

This list of topics is meant to convey the course organization and the range of subjects covered in the course. With each topic we give a list of problems, applications, and sub-topics that we will discuss. The details are subject to change.

- Introduction
  - An opening problem: stable marriages
  - Range of problems we will consider
- General Algorithmic Techniques
  - Greedy algorithms
    - \* Finding optimal solutions with greedy methods (scheduling time intervals)
    - \* The minimum spanning tree problem
  - The Divide and Conquer method (some basic primitives in computational geometry)
  - Dynamic Programming with many applications
    - \* weighted interval scheduling
    - \* knapsack problems
    - \* shortest paths
    - \* sequence alignment (including efficient implementation via divide and conquer)
  - Flows and Cuts in Networks
    - \* The basic flow and cut problems
    - \* Basic methods: augmenting paths
    - \* Application to matching
    - \* Polynomial time methods
    - \* Extensions to more general models
    - \* Applications to resource allocation, sequencing, and segmentation.
- Computational Intractability
  - NP-completeness
    - hardness of problems in optimization and constraint satisfaction.
    - \* How to show NP-completeness: reducibility

- \* Examples including the traveling salesman problem, 3-dimensional matching, covering, packing, partitioning problems, and subset sum.
- PSPACE completeness
  - hardness of problems in artificial intelligence and game-playing.
- Algorithms for Hard Problems
  - Improved exponential methods
  - Approximation algorithms
    - \* greedy algorithms
      - (load balancing, facility location)
    - \* The application of linear programming
  - Local search techniques
    - \* The Metropolis Algorithm
    - \* Simulated annealing
    - \* Applications to graph partitioning and neural networks
- Randomized algorithms
  - (including contention-resolution protocols and satisfiability heuristics)
- Algorithms that run forever