

So starting with an initial state vector  $\underline{v}_0$  we can get the subsequent state vectors  $\underline{v}_k$  by

$$\underline{v}_k = M^k \underline{v}_0$$

Indeed, we could try to find the 'steady state' condition by

$$\underline{v}_\infty = \lim_{k \rightarrow \infty} M^k \underline{v}_0$$

Clearly this is computationally nuts, however, if such a steady state exists, then

$$M \underline{v}_\infty = \underline{v}_\infty \quad (*)$$

so finding the steady state vector reduces to solving (\*). Some of you may recognise this as the eigenvector corresponding to the eigenvalue 1, which points to a far more computationally reasonable approach!

Returning to our composition, a viable transition matrix might be:

$$M = \begin{pmatrix} 0.2 & 0.1 & 0 & 0.2 & 0.3 & 0 & 0.1 & 0.4 \\ 0.1 & 0.1 & 0 & 0.1 & 0.2 & 0.3 & 0 & 0 \\ 0.2 & 0.2 & 0.2 & 0 & 0.1 & 0.2 & 0 & 0.2 \\ 0.05 & 0.2 & 0.3 & 0.1 & 0.05 & 0.2 & 0 & 0.2 \\ 0.2 & 0.2 & 0.2 & 0.4 & 0.1 & 0 & 0.3 & 0 \\ 0.1 & 0.1 & 0.2 & 0.1 & 0.2 & 0.15 & 0 & 0 \\ 0.05 & 0.1 & 0.1 & 0 & 0.05 & 0.15 & 0.1 & 0.1 \\ 0.1 & 0 & 0 & 0.1 & 0.1 & 0 & 0.5 & 0.1 \end{pmatrix}$$

= p(next play G<sub>i</sub> | currently playing E<sub>i</sub>)

There's much more which can be studied on this topic!