

Module 18

Nested Lists

Motivating this Course Module

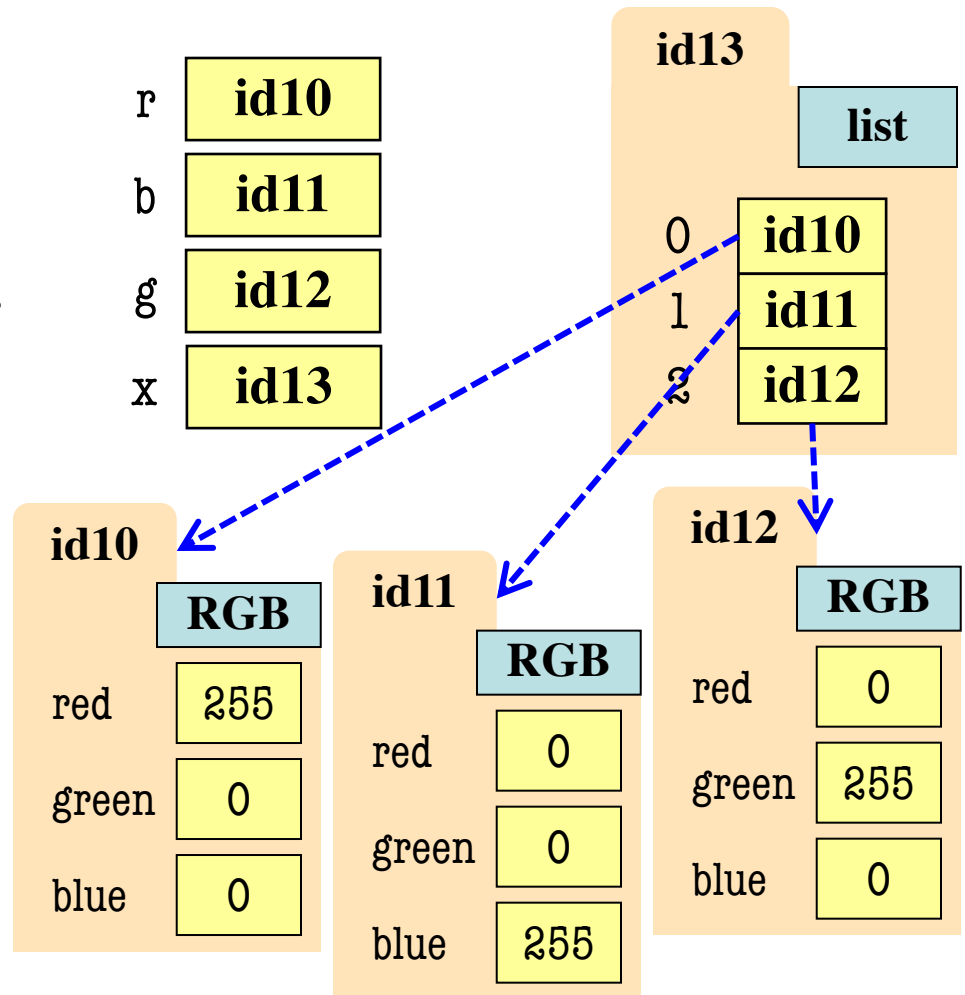
- In previous video series, introduced lists
 - All our examples had *primitives* in the lists
 - So we only showed one folder in visualization
 - **Demo:** $x = [5,6,5,9]$
- But lists can contain anything!
 - What if they can contain objects?
 - Yes, primitives = objects, but ignore folders
 - We mean if we cannot ignore the folders

Lists of Objects

- List positions are variables
 - Can store base types
 - But cannot store folders
 - Can store folder identifiers
- Folders linking to folders
 - Top folder for the list
 - Other folders for contents

- Example:

```
>>> r = introcs.RGB(255,0,0)
>>> b = introcs.RGB(0,0,255)
>>> g = introcs.RGB(0,255,0)
>>> x = [r,b,g]
```



Nested Lists

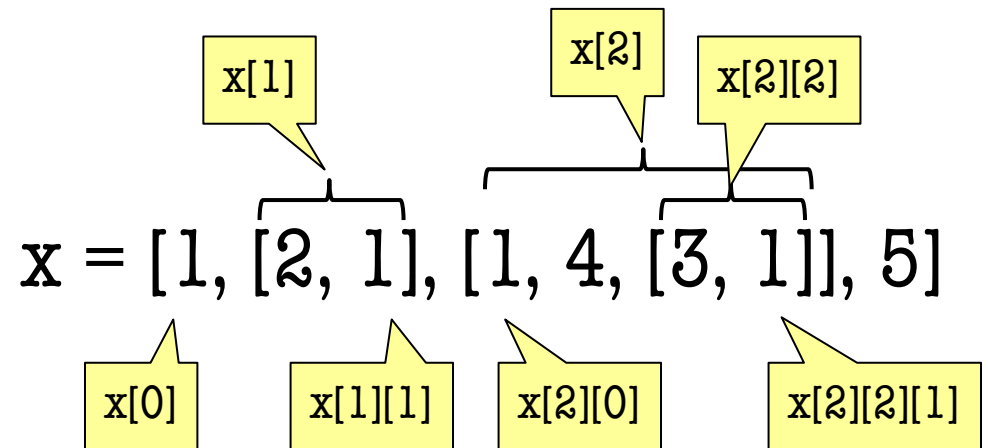
- We have seen that lists can hold any objects
 - Lists are objects
 - Therefore lists can hold other lists!
- Known as **nested or multidimensional list**

$a = [2, 1]$

$b = [3, 1]$

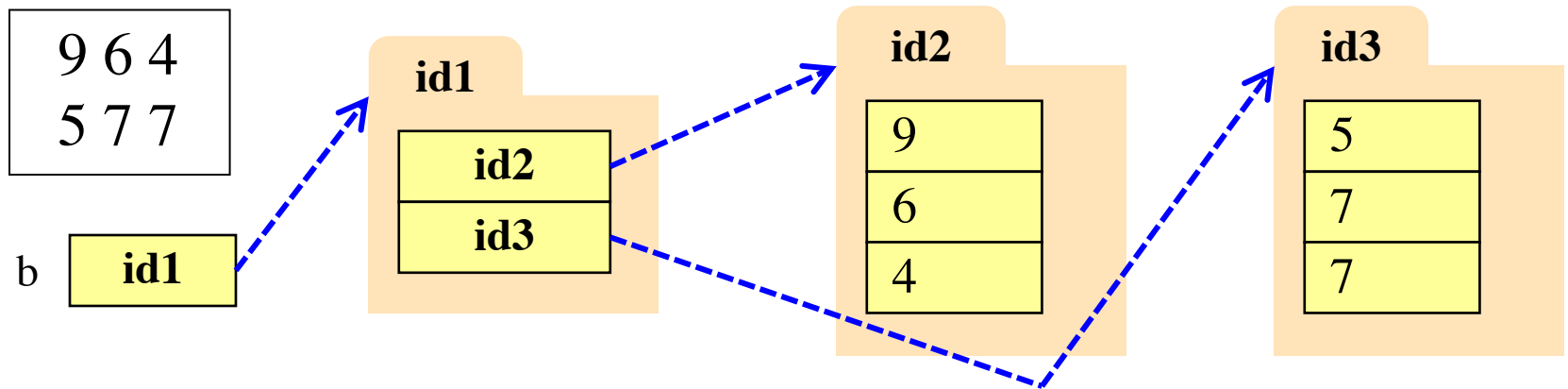
$c = [1, 4, b]$

$x = [1, a, c, 5]$



How Multidimensional Lists are Stored

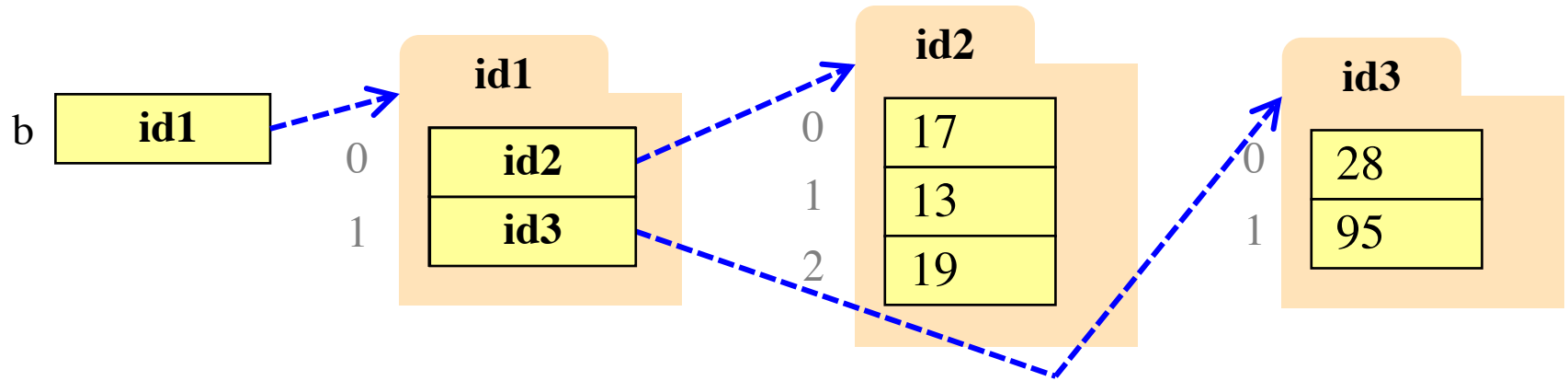
- $b = [[9, 6, 4], [5, 7, 7]]$



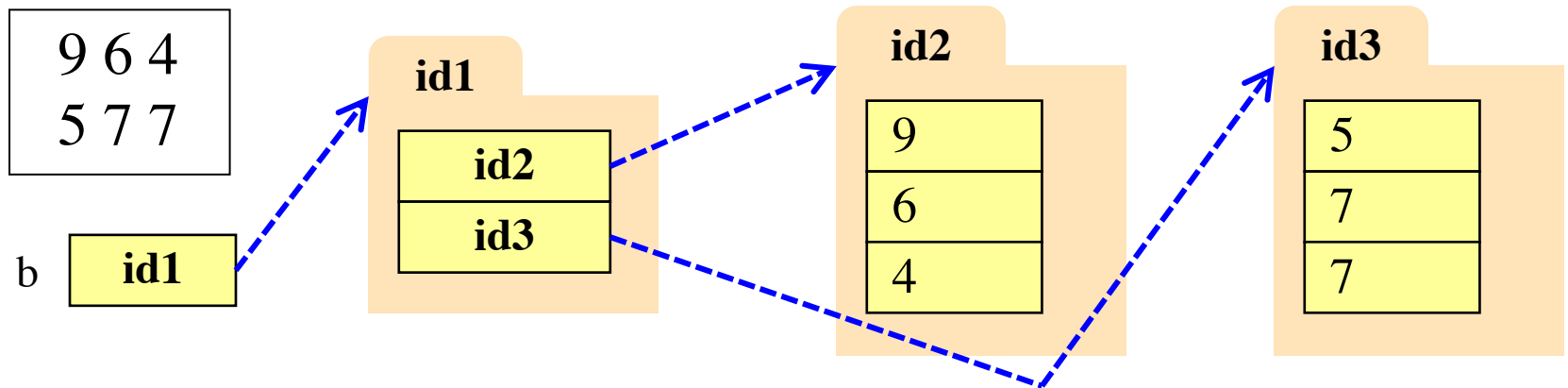
- b holds name of a one-dimensional list
 - Has $\text{len}(b)$ elements
 - Its elements are (the names of) 1D lists
- $b[i]$ holds the name of a one-dimensional list (of ints)
 - Has $\text{len}(b[i])$ elements

Ragged Lists vs Tables

- Ragged is 2d uneven list: $b = [[17,13,19],[28,95]]$

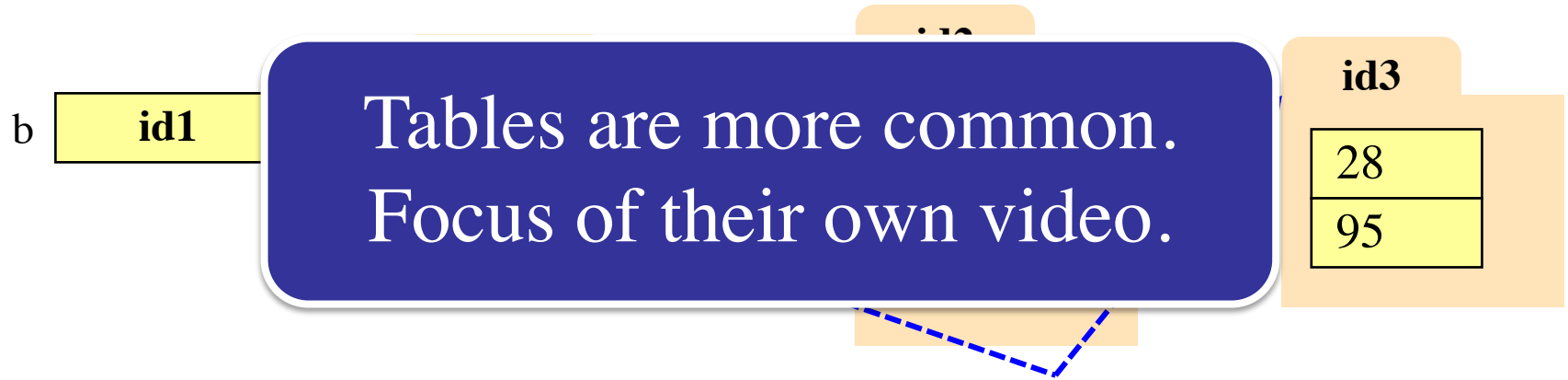


- Table is 2d uniform list: $b = [[9,6,4],[5,7,7]]$

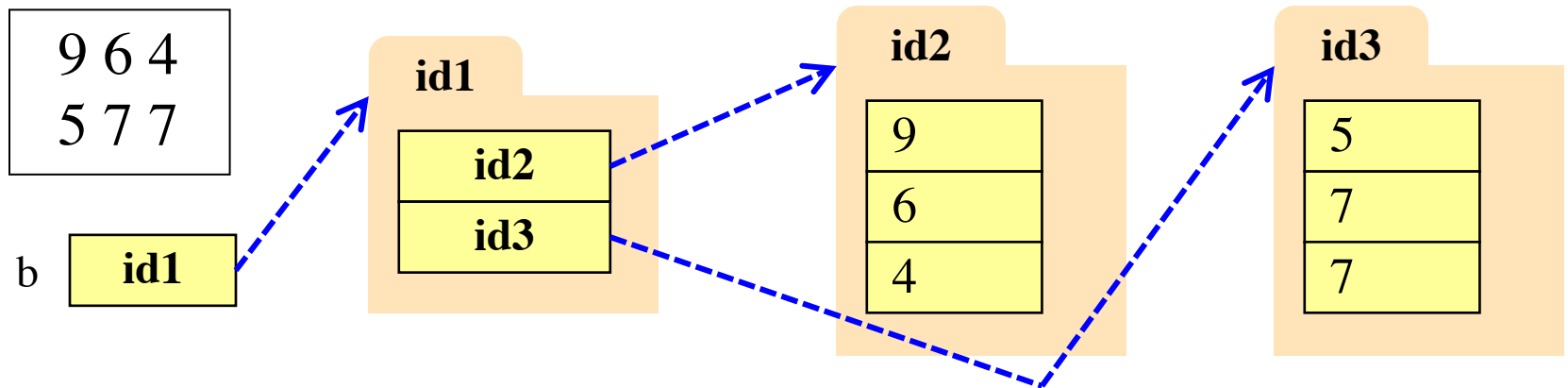


Ragged Lists vs Tables

- Ragged is 2d uneven list: $b = [[17,13,19],[28,95]]$



- Table is 2d uniform list: $b = [[9,6,4],[5,7,7]]$



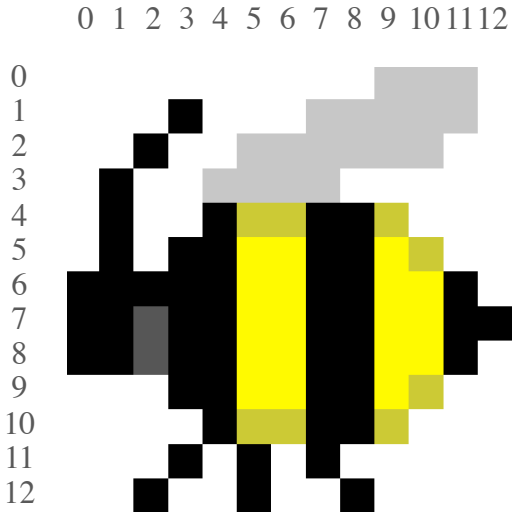
Tables are a Common Type of Data

Spreadsheet

	0	1	2	3
0	5	4	7	3
1	4	8	9	7
2	5	1	2	3
3	4	1	2	9
4	6	7	8	0

table.csv

Image



bee.xlsx

Representing Tables as Lists

Spreadsheet

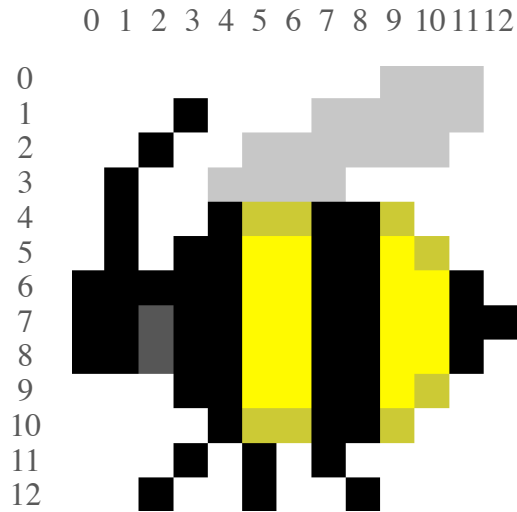
	0	1	2	3
0	5	4	7	3
1	4	8	9	7
2	5	1	2	3
3	4	1	2	9
4	6	7	8	0

Each row,
col has a
value

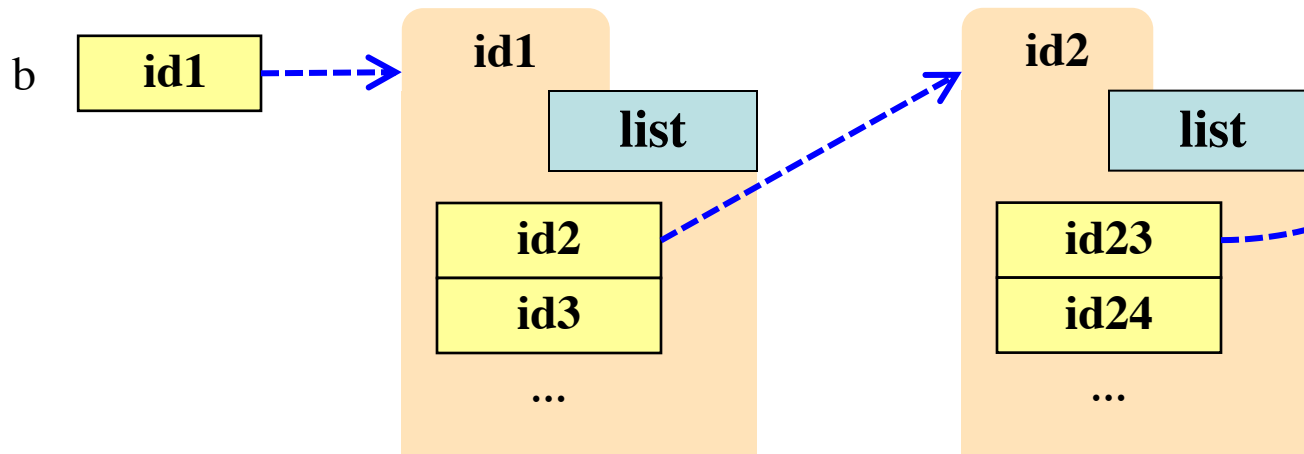
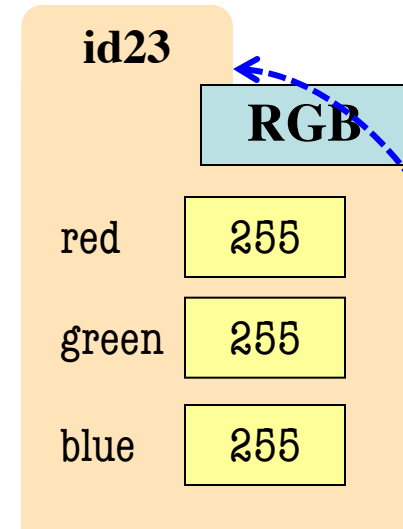
- Represent as 2d list
 - Each table row a list
 - List of all rows
 - **Row major order**
- Column major exists
 - Less common to see
 - Limited to some scientific applications

```
d = [[5,4,7,3],[4,8,9,7],[5,1,2,3],[4,1,2,9],[6,7,8,0]]
```

Image Data: 2D Lists of Pixels



smile.py



Overview of Two-Dimensional Lists

- Access value at row 3, col 2:

`d[3][2]`

- Assign value at row 3, col 2:

`d[3][2] = 8`

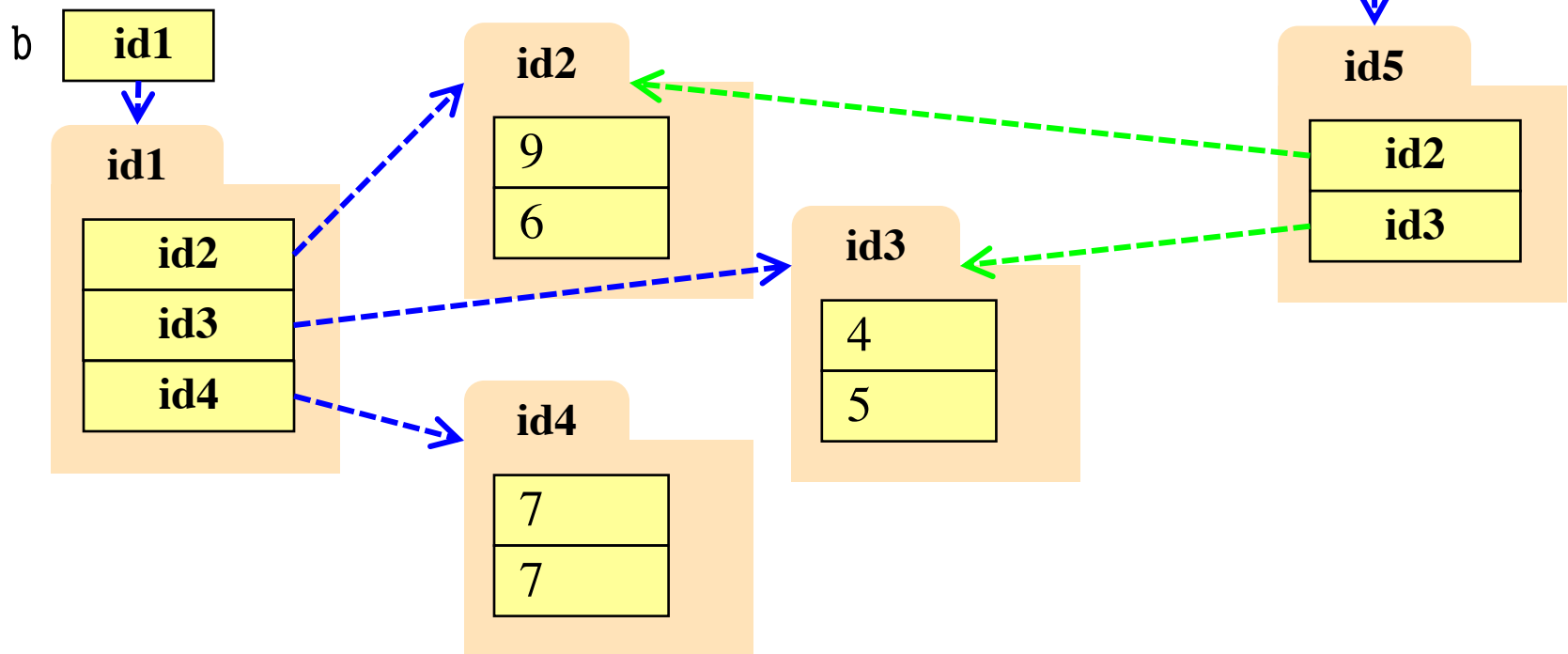
- **There is an odd symmetry**

- Number of rows of `d`: `len(d)`
- Number of cols in row `r` of `d`: `len(d[r])`

	0	1	2	3
d 0	5	4	7	3
1	4	8	9	7
2	5	1	2	3
3	4	1	2	9
4	6	7	8	0

Slices and Multidimensional Lists

- Only “top-level” list is copied.
- Contents of the list are not altered
- $b = [[9, 6], [4, 5], [7, 7]]$



Slices and Multidimensional Lists

- Create a nested list

```
>>> b = [[9,6],[4,5],[7,7]]
```
- Get a slice

```
>>> x = b[:2]
```
- Append to a row of x

```
>>> x[1].append(10)
```
- x now has nested list

```
[[9, 6], [4, 5, 10]]
```

- What are the contents of the list (with name) in **b**?

A: [[9,6],[4,5],[7,7]]

B: [[9,6],[4,5,10]]

C: [[9,6],[4,5,10],[7,7]]

D: [[9,6],[4,10],[7,7]]

E: I don't know

Shallow vs. Deep Copy

- **Shallow copy:** Copy top-level list
 - Happens when slice a multidimensional list
- **Deep copy:** Copy top and all nested lists
 - Requires a special function: `copy.deepcopy`
- **Example:**

```
>>> import copy
```

```
>>> a = [[1,2],[2,3]]
```

```
>>> b = a[:]           # Shallow copy
```

```
>>> c = copy.deepcopy(a) # Deep copy
```

Relationship to Standard Lists

- Functions on nested lists similar to lists
 - Go over (nested) list with *for-loop*
 - Use *accumulator* to gather the results
- But two important differences
 - Need **multiple for-loops**
 - One for each part/dimension of loop
 - In some cases need **multiple accumulators**
 - Latter true when result is new table

Simple Example

```
def all_nums(table):
```

```
    """Returns True if table contains only numbers
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

```
    result = True
```

Accumulator

```
    # Walk through table
```

```
    for row in table:
```

First Loop

```
        # Walk through the row
```

```
        for item in row:
```

Second Loop

```
            if not type(item) in [int,float]:
```

```
                result = False
```

```
    return result
```


Transpose: A Trickier Example

```
def transpose(table):
```

```
    """Returns: copy of table with rows and columns swapped
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

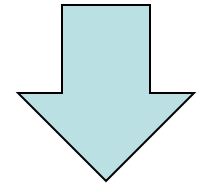
```
    result = []                # Result (new table) accumulator
```

```
    # Loop over columns
```

```
        # Add each column as a row to result
```

```
    return result
```

1	2
3	4
5	6



1	3	5
2	4	6

Transpose: A Trickier Example

```
def transpose(table):
```

```
    """Returns: copy of table with rows and columns swapped
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

```
    numrows = len(table)    # Need number of rows
```

```
    numcols = len(table[0]) # All rows have same no. cols
```

```
    result = []             # Result (new table) accumulator
```

```
    for m in range(numcols):
```

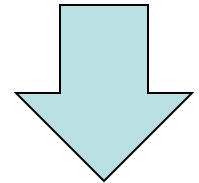
```
        # Get the column elements at position m
```

```
        # Make a new list for this column
```

```
        # Add this row to accumulator table
```

```
    return result
```

1	2
3	4
5	6



1	3	5
2	4	6

Transpose: A Trickier Example

```
def transpose(table):
```

```
    """Returns: copy of table with rows and columns swapped
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

```
    numrows = len(table)    # Need number of rows
```

```
    numcols = len(table[0]) # All rows have same no. cols
```

```
    result = []            # Result (new table) accumulator
```

```
    for m in range(numcols):
```

```
        row = []           # Single row accumulator
```

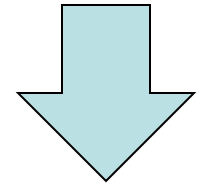
```
        for n in range(numrows):
```

```
            row.append(table[n][m]) # Create a new row list
```

```
        result.append(row)      # Add result to table
```

```
    return result
```

1	2
3	4
5	6



1	3	5
2	4	6

Transpose: A Trickier Example

```
def transpose(table):
```

```
    """Returns: copy of table with rows and columns swapped
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

```
    numrows = len(table)    # Need number of rows
```

```
    numcols = len(table[0]) # All rows have same no. cols
```

```
    result = []             # accumulator
```

```
    for m in range(numcols):
```

```
        row = []           # accumulator
```

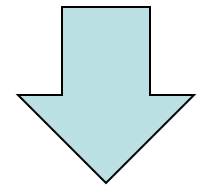
```
        for n in range(numrows):
```

```
            row.append(table[n][m]) # Create a new row list
```

```
        result.append(row)         # Add result to table
```

```
    return result
```

1	2
3	4
5	6



1	3	5
2	4	6

Accumulator
for each loop

Relationship to Standard Lists

- Functions on nested lists similar to lists
 - Do not loop over the list (modifying it)
 - Loop over *range of positions* instead
 - No *accumulator* or return statement
- But one important difference
 - May need **multiple for-loops**
 - Depends on if modifying rows or entries

Simple Example

```
def add_ones(table):
```

```
    """Adds one to every number in the table
```

```
    Preconditions: table is a 2d List,
```

```
    all table elements are int"""
```

```
    # Walk through table
```

```
    for rpos in range(len(table)):
```

```
        # Walk through each column
```

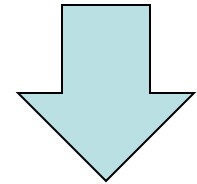
```
        for cpos in range(len(table[rpos])):
```

```
            table[rpos][cpos] = table[rpos][cpos]+1
```

```
    # No return statement
```

Do not loop
over the table

1	3	5
2	4	6



2	4	6
3	5	7

Simple Example

```
def add_ones(table):
```

```
    """Adds one to every number in the table
```

```
    Preconditions: table is a 2d List,
```

```
    all table elements are int"""
```

```
    # Walk through table
```

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    for rpos in range(len(table)):
```

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        # Walk through each column
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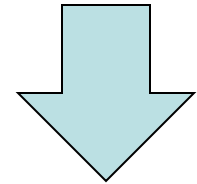
```
        for cpos in range(len(table[rpos])):
```

```
            table[rpos][cpos] = table[rpos][cpos]+1
```

```
    # No return statement
```

Note that
ragged is okay

1	3	5
2	4	6



2	4	6
3	5	7

Another Example

```
def strip(table,col):
```

```
    """Removes column col from the given table
```

```
    Preconditions: table is a (non-ragged) 2d List,
```

```
    col valid column"""
```

```
    # Walk through table
```

```
    for rpos in range(len(table)):
```

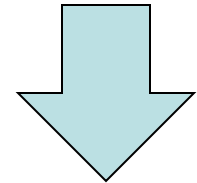
```
        # Modify each row to slice out column
```

```
        table[rpos] = table[rpos][:col] + table[rpos][col+1:]
```

```
    # No return statement
```

Do not loop
over the table

1	3	5
2	4	6



1	5
2	6