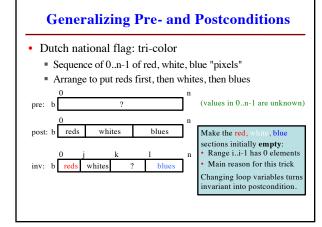
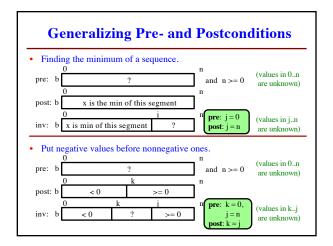
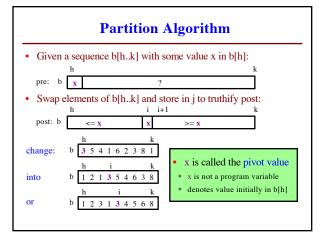


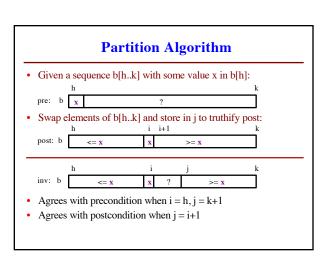
## **Developing Algorithms on Sequences**

- Specify the algorithm by giving its precondition and postcondition as pictures.
- Draw the invariant by drawing another picture that "generalizes" the precondition and postcondition
  - The invariant is true at the beginning and at the end
- The four loop design questions
  - 1. How does loop start (how to make the invariant true)?
  - 2. How does it stop (is the postcondition true)?
  - 3. How does the body make progress toward termination?
  - 4. How does the body keep the invariant true?









## **Partition Algorithm Implementation** def partition(b, h, k): """Partition list b[h..k] around a pivot x = b[h]""" i = h; j = k+1; x = b[h]# invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= xwhile i < j-1: if b[i+1] >= x: partition(b,h,k), not partition(b[h:k+1]) # Move to end of block. Remember, slicing always copies the list! $_swap(b,i+1,j-1)$ We want to partition the original list j=j-1 else: # b[i+1] < x \_swap(b,i,i+1) i = i + 1 # post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= xreturn i

## **Partition Algorithm Implementation** def partition(b, h, k): """Partition list b[h..k] around a pivot x = b[h]""" i = h; j = k+1; x = b[h]1 2 3 1 5 0 6 3 8 # invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= xwhile i < j-1: if b[i+1] >= x: # Move to end of block. $_swap(b,i+1,j-1)$ j=j-1 else: # b[i+1] < x \_swap(b,i,i+1) i = i + 1 # post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= xreturn i

