



Hash-Based Indexes

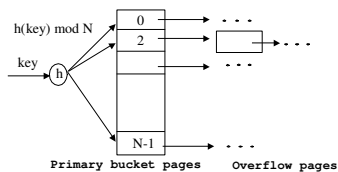
Chapter 11

Introduction

- ❖ As for any index, 3 alternatives for data entries k^* :
 - ① Data record with key value k
 - ② $\langle k, \text{rid of data record with search key value } k \rangle$
 - ③ $\langle k, \text{list of rids of data records with search key } k \rangle$
 - Choice orthogonal to the indexing technique
- ❖ Hash-based indexes are best for equality selections. **Cannot** support range searches.
- ❖ Static and dynamic hashing techniques exist; trade-offs similar to ISAM vs. B+ trees.

Static Hashing

- ❖ # primary pages fixed, allocated sequentially, never de-allocated; overflow pages if needed.
- ❖ $h(k) \bmod M = \text{bucket to which data entry with key } k \text{ belongs. (} M = \# \text{ of buckets)}$



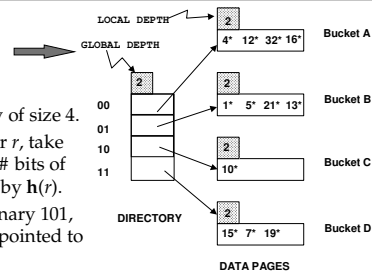
Static Hashing (Contd.)

- ❖ Buckets contain *data entries*.
- ❖ Hash fn works on *search key* field of record r . Must distribute values over range $0 \dots M-1$.
 - $h(\text{key}) = (a * \text{key} + b)$ usually works well.
 - a and b are constants; lots known about how to tune h .
- ❖ Long overflow chains can develop and degrade performance.
 - *Extendible* and *Linear Hashing*: Dynamic techniques to fix this problem.

Extendible Hashing

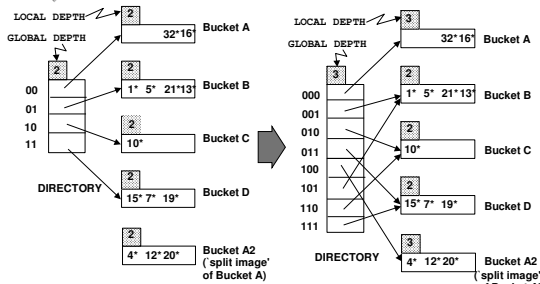
- ❖ Situation: Bucket (primary page) becomes full. Why not re-organize file by *doubling* # of buckets?
 - Reading and writing all pages is expensive!
 - *Idea*: Use *directory of pointers to buckets*, double # of buckets by *doubling the directory*, splitting just the bucket that overflowed!
 - Directory much smaller than file, so doubling it is much cheaper. Only one page of data entries is split. *No overflow page!*
 - Trick lies in how hash function is adjusted!

Example



- ❖ Directory is array of size 4.
- ❖ To find bucket for r , take last '*global depth*' # bits of $h(r)$; we denote r by $h(r)$.
 - If $h(r) = 5 = \text{binary } 101$, it is in bucket pointed to by 01.
- ❖ **Insert**: If bucket is full, *split* it (allocate new page, re-distribute).
- ❖ If necessary, double the directory. (As we will see, splitting a bucket does not always require doubling; we can tell by comparing *global depth* with *local depth* for the split bucket.)

Insert $h(r)=20$ (Causes Doubling)

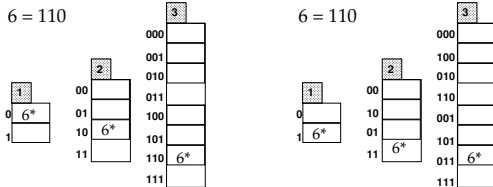


Points to Note

- ❖ $20 = \text{binary } 10100$. Last 2 bits (00) tell us r belongs in A or A2. Last 3 bits needed to tell which.
 - Global depth of directory: Max # of bits needed to tell which bucket an entry belongs to.
 - Local depth of a bucket: # of bits used to determine if an entry belongs to this bucket.
- ❖ When does bucket split cause directory doubling?
 - Before insert, local depth of bucket = global depth. Insert causes local depth to become $>$ global depth; directory is doubled by copying it over and fixing pointer to split image page. (Use of least significant bits enables efficient doubling via copying of directory!)

Directory Doubling

Why use least significant bits in directory?
 \Rightarrow Allows for doubling via copying!



Least Significant

vs.

Most Significant

Comments on Extendible Hashing

- ❖ If directory fits in memory, equality search answered with one disk access; else two.
 - 100MB file, 100 bytes/rec, 4K pages contains 1,000,000 records (as data entries) and 25,000 directory elements; chances are high that directory will fit in memory.
 - Directory grows in spurts, and, if the distribution of hash values is skewed, directory can grow large.
 - Multiple entries with same hash value cause problems!
- ❖ **Delete:** If removal of data entry makes bucket empty, can be merged with 'split image'. If each directory element points to same bucket as its split image, can halve directory.

Linear Hashing

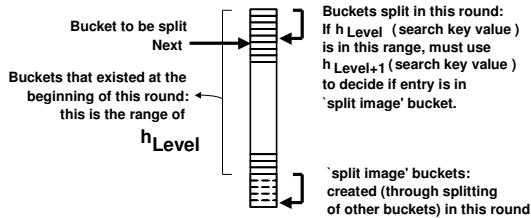
- ❖ This is another dynamic hashing scheme, an alternative to Extendible Hashing.
- ❖ LH handles the problem of long overflow chains without using a directory, and handles duplicates.
- ❖ **Idea:** Use a family of hash functions h_0, h_1, h_2, \dots
 - $h_i(\text{key}) = h(\text{key}) \bmod (2^i N)$; $N = \text{initial \# buckets}$
 - h is some hash function (range is not 0 to $N-1$)
 - If $N = 2^{d_0}$, for some d_0 , h_i consists of applying h and looking at the last d_i bits, where $d_i = d_0 + i$.
 - h_{i+1} doubles the range of h_i (similar to directory doubling)

Linear Hashing (Contd.)

- ❖ Directory avoided in LH by using overflow pages, and choosing bucket to split round-robin.
 - Splitting proceeds in 'rounds'. Round ends when all N_R initial (for round R) buckets are split. Buckets 0 to $Next-1$ have been split; $Next$ to N_R yet to be split.
 - Current round number is $Level$.
 - **Search:** To find bucket for data entry r , find $h_{Level}(r)$:
 - ♦ If $h_{Level}(r)$ in range 'Next to N_R ', r belongs here.
 - ♦ Else, r could belong to bucket $h_{Level}(r)$ or bucket $h_{Level}(r) + N_{R'}$ must apply $h_{Level+1}(r)$ to find out.

Overview of LH File

- ❖ In the middle of a round.

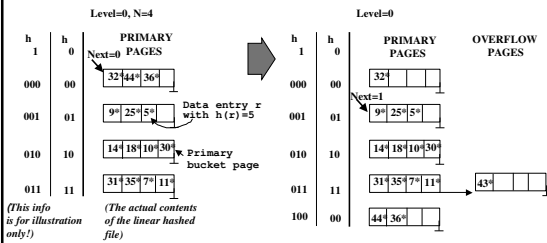


Linear Hashing (Contd.)

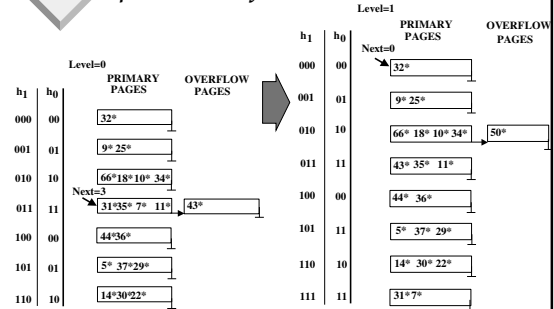
- ❖ **Insert:** Find bucket by applying $h_{Level} / h_{Level+1}$
 - If bucket to insert into is full:
 - ♦ Add overflow page and insert data entry.
 - ♦ (Maybe) Split *Next* bucket and increment *Next*.
- ❖ Can choose any criterion to 'trigger' split.
- ❖ Since buckets are split round-robin, long overflow chains don't develop!
- ❖ Doubling of directory in Extendible Hashing is similar; switching of hash functions is *implicit* in how the # of bits examined is increased.

Example of Linear Hashing

- ❖ On split, $h_{Level+1}$ is used to re-distribute entries.



Example: End of a Round



LH Described as a Variant of EH

- ❖ The two schemes are actually quite similar:
 - Begin with an EH index where directory has N elements.
 - Use overflow pages, split buckets round-robin.
 - First split is at bucket 0. (Imagine directory being doubled at this point.) But elements $\langle 1, N+1 \rangle, \langle 2, N+2 \rangle, \dots$ are the same. So, need only create directory element N , which differs from 0, now.
 - ♦ When bucket 1 splits, create directory element $N+1$, etc.
- ❖ So, directory can double gradually. Also, primary bucket pages are created in order. If they are *allocated* in sequence too (so that finding i 'th is easy), we actually don't need a directory! Voila, LH.

Summary

- ❖ Hash-based indexes: best for equality searches, cannot support range searches.
- ❖ Static Hashing can lead to long overflow chains.
- ❖ Extendible Hashing avoids overflow pages by splitting a full bucket when a new data entry is to be added to it. (*Duplicates may require overflow pages.*)
 - Directory to keep track of buckets, doubles periodically.
 - Can get large with skewed data; additional I/O if this does not fit in main memory.

Summary (Contd.)

- ❖ Linear Hashing avoids directory by splitting buckets round-robin, and using overflow pages.
 - Overflow pages not likely to be long.
 - Duplicates handled easily.
 - Space utilization could be lower than Extendible Hashing, since splits not concentrated on `dense` data areas.
 - ◆ Can tune criterion for triggering splits to trade-off slightly longer chains for better space utilization.
- ❖ For hash-based indexes, a *skewed* data distribution is one in which the *hash values* of data entries are not uniformly distributed!