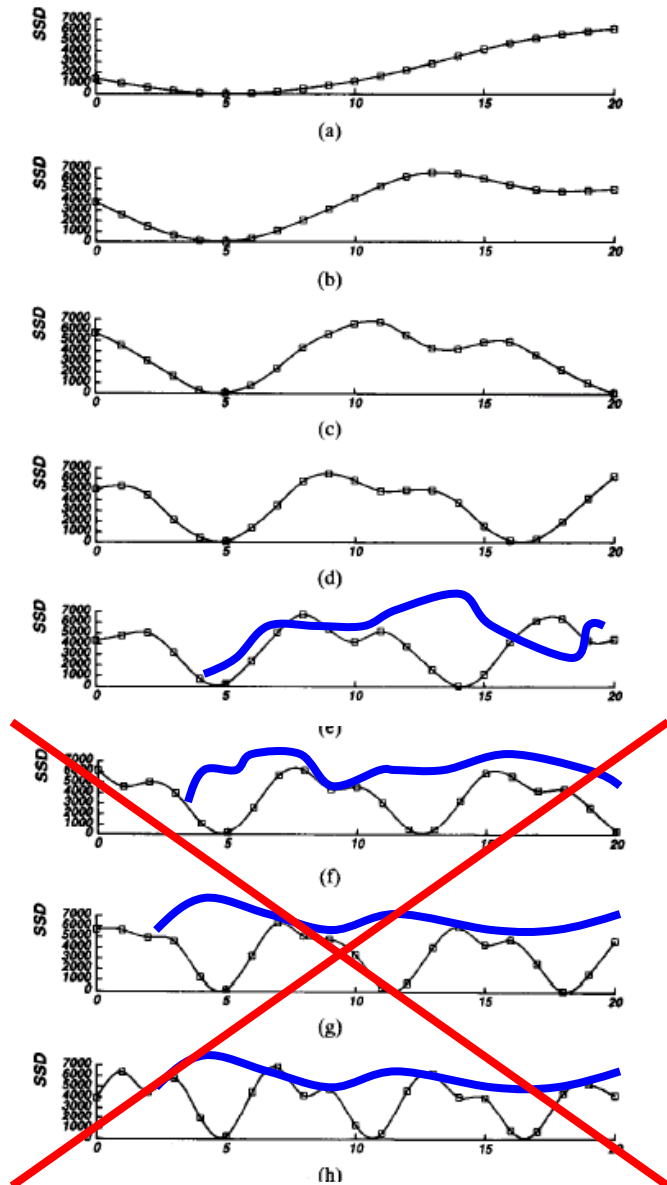


Fig. 5. SSD values versus inverse distance: (a)  $B = b$ ; (b)  $B = 2b$ ; (c)  $B = 3b$ ; (d)  $B = 4b$ ; (e)  $B = 5b$ ; (f)  $B = 6b$ ; (g)  $B = 7b$ ; (h)  $B = 8b$ . The horizontal axis is normalized such that  $8bF = 1$ .

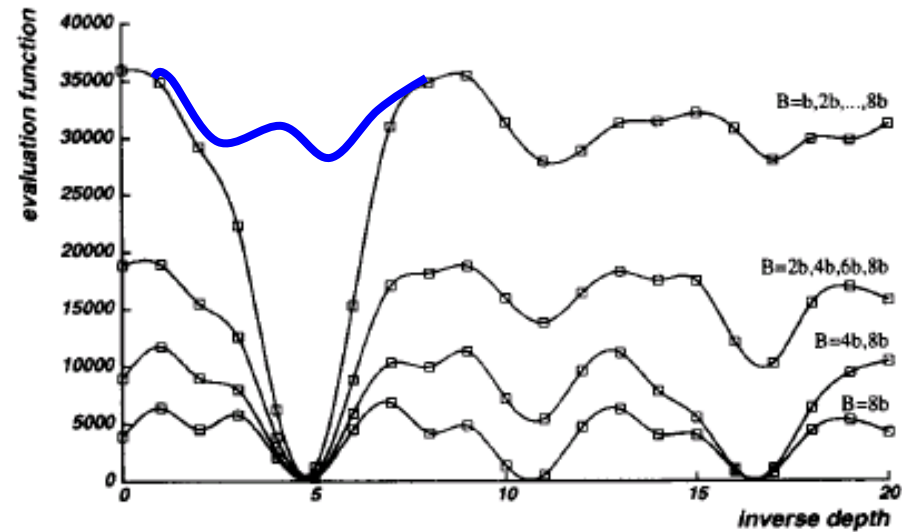


Fig. 7. Combining multiple baseline stereo pairs.

## Some Solutions

- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD, Ignore NCC values > threshold [Hernandez & Schmitt 03]

# Popular matching scores

- SSD (Sum of Squared Differences)  $\sum_{x,y} |W_1(x,y) - W_2(x,y)|^2$
- SAD (Sum of Absolute Differences)  $\sum_{x,y} |W_1(x,y) - W_2(x,y)|$
- ZNCC (Zero-mean Normalized Cross Correlation)

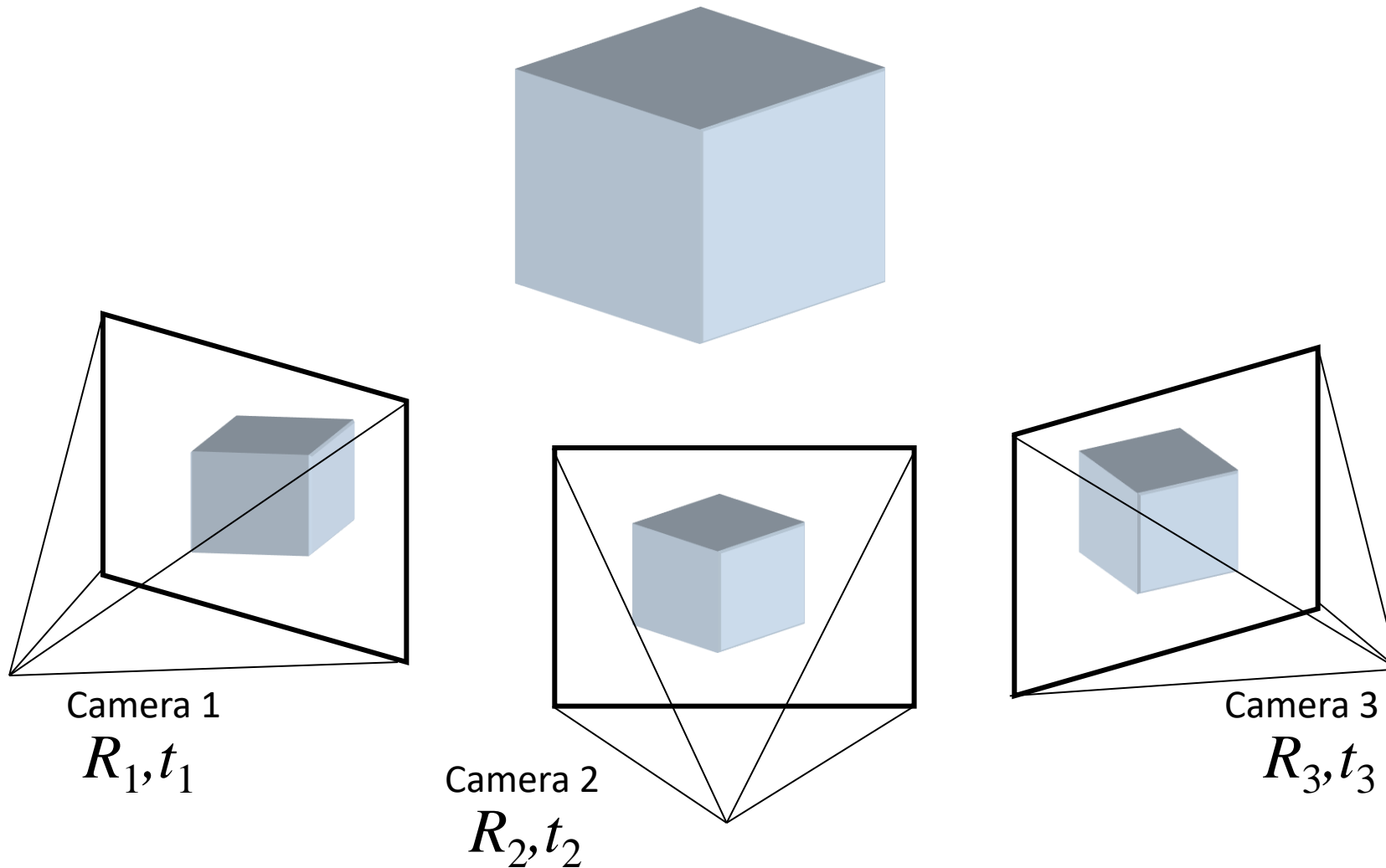
$$\frac{\sum_{x,y} (W_1(x,y) - \overline{W_1})(W_2(x,y) - \overline{W_2})}{\sigma_{W_1} \sigma_{W_2}}$$

– where  $\overline{W_i} = \frac{1}{n} \sum_{x,y} W_i$      $\sigma_{W_i} = \sqrt{\frac{1}{n} \sum_{x,y} (W_i - \overline{W_i})^2}$

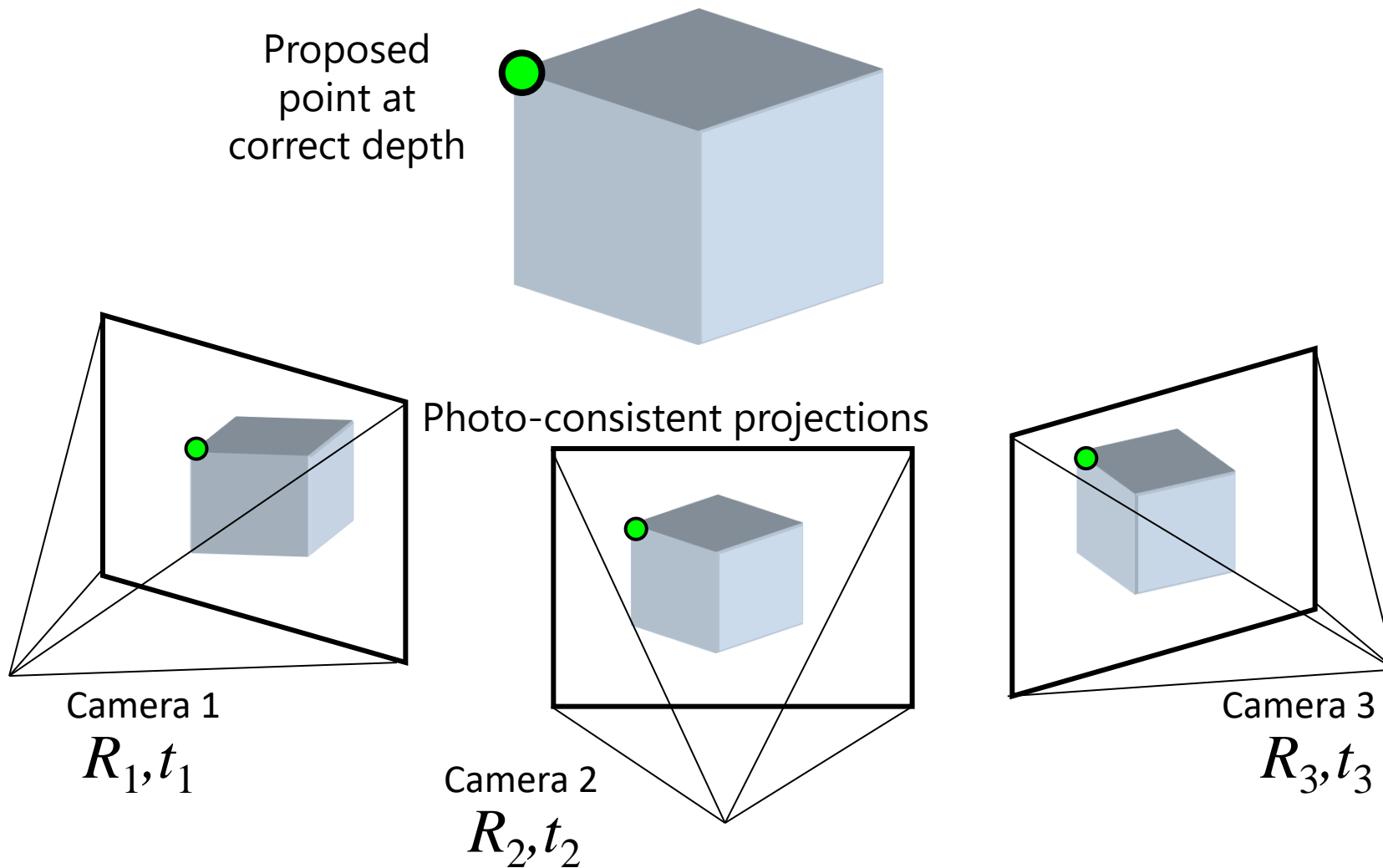
– what advantages might NCC have?

**Questions?**

# Plane-Sweep Stereo

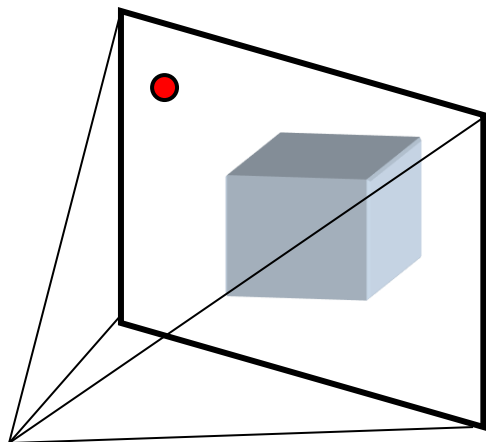
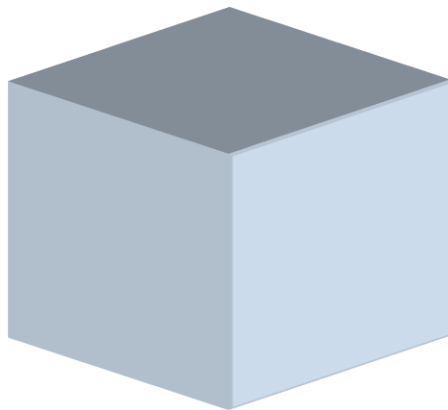


# Plane-Sweep Stereo



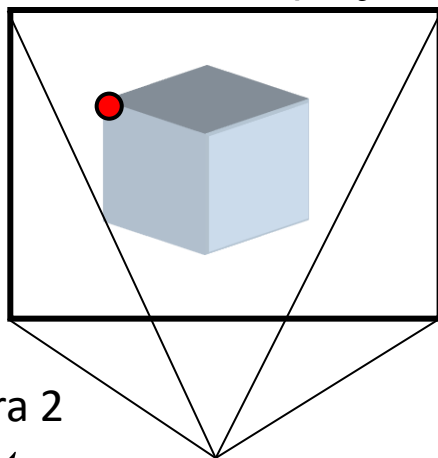
# Plane-Sweep Stereo

Proposed point at  
incorrect depth

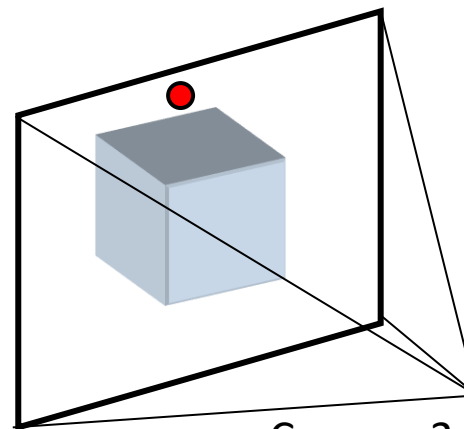


Camera 1  
 $R_1, t_1$

Photo-inconsistent projections



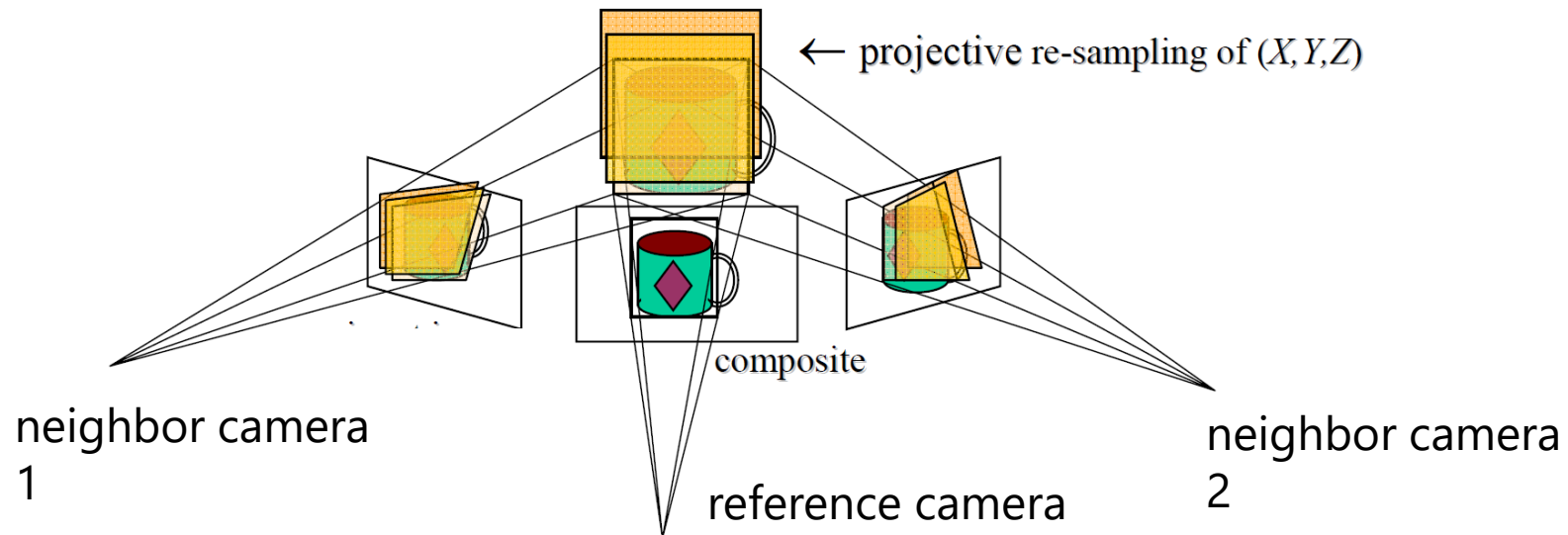
Camera 2  
 $R_2, t_2$



Camera 3  
 $R_3, t_3$

# Plane-Sweep Stereo

- Sweep family of planes parallel to the reference camera image plane
- Reproject neighbors onto each plane (via homography) and compare reprojections



# Plane-Sweep Stereo



Left neighbor



Reference image



Right neighbor



Left neighbor projected into reference image



Average images on each plane



Right neighbor projected into reference image



# Another example



Left neighbor



Reference image



Right neighbor



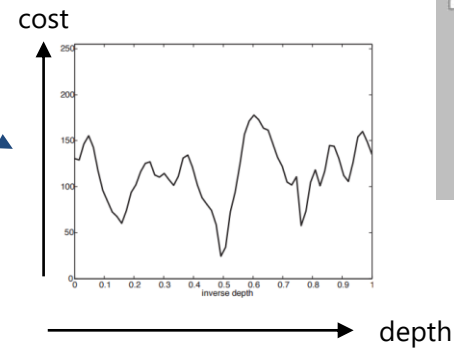
Planar image reprojections  
swept over depth (averaged)

# Cost Volumes -> Depth Maps

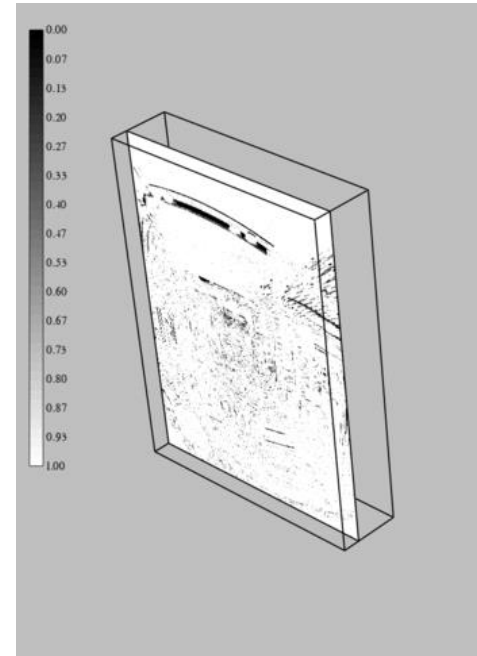


Reference image

Plane sweep



Single pixel's cost profile



Full cost volume

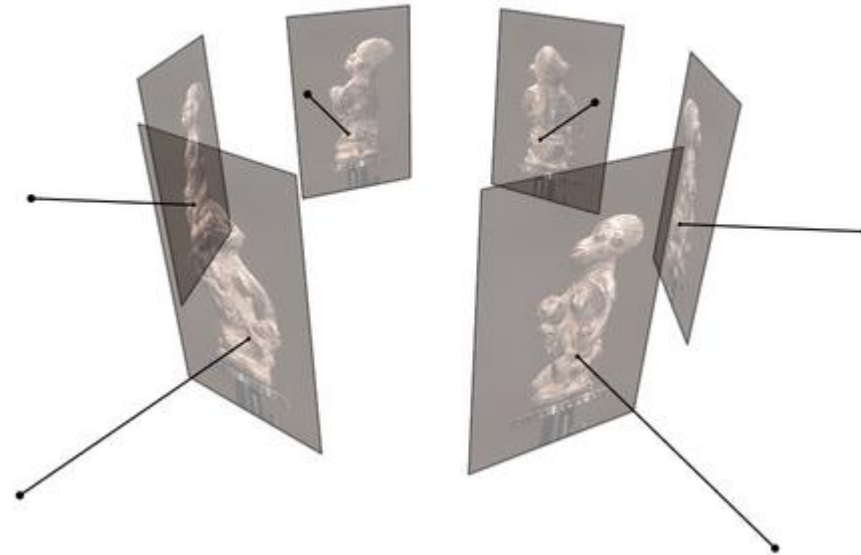
Depth map solver

(Belief propagation, graph cuts, etc.)



# Fusing multiple depth maps

- Compute depth map per image
- Fuse the depth maps into a 3D model



Figures by Carlos Hernandez

# Another approach: NeRF

- Represent scenes as functions from  $(x, y, z)$  to RGB and alpha (transparency), use volume rendering to render images



NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis, ECCV 2020

**Questions?**