

# Linked lists



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# Administrivia

- Assignment 2, Part 2 due tomorrow
  - Please don't wait until the last minute to finish (the last two problems are challenging)
- Assignment 3 will be posted tomorrow
  - Due in two weeks (Friday, 3/6)
- Prelim 1 next Thursday, 2/26 in class
  - Review session: Tuesday or Wednesday evening?
  - Topics include: running time, graphs, linked lists

# Making quickselect fast on non-random input

- The version of quickselect in A2 can be **very** slow
- What is the problem?
- How can we fix it?

# Conditionals with multiple branches

- What if we want the robot to correctly obey a traffic signal?

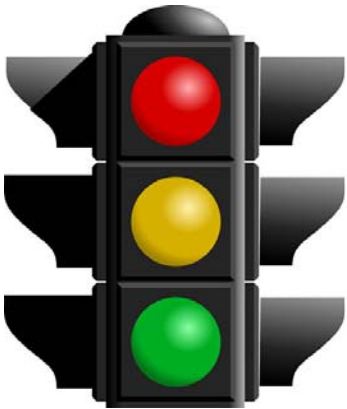


```
L = getLightColor();  
if L == 'red'  
    robotStop();  
end  
if L == 'green'  
    robotDriveStraight(r, 10, 100);  
end  
if L == 'yellow'  
    robotDriveStraight(r, 100, 100);  
end  
if L ~= 'red' && L ~= 'green' && L ~= 'yellow'  
    fprintf('Unknown light color\n');  
end
```

# Conditionals with multiple branches

- What if we want the robot to correctly obey a traffic signal?

```
L = getLightColor();
if L == 'red'
    robotStop();
else
    if L == 'green'
        robotDriveStraight(r, 10, 100);
    else
        if L == 'yellow'
            robotDriveStraight(r, 100, 100);
        else
            fprintf('Unknown light color\n');
        end
    end
end
end
```



# Conditionals with multiple branches

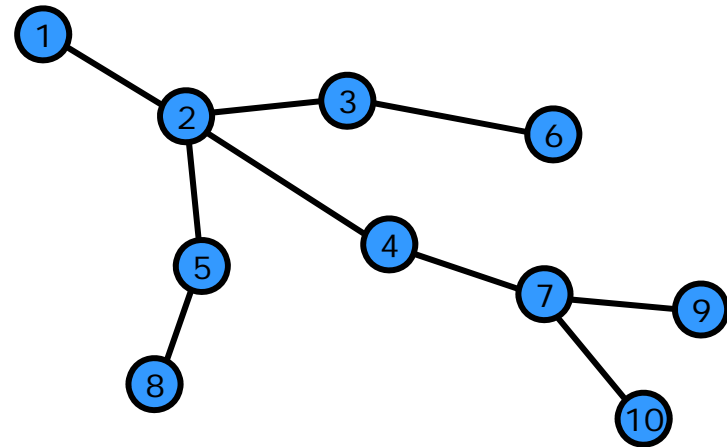
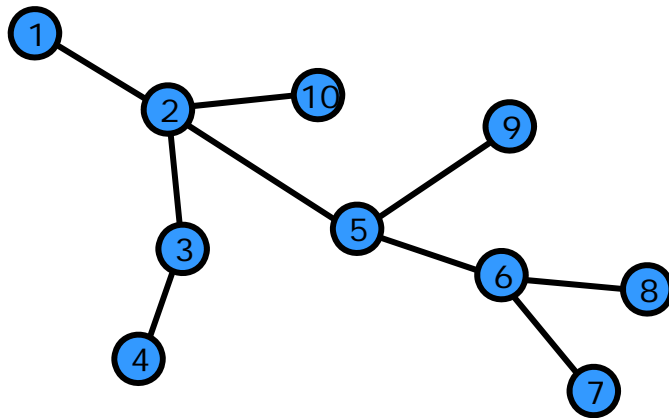
- What if we want the robot to correctly obey a traffic signal?



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    robotDriveStraight(r, 100, 100);  
else  
    fprintf('Unknown light color\n');  
end
```

# Last time

- Graph traversal



- Two types of todo lists:
  - Stacks → Depth-first search
  - Queues → Breadth-first search

# Last time

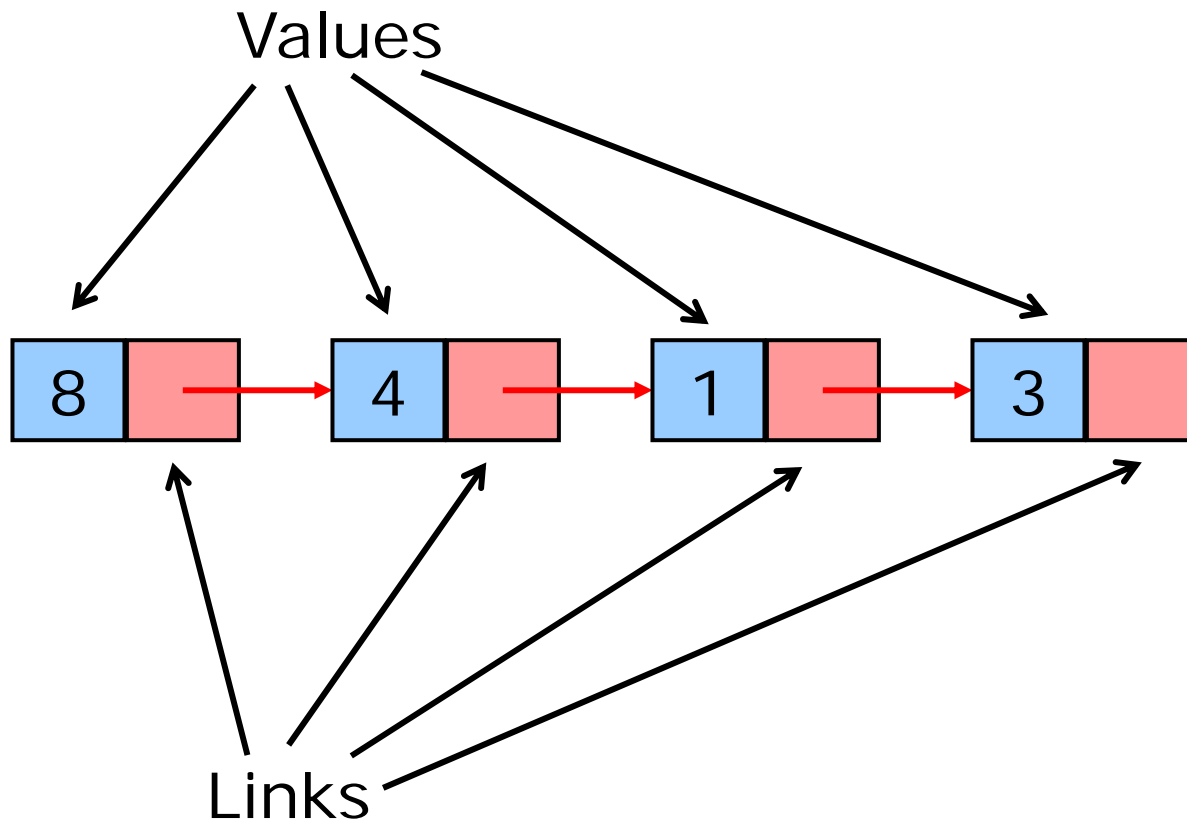
- Implementing a stack and queue using arrays
- What went wrong?
- Today we'll talk about a better approach



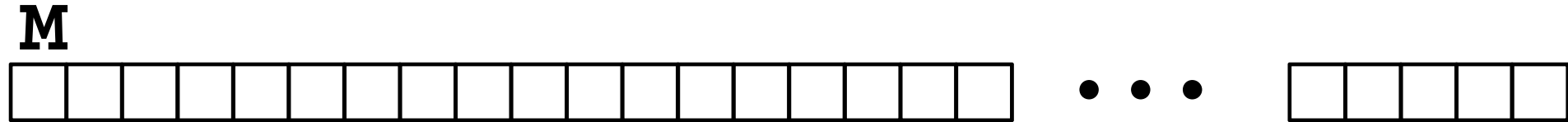
# Linked lists

- Alternative to an array
- Every element (cell) has two parts:
  1. A value (as in an array)
  2. A link to the next cell

# Linked lists



# Linked lists as memory arrays

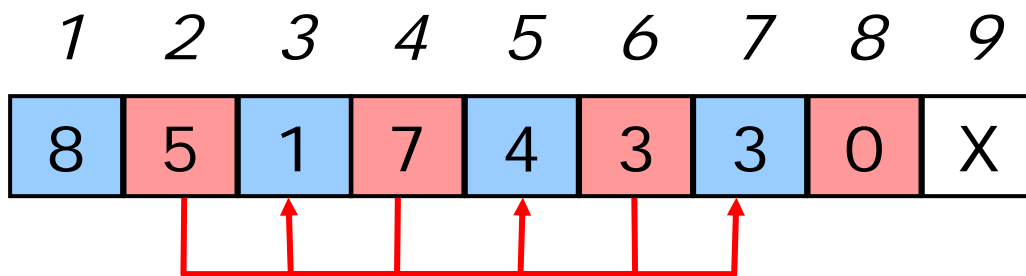
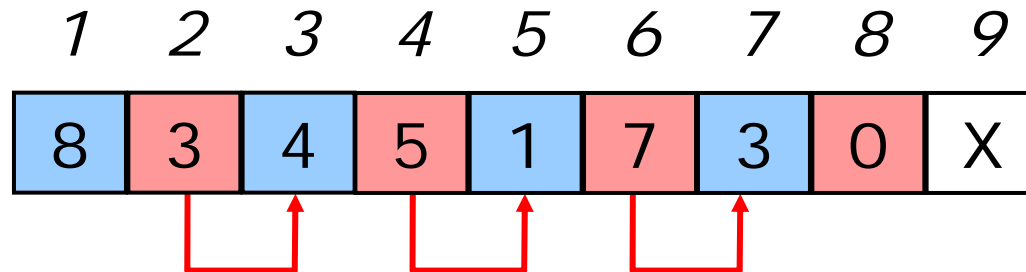
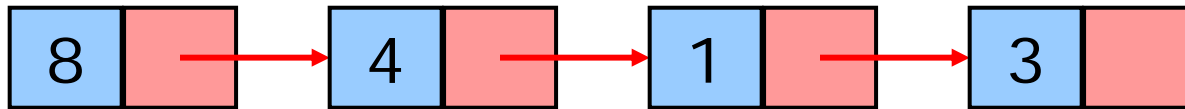


- We'll implement linked lists using M
- A cell will be represented by a pair of adjacent array entries

# A few details

- I will draw odd numbered entries in blue and even ones in red
  - Odd entries are values
    - Number interpreted as list elements
  - Even ones are links
    - Number interpreted as index of the next cell
    - AKA *location, address, or **pointer***
- The first cell is M(1) and M(2) (for now)
- The last cell has 0, i.e. pointer to M(0)
  - Also called a “null pointer”

# Example



# Traversing a linked list

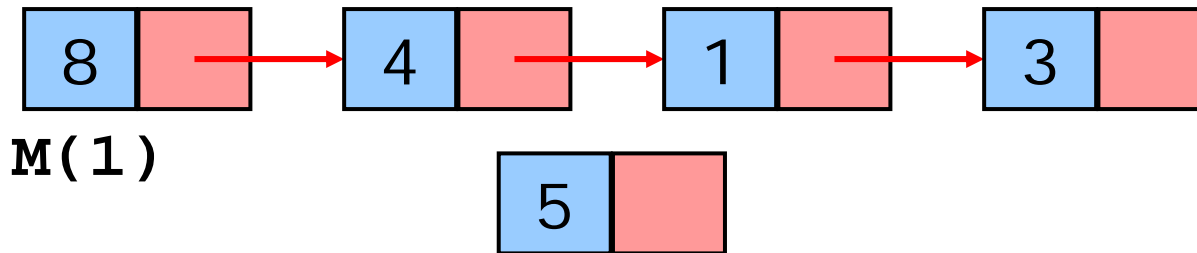
- Start at the first cell,  $[M(1), M(2)]$
- Access the first value,  $M(1)$
- The next cell is at location  $c = M(2)$
- If  $c = 0$ , we're done
- Otherwise, access the next value,  $M(c)$
- The next cell is at location  $c = M(c+1)$
- Keep going until  $c = 0$

# Inserting an element – arrays

- How can we insert an element  $\mathbf{x}$  into an array  $\mathbf{A}$ ?
- Depends where it needs to go:
  - End of the array:  
 $\mathbf{A} = [\mathbf{A} \ \mathbf{x}];$
  - Middle of the array (say, between elements  $A(5)$  and  $A(6)$ )?
  - Beginning of the array?

# Inserting an element – linked lists

- Create a new cell and splice it into the list



- Splicing depends on where the cell goes:
  - How do we insert:
    - At the end?
    - In the middle?
    - At the beginning?



# Adding a header

- We can represent the linked list just by the initial cell, but this is problematic
  - Problem with inserting at the beginning
- Instead, we add a header – a few entries that are not cells, but hold information about the list
  1. A pointer to the first element
  2. A count of the number of elements

# Linked list insertion

Initial list

	1	2	3	4	5	6	7	8	9	10	11	12	13
	5	2	2	0	1	3	X	X	X	X	X	X	X

First element starts at 5

Size of list is 2

	1	2	3	4	5	6	7	8	9	10	11	12	13
	5	3	2	7	1	3	5	0	X	X	X	X	X

Insert a 5 at end

	1	2	3	4	5	6	7	8	9	10	11	12	13
	5	3	2	7	1	3	5	0	X	X	X	X	X

Insert an 8 after the 1

	1	2	3	4	5	6	7	8	9	10	11	12	13
	5	4	2	7	1	9	5	0	8	3	X	X	X

Insert a 6 at the start

	1	2	3	4	5	6	7	8	9	10	11	12	13
	11	5	2	0	1	9	5	0	8	3	6	5	X

# Linked list deletion

- We can also delete cells
- Simply update the header and change one pointers (to skip over the deleted element)
- Deleting things is the source of many bugs in computer programs
  - You need to make sure you delete something once, and only once

# Linked list deletion

Initial list

1	2	3	4	5	6	7	8	9	10	11	12	13
5	4	2	7	1	9	5	0	8	3	X	X	X

Delete the last cell

1	2	3	4	5	6	7	8	9	10	11	12	13
5	3	2	0	1	9	5	0	8	3	X	X	X

Delete the 8

1	2	3	4	5	6	7	8	9	10	11	12	13
5	2	2	0	1	3	5	0	8	3	X	X	X

Delete the first cell

1	2	3	4	5	6	7	8	9	10	11	12	13
3	1	2	0	1	3	5	0	8	3	X	X	X

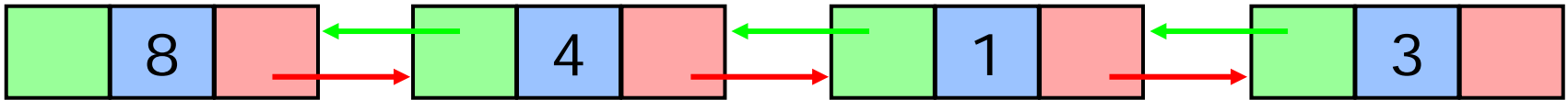
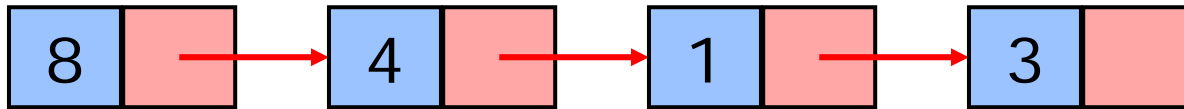
# Linked lists – running time

- We can insert an item (at the front) in constant ( $O(1)$ ) time
  - Just manipulating the pointers
  - As long as we know where to *allocate* the cell
- We can delete an element (at the front) in constant time

# Linked lists – running time

- What about inserting / deleting from the end of the list?
  
  
  
  
  
  
  
  
  
  
- How can we fix this?

# Doubly linked lists



# A doubly-linked list in memory

