



Design Patterns & Some Unresolved Problems

Lecture 26
CS211 - Fall 2006

Announcements

- Final Exam
 - Wednesday, Dec 13
 - 7:00 - 9:30 pm
 - Uris Hall, Auditorium
- Review Session
 - To be determined
- Check your final exam schedule!
- For exam conflicts:
 - Notify Kelly Patwell (patwell@cs.cornell.edu)
 - You must provide
 - Your entire exam schedule
 - Include the course numbers
- Definition of exam conflict:
 - Two exams at the same time or
 - Three or more exams within 24 hours

Late-Breaking Announcements

- Thinking about a Masters of Engineering degree?
 - Come to the next ACSU general meeting
 - Wednesday, November 29th at 4:45pm in Phillips 203
 - Professor Bailey, director of the Computer Science M. Eng. program, will discuss CS M. Eng. opportunities
 - As always, pizza will be served!
- Jealous of the glamorous life of CS consultants?
 - We're recruiting next-semester consultants for CS100 and CS211
 - Interested students should fill out an application, available in 303 Upton Hall

Design Patterns

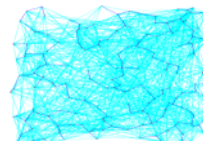
- Design Patterns: A catalog of common interactions between objects that programmers have frequently found useful
 - Influential book:
Design Patterns: Elements of Reusable Software, Gamma, Helm, Johnson and Vlissides (1995)
- Design patterns are often divided into 3 groups:
 - Creational patterns
 - Used to create objects
 - Structural patterns
 - Composing groups of objects to build more complex structures
 - Behavioral patterns
 - Communication & flow control

A Few Design Patterns in Java

- Design patterns can be used with any Object-Oriented language
- Chain of Responsibility Pattern
 - A request is passed along a "chain" of classes until one of the classes can handle it
 - Java example: The inheritance structure itself; a method-call is passed up the inheritance chain until the first parent class containing that method is found
- Adapter pattern
 - Provides an alternate interface to a class
 - Java example: MouseAdapter is a class used in Java to simplify the MouseListener interface
- Iterator Pattern
 - A standard interface for moving through a collection
 - Java example: Iterator interface in the JCF

Complexity of Bounded-Degree Euclidean MST?

- The Euclidean MST (Minimum Spanning Tree) problem:
 - Given n points in the plane, determine the MST
 - Can be solved in $O(n \log n)$ time by first building the Delaunay Triangulation
- Bounded-degree version:
 - Given n points in the plane determine the MST where each vertex has degree $\leq k$
 - Known to be NP-hard for $k=3$ [Papadimitriou & Vazirani 84]
 - $O(n \log n)$ algorithm for $k=5$ (or greater)
 - Can show Euclidean MST has degree ≤ 5
 - Unknown for $k=4$



Runtime for Euclidean MST in R^d ?

- Given n points in dimension d , determine the MST
 - Is there an algorithm with runtime close to the $\Omega(n \log n)$ lower bound?
- Best algorithms for general graphs run in time linear in $m = \text{number of edges}$
 - But for Euclidean distances on points, the number of edges is $n(n-1)/2$
- Can solve in time $O(n \log n)$ for $d=2$
- For large d , it appears that runtime approaches $O(n^2)$

$O(n^2)$ Time for X+Y Sorting?

How long does it take to sort an n -by- n table of numbers?



+	1	3	5	8
2	3	5	7	10
10	11	13	15	18
12	13	15	17	20
14	15	17	19	22

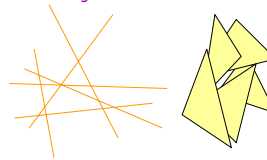
- $O(n^2 \log n)$ because there are n^2 numbers in the table
- What if it's an *addition table*?
 - Shouldn't it be easier to sort than an arbitrary set of n^2 numbers?
- There is a technique [Fredman 76] that uses just $O(n^2)$ comparisons
 - But it uses $O(n^2 \log n)$ time [Lambert 92] to decide *which* comparisons to use
- This problem is closely related to the problem of *sorting the vertices of a line arrangement*

$O(n \log n)$ Time for ShellSort?

- Is there a sequence of ShellSort step-sizes for which ShellSort runs in time $O(n \log n)$?
- There *is* a sequence for which ShellSort runs in time $O(n \log^2 n)$
 - Pratt sequence: numbers of the form 2^{2^i} arranged in order

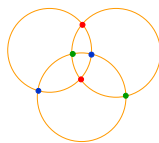
3SUM in Subquadratic Time?

- Given a set of n integers, are there three that sum to zero?
 - $O(n^2)$ algorithms are easy (e.g., use a hashtable)
 - Are there better algorithms?
- This problem is closely related to many other problems [Gajentaan & Overmars 95]
 - Given n lines in the plane, are there 3 lines that intersect in a point?
 - Given n triangles in the plane, does their union have a hole?



Great-Circle Graph 3-Colorable?

- Build a graph by drawing great-circles on a sphere
 - Create a vertex for each intersection
 - Assume no three great circles intersect in a point
- Is the resulting graph 3-colorable?
- All arrangements for up to 11 great circles have been verified as 3-colorable
- For *general* circles on the sphere (or for circles on the plane) the graph can require 4 colors



The Big Question: Is $P=NP$?

- P represents problems that can be *solved* in polynomial time
 - These problems are said to be *tractable*
 - Problems that are not in P are said to be *intractable*
- NP represents problems that, for a *given solution*, the solution can be *checked* in polynomial time
- For ease of comparison, problems are usually stated as yes-or-no questions
- Examples
 - Given a weighted graph G and a bound k , does G have a spanning tree of size $\leq k$?
 - This is in P because we have an algorithm for the MST with runtime $O(m + n \log n)$
 - Given graph G , does G have a cycle that visits all vertices?
 - This is in NP because, given a possible solution, we can check in polynomial time that it's a cycle and that it visits all vertices

Current Status: P vs. NP

- It's easy to show that $P \subseteq NP$
- Most researchers believe that $P \neq NP$
 - But at present, there is no proof
 - We do have a large collection of *NP-complete problems*
 - If any NP-complete problem has a polynomial time algorithm then they all do
- Definition: A problem B is *NP-complete* if, by making use of an *imaginary* fast subroutine for B, any problem in NP could be solved in polynomial time
 - [Cook 1971] showed a particular problem to be NP-complete
 - [Karp 1972] showed that many useful problems are NP-complete

NP-Complete Problems

- Graph coloring: Given graph G and bound k , is G k -colorable?
- Planar 3-coloring: Given planar graph G , is G 3-colorable?
- Traveling Salesman: Given weighted graph G and bound k , is there a cycle of cost $\leq k$ that visits each vertex exactly once?
- Hamiltonian Cycle: Given graph G , is there a cycle that visits each vertex exactly once?
- What if you really *need* an algorithm for an NP-complete problem?
 - Some special cases can be solved in polynomial time
 - If you're lucky, you have such a special case
 - Otherwise, once a problem is shown to be NP-complete, the best strategy is to start looking for an approximation
- For a while, a new proof showing a problem NP-complete was enough for a paper
 - Nowadays, no one is interested unless the result is somehow unexpected