

Dataflow Equations

 $in[B] = \Pi \{out[B'] \mid B' \in pred(B)\}, for all B$

 $out[B] = F_{B}(in[B])$, for all B

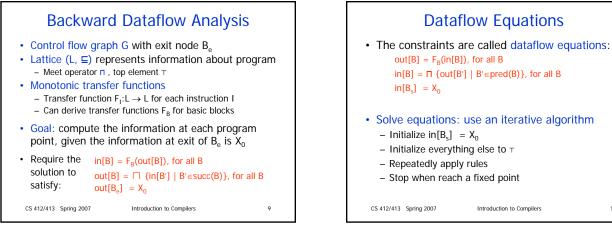
 $in[B_s] = X_0$

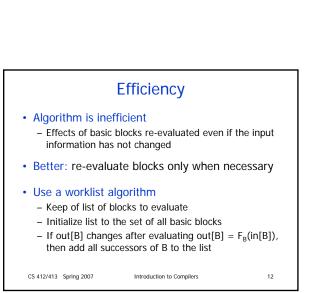
- Initialize in $[B_s] = X_0$

- Repeatedly apply rules

– Initialize everything else to T

- Stop when reach a fixed point





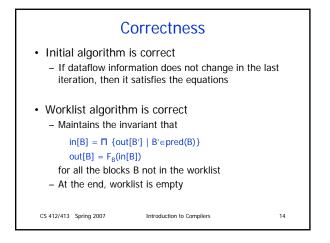
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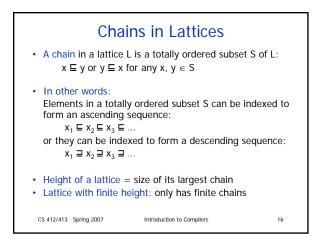
Algorithm $in[B_S] = X_0$ out[B] = τ , for all B Repeat For each basic block $B \neq B_s$ $in[B] = \pi \{out[B'] \mid B' \in pred(B)\}$ For each basic block B $out[B] = F_{B}(in[B])$ Until no change

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Termination · Do these algorithms terminate? · Key observation: at each iteration, information decreases in the lattice $in_{k+1}[B] \sqsubseteq in_k[B]$ and $out_{k+1}[B] \sqsubseteq out_k[B]$ where $in_k[B]$ is info before B at iteration k and $out_k[B]$ is info after B at iteration k • Proof by induction: - Induction basis: true, because we start with top element, which is greater than everything - Induction step: use monotonicity of transfer functions and meet operation Information forms a chain: in₁[B] ⊒ in₂[B] ⊒ in₃[B] ... CS 412/413 Spring 2007 Introduction to Compilers 15



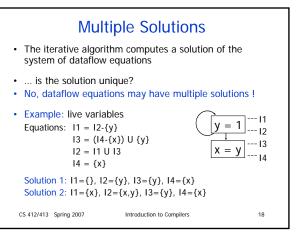
Termination

 In the iterative algorithm, for each block B: {in1[B], in2[B], ...} is a chain in the lattice, because transfer functions and meet operation are monotonic

- If lattice has finite height then these sets are finite, i.e., there is a number k such that $in_i[B] = in_{i+1}[B]$, for all $i \geq k$ and all B
- If $in_i[B] = in_{i+1}[B]$ then also $out_i[B] = out_{i+1}[B]$
- · Hence algorithm terminates in at most k iterations
- To summarize: dataflow analysis terminates if
 - 1. Transfer functions are monotonic
- 2. Lattice has finite height

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Safety

- · Solution for live variable analysis:
 - Sets of live variables must include each variable whose values will further be used in some execution
 - ... may also include variables never used in any execution!
- The analysis is safe if it takes into account all possible executions of the program
 - ... may also characterize cases which never occur in any execution of the program
 - Say that the analysis is a conservative approximation of all executions

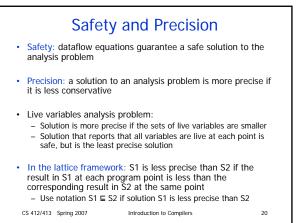
In example

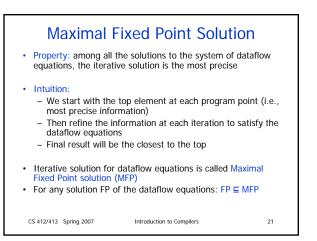
Solution 2 includes x in live set 11, which is not used later
However, analysis is conservative

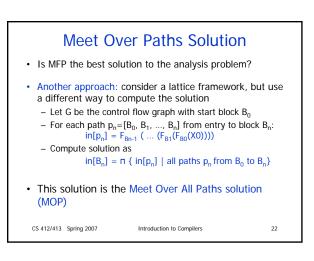
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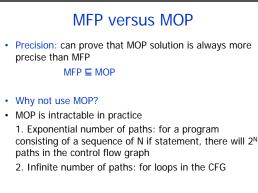
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Importance of Distributive
type• roperty: if transfer functions are distributive, then
tae solution to the dataflow equations is identical to
the network solution. $\mathcal{MFP} = \mathcal{MOP}$ • for distributive transfer functions, can compute the
intractable MOP solution using the iterative fixed-
point algorithm

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