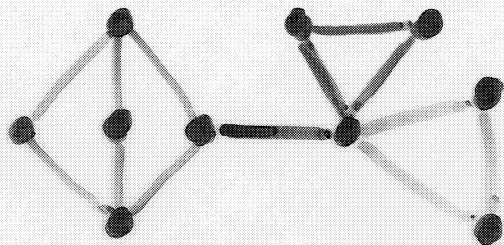


An immediate consequence of this is that  $\Gamma$  is bipartite iff it's 2-colourable; since we simply pick a node and colour it black, then colour all its neighbours red, continuing by alternating colours. The theorem guarantees that this will work for all cycles iff  $\Gamma$  is bipartite, and the non-cycles can be set to alternate until termination.

Sometimes the emphasis is more on the connectivity of a graph. We define a cutnode of  $\Gamma$  to be a node whose removal increases the number of connected components of  $\Gamma$ , and define a bridge of  $\Gamma$  to be an edge with the same property. Further, a non-separable graph is connected and has no cutnodes (and is non-trivial — has more than one node!). Given a graph  $\Gamma$ , a block of  $\Gamma$  is a maximal non-separable subgraph. For example ...



This graph has its four blocks separately coloured and has obvious cutnodes and an obvious bridge.

Given a graph  $\Gamma$ , its complement  $\bar{\Gamma}$  has the same nodes as  $\Gamma$ , but a pair of nodes are joined by an edge in  $\bar{\Gamma}$  iff they are not neighbours in  $\Gamma$ . For example ...

