



$$J(\pi) - J(\pi^*)$$

$\pi$  makes mistakes with prob  $\epsilon$  on expert states.

$$J(\pi^*) = \sum_{t=0}^{T-1} \mathbb{E}_{s_t \sim d_t^{\pi^*}} c(s_t, \pi^*(s_t)) = ? 0$$

$$J(\pi) = \sum_{t=0}^{T-1} \mathbb{E}_{s_t \sim d_t^{\pi}} c(s_t, \pi(s_t))$$

$$= \epsilon \times \left( \underbrace{1 + 1 + 1 + \dots}_{T} \right) + (1-\epsilon) \times \left( 0 + \epsilon \times \left( \underbrace{1 + 1 + 1 \dots}_{T-1} \right) \right)$$

$$+ (1-\epsilon) \times \left( 0 + \dots \right)$$

$$= \epsilon T + (1-\epsilon) \epsilon (T-1) + (1-\epsilon)^2 \epsilon (T-2) + \dots$$

$$= \epsilon \left( T + \underbrace{(1-\epsilon)}_{\leq 1} (T-1) + \underbrace{(1-\epsilon)^2}_{\leq 1} (T-2) + \dots \right)$$

$$\leq \epsilon \left( T + (T-1) + (T-2) + \dots + 3 + 2 + 1 \right)$$

$$\leq \epsilon \cdot \frac{T(T+1)}{2} \approx O(\epsilon T^2)$$