

Prof. Noah Snavely CS1114

http://cs1114.cs.cornell.edu



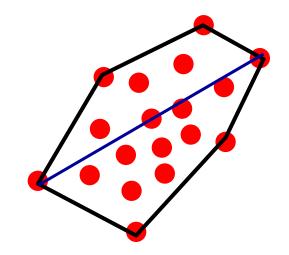
#### **Administrivia**

- Assignment 3 due tomorrow by 5pm
  - Please sign up for a demo slot
- Assignment 4 will be posted tomorrow

• Quiz 3 next Thursday

#### Last time

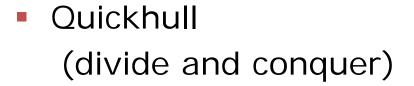
 Convex hull – the smallest convex polygon containing a point set

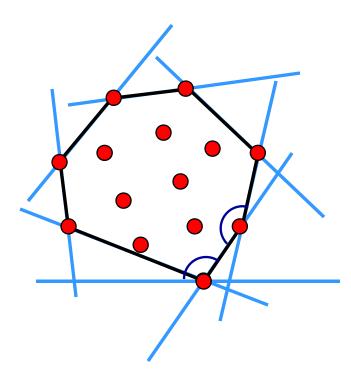


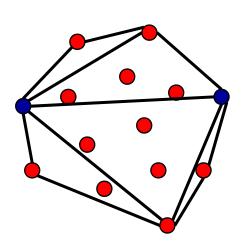
- We can use this to describe the shape of the red blob
- And find its orientation

### Computing the convex hull

Gift wrapping algorithm ("Jarvis march")







### Today: back to images

This photo is too small:



- Where was this taken?
- What time was it taken?
- How can we zoom in?

## Today: back to images

This photo is too small:



• Might need this for forensics:

http://www.youtube.com/watch?v=XgRwI4Z6Wqo

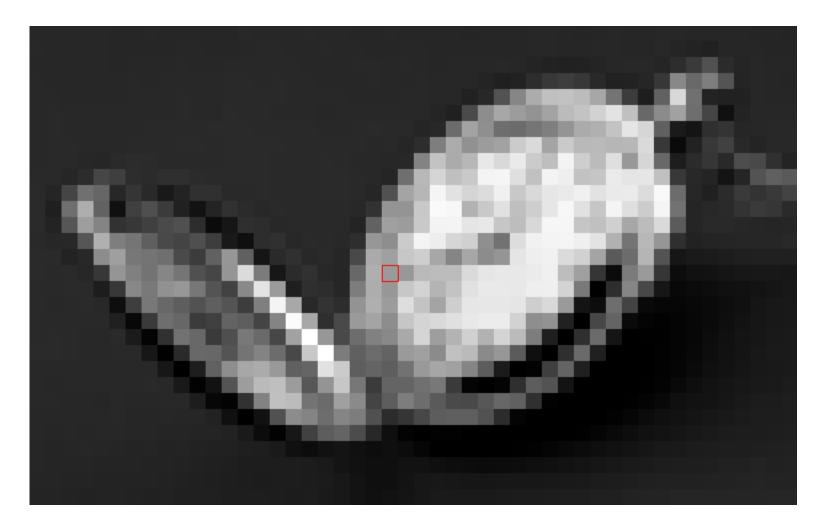
#### Zooming

 First consider a black and white image (one intensity value per pixel)



- We want to blow it up to poster size (say, zoom in by a factor of 16)
- First try: repeat each row 16 times, then repeat each column 16 times

# Zooming: First attempt



- That didn't work so well
- We need a better way to find the in between values
- Let's consider one horizontal slice through the image (one scanline)



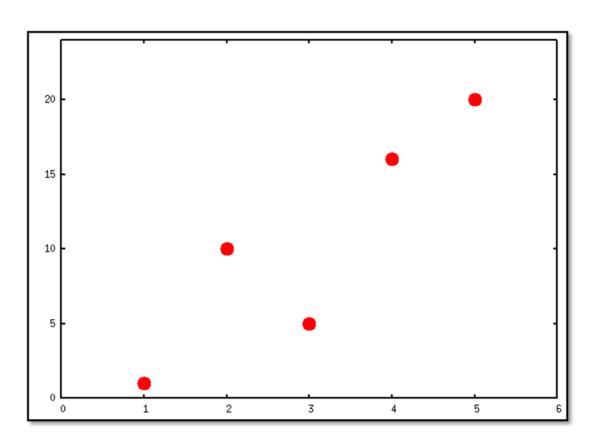
#### To Matlab



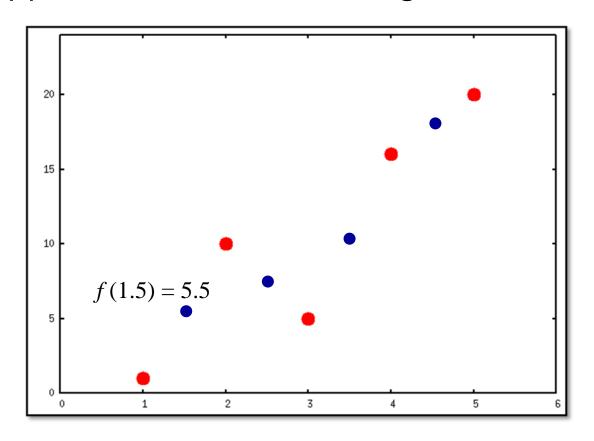
- Problem statement:
- We are given the values of a function f at a few locations, e.g., f(1), f(2), f(3), ...
- Want to find the rest of the values
  - What is f(1.5)?
- This is called interpolation
- We need some kind of model that predicts how the function behaves

#### Example:

$$f(1) = 1$$
,  $f(2) = 10$ ,  $f(3) = 5$ ,  $f(4) = 16$ ,  $f(5) = 20$ 

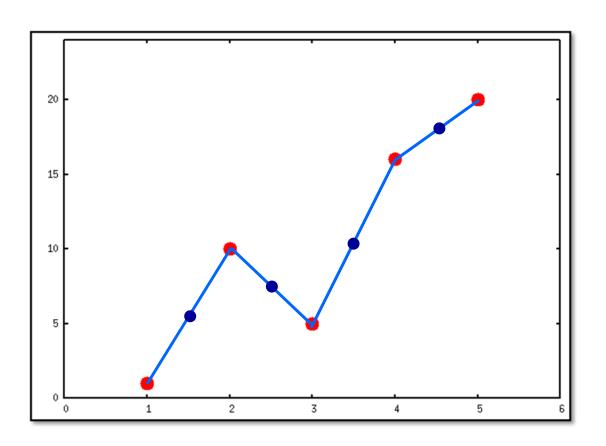


- How can we find f(1.5)?
- One approach: take the average of f(1) and f(2)



## Linear interpolation (lerp)

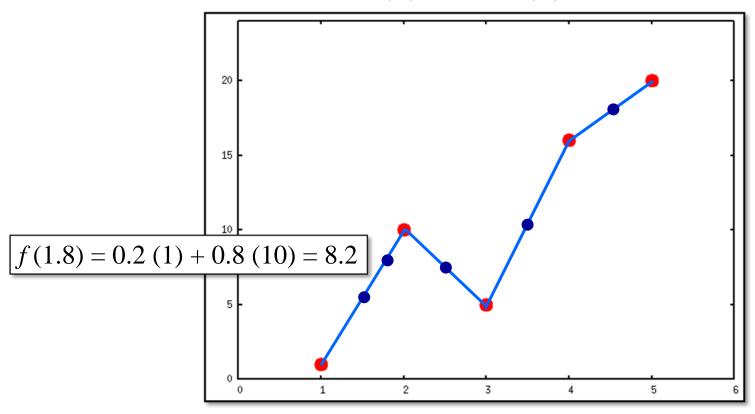
Fit a line between each pair of data points



#### Linear interpolation

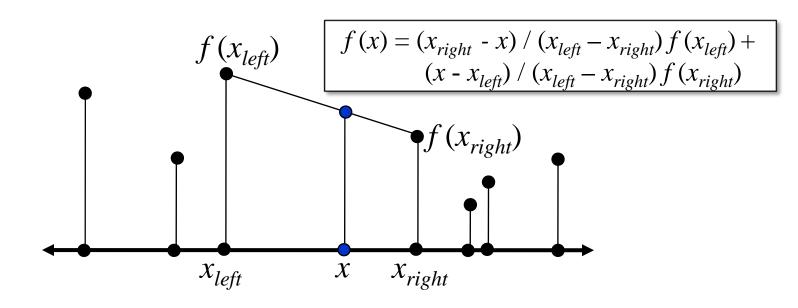
What is f(1.8)?

Answer: 0.2 f(1) + 0.8 f(2)



#### Linear interpolation

• To compute f(x), find the two points  $x_{left}$  and  $x_{right}$  that x lies between

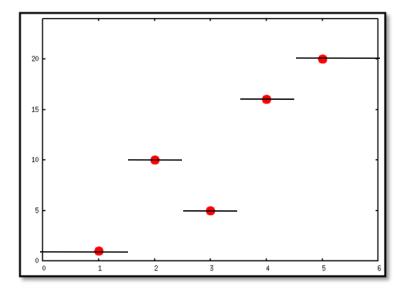


#### Nearest neighbor interpolation

The first technique we tried

We use the value of the data point we are

closest to



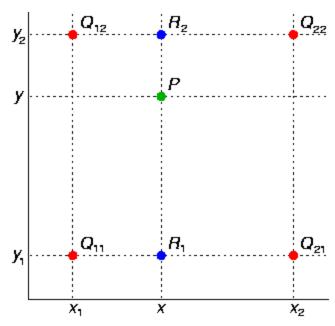
This is a fast way to get a bad answer

#### Bilinear interpolation

- What about in 2D?
  - Interpolate in x, then in y

#### Example

- We know the red values
- Linear interpolation in x between red values gives us the blue values
- Linear interpolation in y between the blue values gives us the answer



http://en.wikipedia.org/wiki/ Bilinear\_interpolation

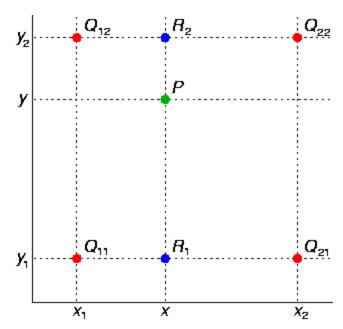
#### Bilinear interpolation

$$f(x,y) \approx \frac{f(Q_{11})}{(x_2 - x_1)(y_2 - y_1)}(x_2 - x)(y_2 - y)$$

$$+ \frac{f(Q_{21})}{(x_2 - x_1)(y_2 - y_1)}(x - x_1)(y_2 - y)$$

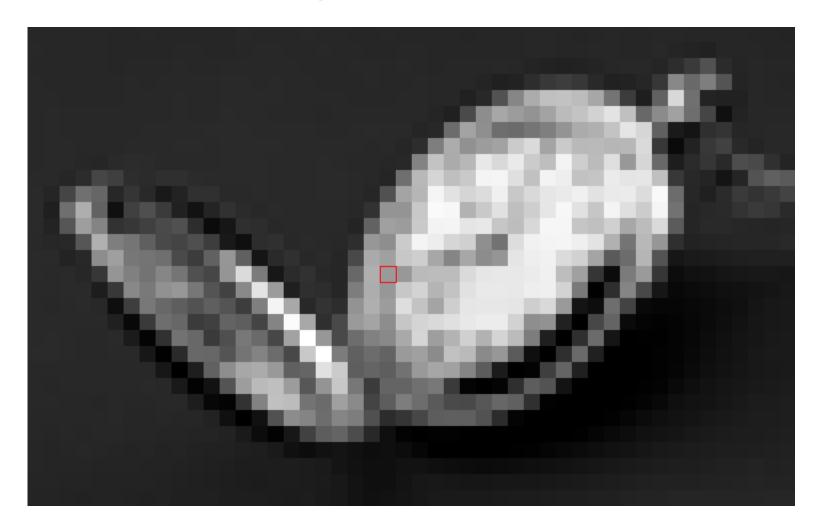
$$+ \frac{f(Q_{12})}{(x_2 - x_1)(y_2 - y_1)}(x_2 - x)(y - y_1)$$

$$+ \frac{f(Q_{22})}{(x_2 - x_1)(y_2 - y_1)}(x - x_1)(y - y_1).$$



http://en.wikipedia.org/wiki/ Bilinear\_interpolation

## Nearest neighbor interpolation

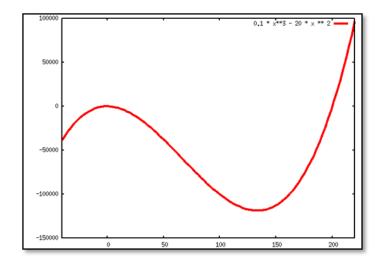


## Bilinear interpolation



#### **Beyond linear interpolation**

- Fits a more complicated model to the pixels in a neighborhood
- E.g., a cubic function

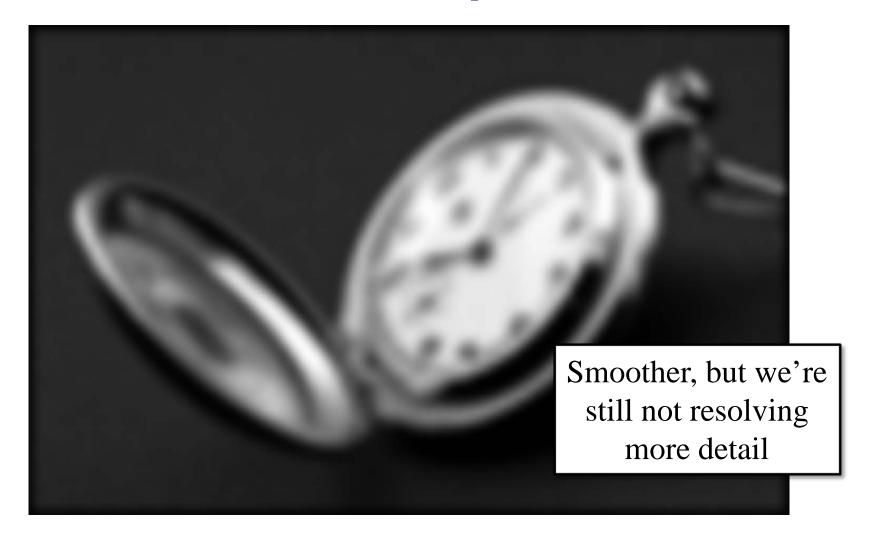


http://en.wikipedia.org/wiki/Bicubic\_interpolation

## Bilinear interpolation

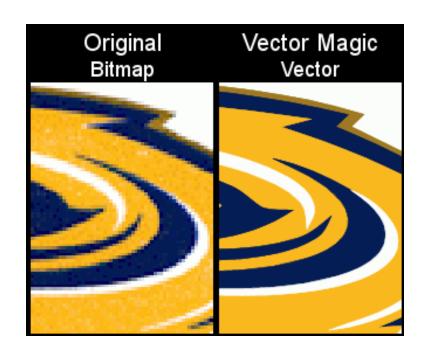


#### Bicubic interpolation



#### Even better interpolation

 Detect curves in the image, represents them analytically





#### Even better interpolation



nearest-neighbor interpolation



hq4x filter

SNES resolution: 256x224

Typical PC resolution: 1920x1200

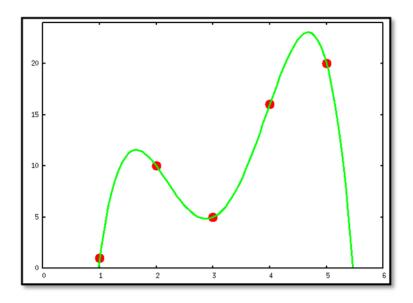




As seen in ZSNES

## Polynomial interpolation

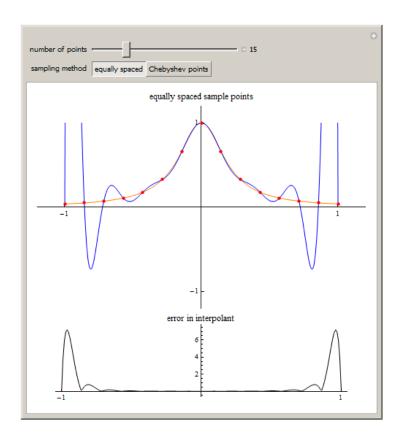
• Given n points to fit, we can find a polynomial p(x) of degree n-1 that passes through every point exactly



$$p(x) = -2.208 x^4 + 27.08x^3 - 114.30 x^2 + 195.42x - 104$$

### Polynomial interpolation

For large n, this doesn't work so well...



#### Other applications of interpolation

Computer animation (keyframing)





#### Gray2Color







### Limits of interpolation

- Can you prove that it is impossible to interpolate correctly?
- Suppose I claim to have a correct way to produce an image with 4x as many pixels
  - Correct, in this context, means that it gives what a better camera would have captured
  - Can you prove this cannot work?
- Related to impossibility of compression

#### Example algorithm that can't exist

- Consider a compression algorithm, like zip
  - Take a file F, produce a smaller version F'
  - Given F', we can uncompress to recover F
  - This is lossless compression, because we can "invert" it
    - MP3, JPEG, MPEG, etc. are not lossless

 Claim: there is no such algorithm that always produces a smaller file F' for every input file F

#### Proof of claim (by contradiction)

- Pick a file F, produce F' by compression
  - F' is smaller than F, by assumption
- Now run compression on F'
  - Get an even smaller file, F"
- At the end, you've got a file with only a single byte (a number from 0 to 255)
  - Yet by repeatedly uncompressing this you can eventually get F
- However, there are more than 256 different files F that you could start with!

#### Conclusions

- 1. Some files will get larger if you compress them (usually files with random data)
- 2. We can't (always) correctly recover missing data using interpolation

3. A low-res image can represent multiple

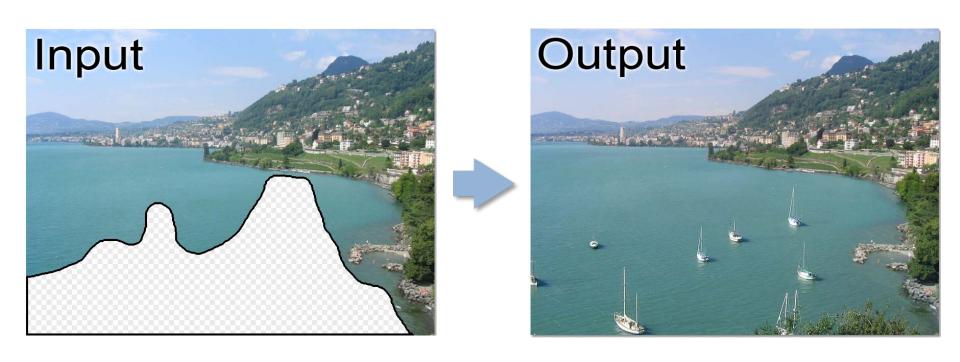
high-res images



#### Extrapolation

- Suppose you only know the values f(1), f(2), f(3), f(4) of a function
  - What is f(5)?
- This problem is called extrapolation
  - Much harder than interpolation: what is outside the image?
  - For the particular case of temporal data, extrapolation is called prediction (what will the value of MSFT stock be tomorrow?)
  - If you have a good model, this can work well

#### Image extrapolation



<a href="http://graphics.cs.cmu.edu/projects/scene-completion/">http://graphics.cs.cmu.edu/projects/scene-completion/</a><a href="http://graphics.cs.cmu.edu/projects/scene-completion/">http://graphics.cs.cmu.edu/projects/scene-completion/</a></a><a href="http://graphics.cmu.edu/projects/scene-completion/">http://graphics.cm

