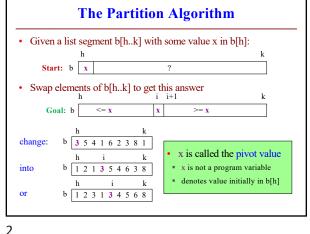
Recall Our Problem

- Both insertion, selection sort are **nested loops**
 - Outer loop over each element to sort
 - Inner loop to put next element in place
 - Each loop is n steps. $n \times n = n^2$
- To do better we must *eliminate* a loop
 - But how do we do that?
 - What is like a loop? **Recursion!**
 - First need an *intermediate* algorithm

1



Designing the Partition Algorithm

• Given a list b[h..k] with some value x in b[h]:

```
h k
Start: b x ?
```

• Swap elements of b[h..k] to get this answer

Indices b, h important! Might partition only part

3

Implementating the Partition Algorithm def partition(b, h, k): """Partition list b[h..k] around a pivot x = b[h]""" i = h; j = k+1; x = b[h]while i < j-1: if b[i+1] >= x: partition(b,h,k), not partition(b[h:k+1]) # Move to end of block. Remember, slicing always copies the list! swap(b,i+1,j-1)We want to partition the original list j = j - 1 else: # b[i+1] < x swap(b,i,i+1) i = i + 1return i

4

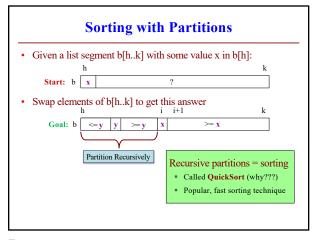
Partition Algorithm Implementation

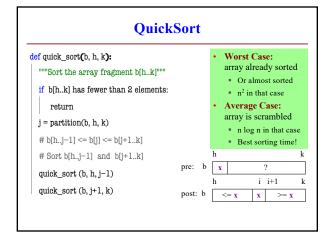
Why is this Useful?

- Will use this algorithm to replace inner loop
 - The inner loop cost us n swaps every time
- Can this reduce the number of swaps?
 - Worst case is k-h swaps
 - This is n if partitioning the whole list
 - But less if only partitioning part
- Idea: Break up list and partition only part?
 - This is **Divide-and-Conquer!**

5 6

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So Does that Solve It?

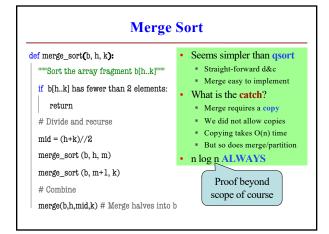
Worst case still seems bad! Still n² But only happens in small number of cases Just happens that case is common (already sorted) Can greatly reduce issue with randomization Swap start with random element in list Now pivot is random and already sorted unlikely

Can We Do Better?

- · Recursion seems to be the solution
 - Partitioned the list into two halves
 - Recursively sorted each half
- How about a traditional divide-and-conquer?
 - **Divide** the list into two halves
 - Recursively sort the two halves
 - **Combine** the two sort halves
- How do we do the last step?

9

10



What Does Python Use? The sort() method is Timsort Invented by Tim Peters in 2002 Combination of insertion sort and merge sort Why a combination of the two? Merge sort requires copies of the data Copying pays off for large lists, but not small lists Insertion sort is not that slow on small lists Balancing two properly still gives n log n

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