

Lecture 4

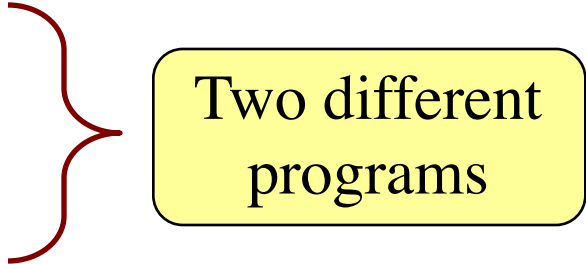
Defining Functions

Academic Integrity Quiz

- **Remember:** quiz about the course AI policy
 - Have posted grades for completed quizzes
 - Right now, missing ~125 enrolled students
 - If did not receive perfect, take it again
- If you are not aware of the quiz
 - Go to <http://www.cs.cornell.edu/courses/cs11110/>
 - Click **Academic Integrity** in side bar
 - Read and take quiz in CMS

Recall: Modules

- Modules provide extra functions, variables
 - **Example:** math provides `math.cos()`, `math.pi`
 - Access them with the `import` command
- Python provides a lot of them for us
- **This Lecture:** How to make modules
 - Komodo Edit to *make* a module
 - Python to *use* the module



Two different programs

We Write Programs to Do Things

- Functions are the **key doers**

Function Call

- Command to **do** the function

```
>>> plus(23)
```

```
24
```

```
>>>
```

Function Definition

- Defines what function **does**

```
def plus(n):
```

```
    return n+1
```

- **Parameter:** variable that is listed within the parentheses of a method header.
- **Argument:** a value to assign to the method parameter when it is called

We Write Programs to Do Things

- Functions are the **key doers**

Function Call

- Command to **do** the function

```
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Function
Header

Function Definition

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We Write Programs to Do Things

- Functions are the **key doers**

Function Call

- Command to **do** the function

```
>>> plus(23)
```

```
24
```

```
>>>
```

Function
Header

```
def plus(n):
```

```
    return n+1
```

Function
Body
(indented)

- **Parameter:** variable that is listed within the parentheses of a method header.
- **Argument:** a value to assign to the method parameter when it is called

We Write Programs to Do Things

- Functions are the **key doers**

Function Call

- Command to **do** the function

```
>>> plus(23)
```

```
24
```

argument to
assign to n

Function
Header

```
def plus(n):
```

```
    return n+1
```

declaration of
parameter n

Function
Body
(indented)

- **Parameter:** variable that is listed within the parentheses of a method header.
- **Argument:** a value to assign to the method parameter when it is called

Anatomy of a Function Definition

name

parameters

```
def plus(n):
```

Function Header

```
    """Returns the number n+1
```

Docstring
Specification

```
    Parameter n: number to add to  
    Precondition: n is a number"""
```

```
    x = n+1
```

Statements to
execute when called

```
    return x
```


Anatomy of a Function Definition

name

parameters

```
def plus(n):
```

Function Header

```
    """Returns the number n+1
```

Docstring
Specification

```
    Parameter n: number to add to  
    Precondition: n is a number"""
```

```
    x = n+1
```

Statements to
execute when called

```
    return x
```

The vertical line
indicates indentation

Use vertical lines when you write Python
on **exams** so we can see indentation

The **return** Statement

- **Format:** `return <expression>`
 - Used to evaluate *function call* (as an expression)
 - Also stops executing the function!
 - Any statements after a **return** are ignored
- **Example:** temperature converter function

`def to_centrigrade(x):`

```
    """Returns: x converted to centigrade"""
```

```
    return 5*(x-32)/9.0
```

A More Complex Example


Function Definition

```
def foo(a,b):  
    """Return something  
    Param a: number  
    Param b: number"""  
  
    x = a  
    y = b  
    return x*y+y
```

Function Call

```
>>> x = 2
```

```
>>> foo(3,4)
```

x 

What is in the box?

A More Complex Example

Function Definition

```
def foo(a,b):  
    """Return something  
    Param a: number  
    Param b: number"""  
  
    x = a  
    y = b  
    return x*y+y
```

Function Call

```
>>> x = 2
```

```
>>> foo(3,4)
```

x ?

What is in the box?

A: 2

B: 3

C: 16

D: Nothing!

E: I do not know

A More Complex Example

Function Definition

```
def foo(a,b):  
    """Return something  
    Param a: number  
    Param b: number"""  
  
    x = a  
    y = b  
    return x*y+y
```

Function Call

```
>>> x = 2
```

```
>>> foo(3,4)
```

x ?

What is in the box?

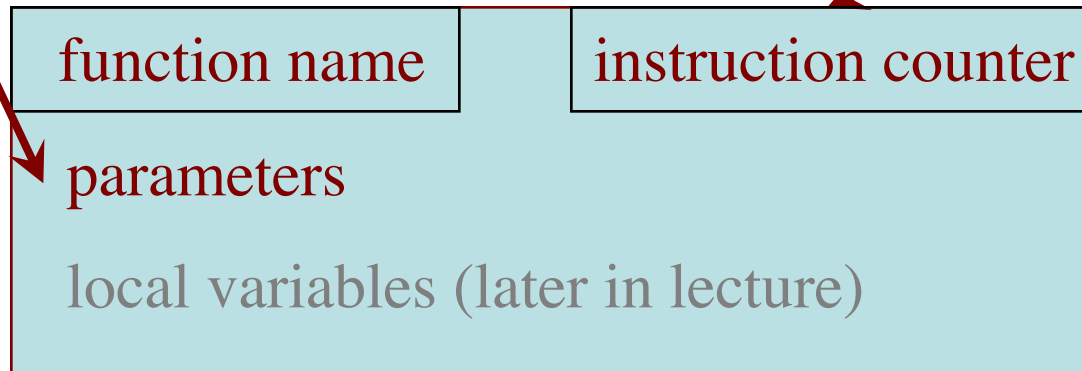
- A: 2 **CORRECT**
- B: 3
- C: 16
- D: Nothing!
- E: I do not know

Understanding How Functions Work

- **Function Frame:** Representation of function call
- A **conceptual model** of Python

Draw parameters
as variables
(named boxes)

- Number of statement in the
function body to execute next
- **Starts with 1**



Text (Section 3.10) vs. Class

Textbook

to_centrigrade

$x \rightarrow 50.0$

This Class

to_centrigrade

1

x **50.0**

Definition:

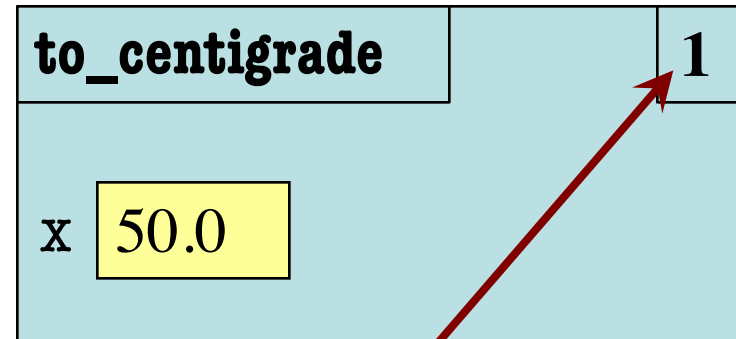
```
def to_centrigrade(x):  
    | return 5*(x-32)/9.0
```

Call: to_centrigrade(50.0)

Example: to_centigrade(50.0)

1. Draw a frame for the call
2. Assign the argument value to the parameter (in frame)
3. Execute the function body
 - Look for variables in the frame
 - If not there, look for global variables with that name
4. Erase the frame for the call

Initial call frame
(before exec body)



next line to execute

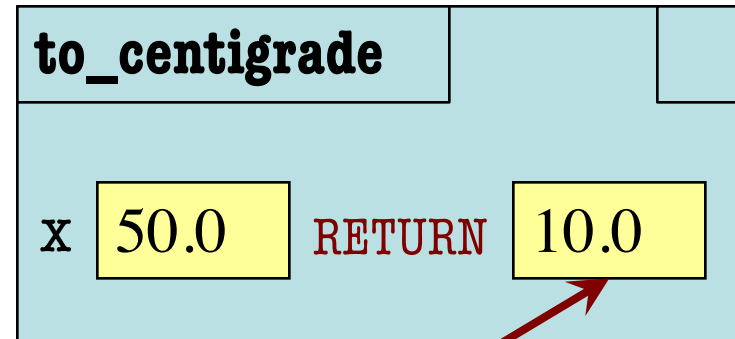
```
def to_centigrade(x):  
1 | return 5*(x-32)/9.0
```


Example: to_centigrade(50.0)

1. Draw a frame for the call
2. Assign the argument value to the parameter (in frame)
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```
def to_centigrade(x):  
1 | return 5*(x-32)/9.0
```

Executing the
return statement



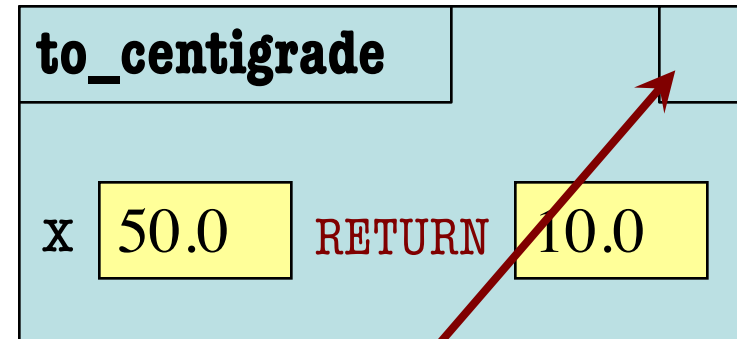
Return statement creates a
special variable for result

Example: to_centigrade(50.0)

1. Draw a frame for the call
2. Assign the argument value to the parameter (in frame)
3. Execute the function body
 - Look for variables in the frame
 - If not there, look for global variables with that name
4. Erase the frame for the call

```
def to_centigrade(x):  
1 | return 5*(x-32)/9.0
```

Executing the
return statement



The return terminates;
no next line to execute

Example: to_centigrade(50.0)

1. Draw a frame for the call
2. Assign the argument value to the parameter (in frame)
3. Execute the function body
 - Look for variables in the frame
 - If not there, look for global variables with that name
4. Erase the frame for the call

ERASE WHOLE FRAME

```
1 def to_centigrade(x):  
  | return 5*(x-32)/9.0
```

But don't actually
erase on an exam

Call Frames vs. Global Variables

The specification is a **lie**:

```
def swap(a,b):  
    """Swap global a & b"""  
1    tmp = a  
2    a = b  
3    b = tmp
```

```
>>> a = 1
```

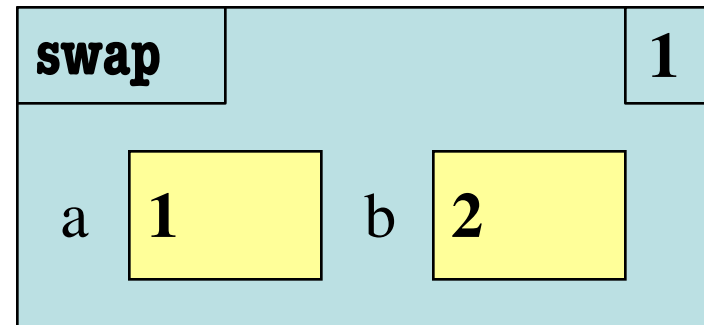
```
>>> b = 2
```

```
>>> swap(a,b)
```

Global Variables

a **1** b **2**

Call Frame



Call Frames vs. Global Variables

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```
def swap(a,b):  
    """Swap global a & b"""  
1   tmp = a  
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```

```
>>> a = 1
```

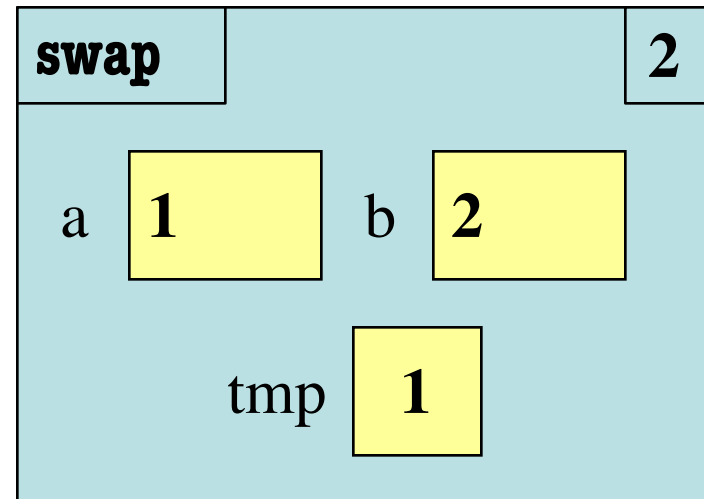
```
>>> b = 2
```

```
>>> swap(a,b)
```

Global Variables

a **1** b **2**

Call Frame



Call Frames vs. Global Variables

The specification is a **lie**:

```
def swap(a,b):  
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1   tmp = a  
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```

```
>>> a = 1
```

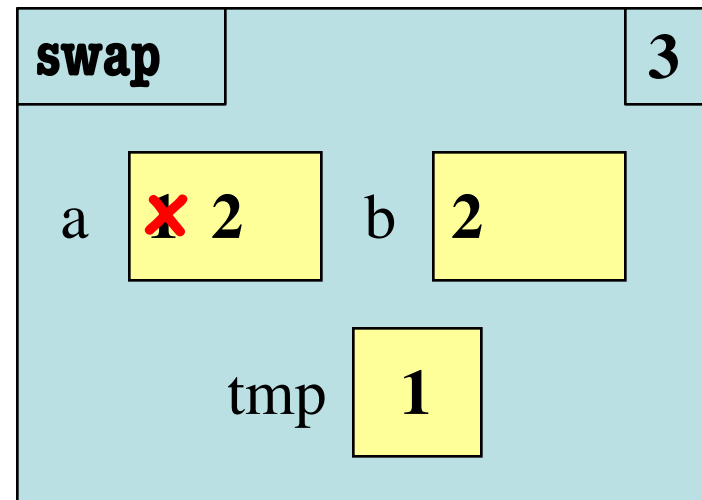
```
>>> b = 2
```

```
>>> swap(a,b)
```

Global Variables

a **1** b **2**

Call Frame



Call Frames vs. Global Variables

The specification is a **lie**:

```
def swap(a,b):  
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1   tmp = a  
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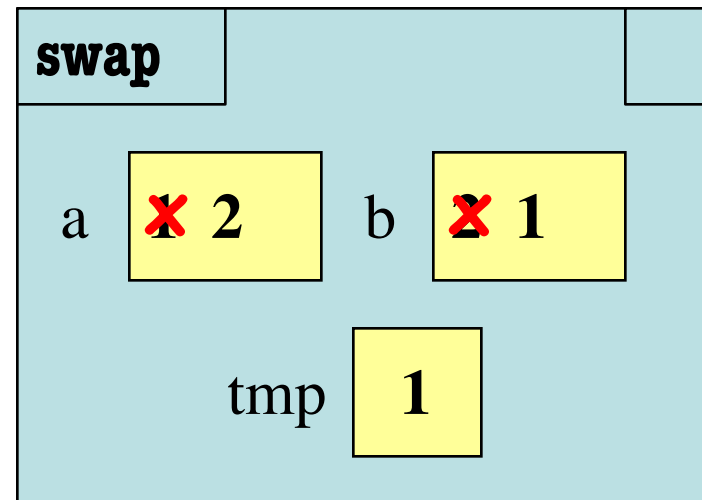
```
>>> b = 2
```

```
>>> swap(a,b)
```

Global Variables

a **1** b **2**

Call Frame



Call Frames vs. Global Variables

The specification is a **lie**:

```
def swap(a,b):  
    """Swap global a & b"""  
1   tmp = a  
2   a = b  
3   b = tmp
```

```
>>> a = 1
```

```
>>> b = 2
```

```
>>> swap(a,b)
```

Global Variables

a 1 b 2

Call Frame

ERASE THE FRAME

Function Access to Global Space

- All function definitions are in some module
- Call can access global space for **that module**
 - `math.cos`: global for `math`
 - `temperature.to_centigrade` uses global for `temperature`
- But **cannot** change values
 - Assignment to a global makes a new local variable!
 - Why we limit to constants

Global Space
(for `globals.py`) a 4

get_a 1

```
# globals.py
"""Show how globals work"""
a = 4 # global space

def get_a():
    |     return a # returns global
```

Function Access to Global Space

- All function definitions are in some module
- Call can access global space for **that module**
 - `math.cos`: global for `math`
 - `temperature.to_centrigrade` uses global for `temperature`
- But **cannot** change values
 - Assignment to a global makes a new local variable!
 - Why we limit to constants

Global Space
(for `globals.py`) a 4

change_a

a 3.5

```
# globals.py
"""Show how globals work"""
a = 4 # global space
def change_a():
    a = 3.5 # local variable
    return a
```

Exercise Time

Function Definition

```
def foo(a,b):
```

```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1 x = a
```

```
2 y = b
```

```
3 return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

What does the
frame look like
at the **start**?

Which One is Closest to Your Answer?

A:

foo		0	
a	3	b	4

B:

foo		1	
a	3	b	4


C:

foo		1	
a	3	b	4
x	3		

D:

foo		1	
a	3	b	4
x		y	

Which One is Closest to Your Answer?

A:	<table border="1"><tr><td>foo</td><td></td><td>0</td></tr><tr><td>a</td><td>3</td><td>b</td><td>4</td></tr></table>	foo		0	a	3	b	4	B:	<table border="1"><tr><td>foo</td><td></td><td>1</td></tr><tr><td>a</td><td>3</td><td>b</td><td>4</td></tr></table>	foo		1	a	3	b	4				
foo		0																			
a	3	b	4																		
foo		1																			
a	3	b	4																		
E: 																					
C:	<table border="1"><tr><td>foo</td><td></td><td></td></tr><tr><td>a</td><td>3</td><td></td></tr><tr><td>x</td><td>3</td><td></td></tr></table>	foo			a	3		x	3		<table border="1"><tr><td></td><td></td><td>1</td></tr><tr><td>b</td><td>4</td><td></td></tr><tr><td>x</td><td></td><td>y</td><td></td></tr></table>			1	b	4		x		y	
foo																					
a	3																				
x	3																				
		1																			
b	4																				
x		y																			

Exercise Time

Function Definition

```
def foo(a,b):
```

```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1 x = a
```

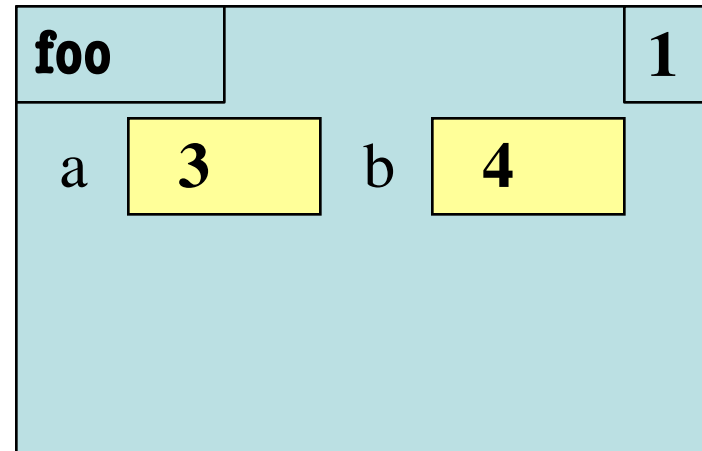
```
2 y = b
```

```
3 return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

B:



Exercise Time

Function Definition

```
def foo(a,b):
```

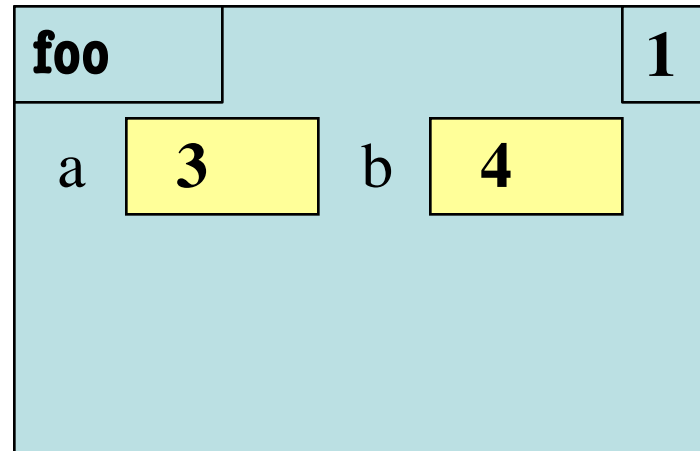
```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1 x = a  
2 y = b  
3 return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

B:



What is the **next step**?

Which One is Closest to Your Answer?

A:

foo						2
a	3	b	4			

B:

foo						1
a	3	b	4			
x	3					

C:

foo						2
a	3	b	4			
x	3					

D:

foo						2
a	3	b	4			
x	3	y				

Exercise Time

Function Definition

```
def foo(a,b):
```

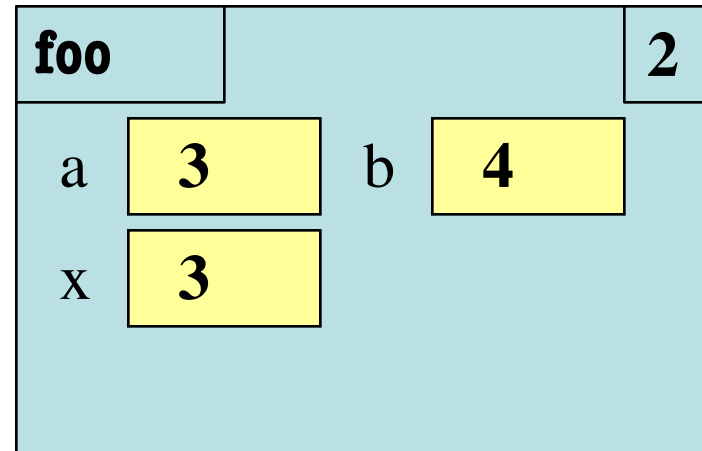
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    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1  x = a  
2  y = b  
3  return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

C:



Exercise Time

Function Definition

```
def foo(a,b):
```

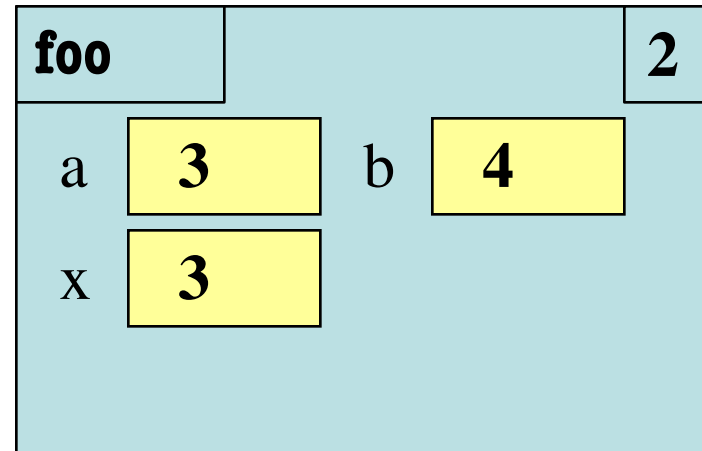
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Function Call

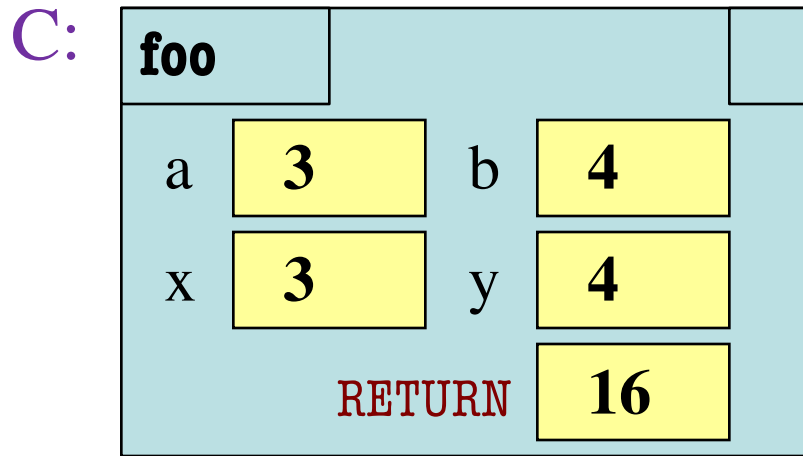
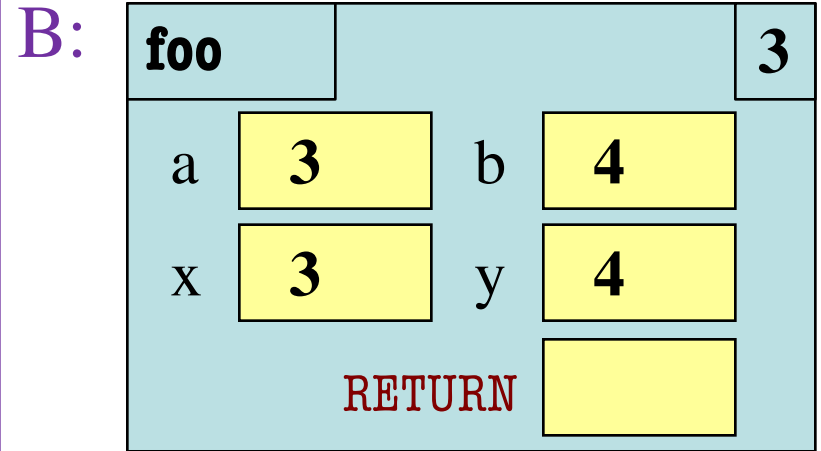
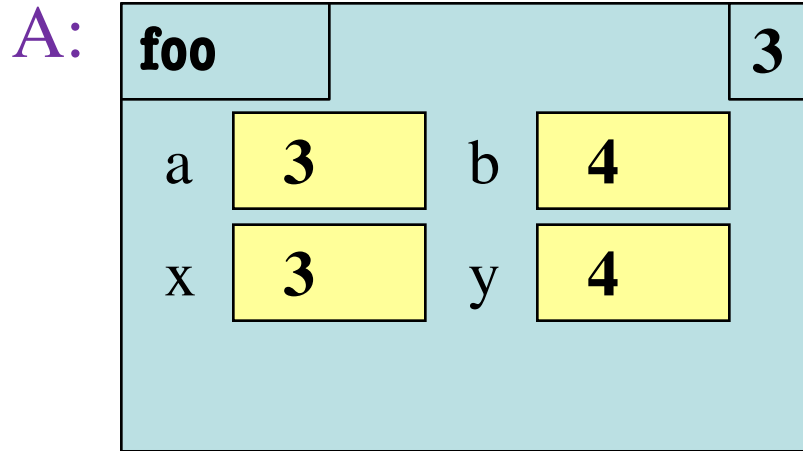
```
>>> x = foo(3,4)
```

C:



What is the **next step**?

Which One is Closest to Your Answer?



Exercise Time

Function Definition

```
def foo(a,b):
```

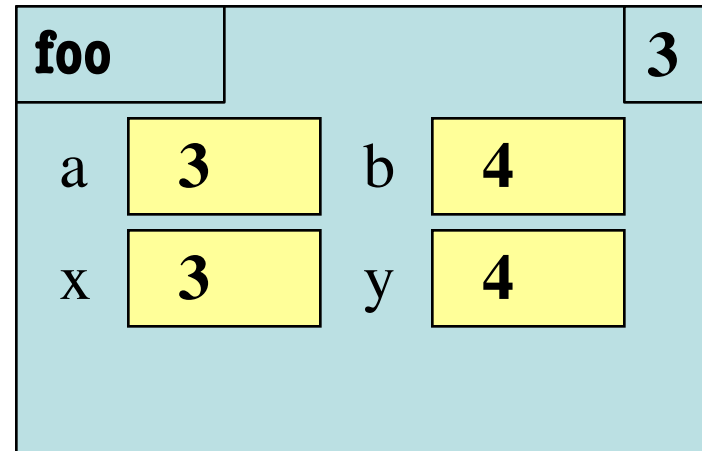
```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1  x = a  
2  y = b  
3  return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

A:



Exercise Time

Function Definition

```
def foo(a,b):
```

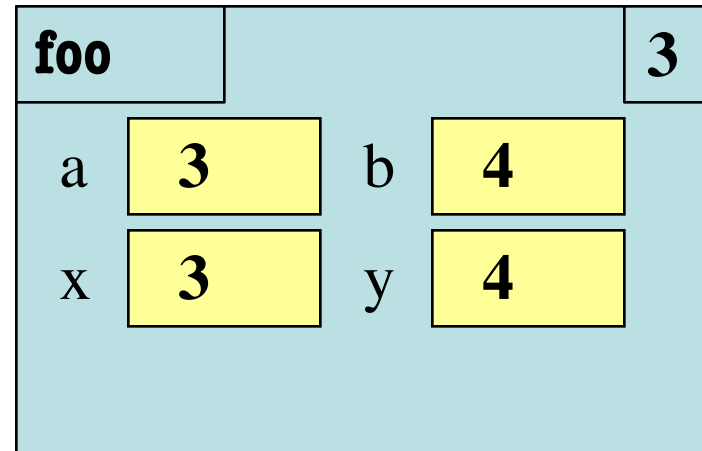
```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1  x = a  
2  y = b  
3  return x*y+y
```

Function Call

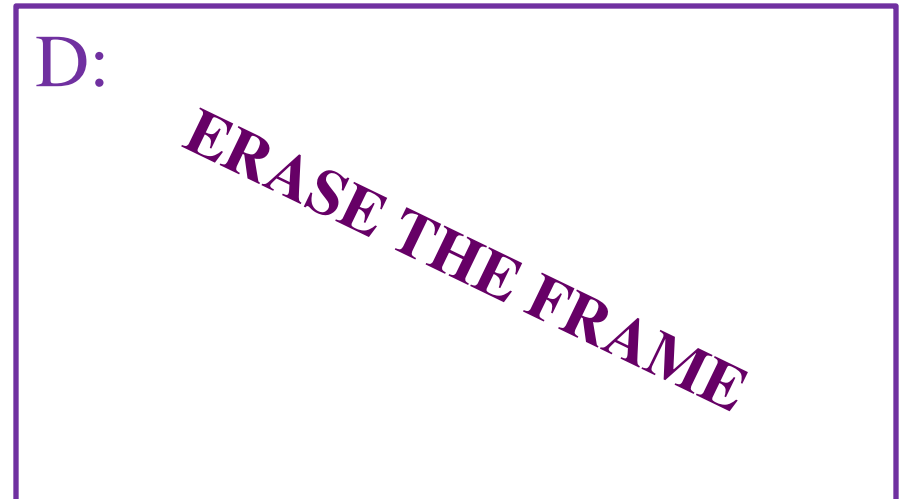
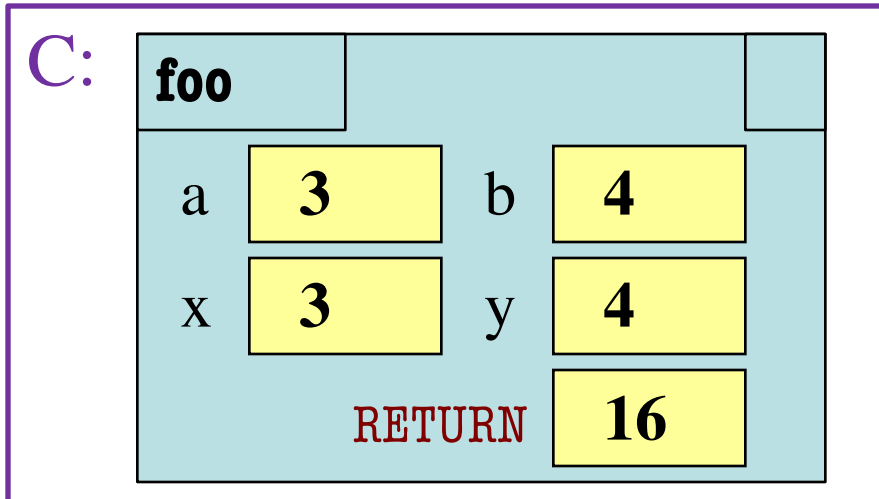
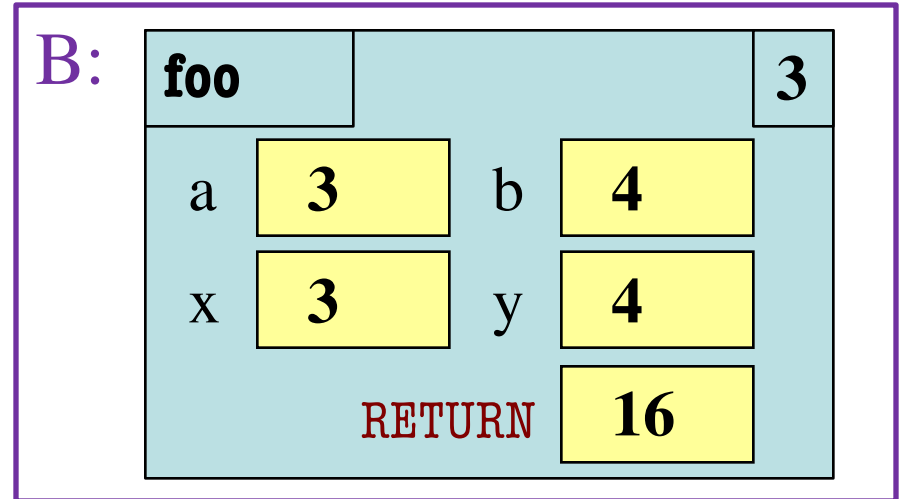
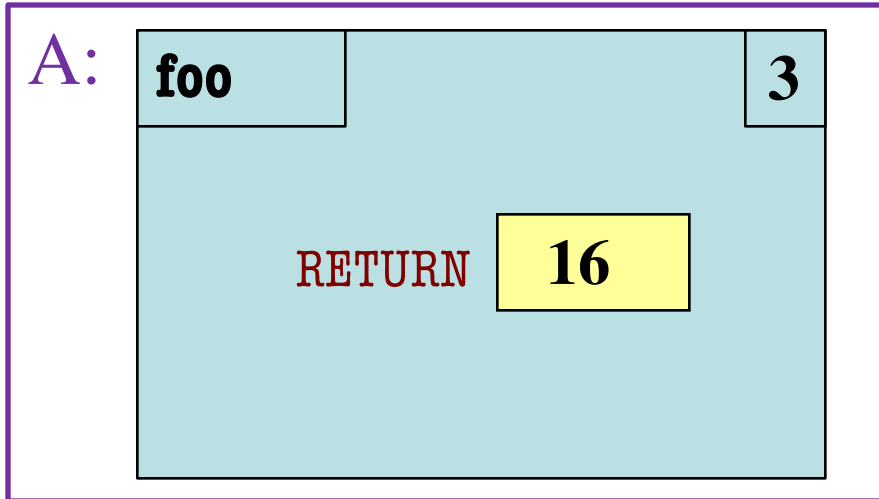
```
>>> x = foo(3,4)
```

A:



What is the **next step**?

Which One is Closest to Your Answer?



Exercise Time

Function Definition

```
def foo(a,b):
```

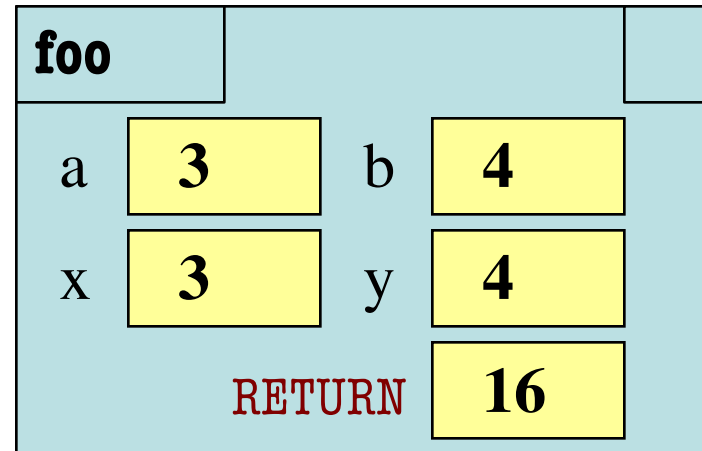
```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1  x = a  
2  y = b  
3  return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

C:



Exercise Time

Function Definition

```
def foo(a,b):
```

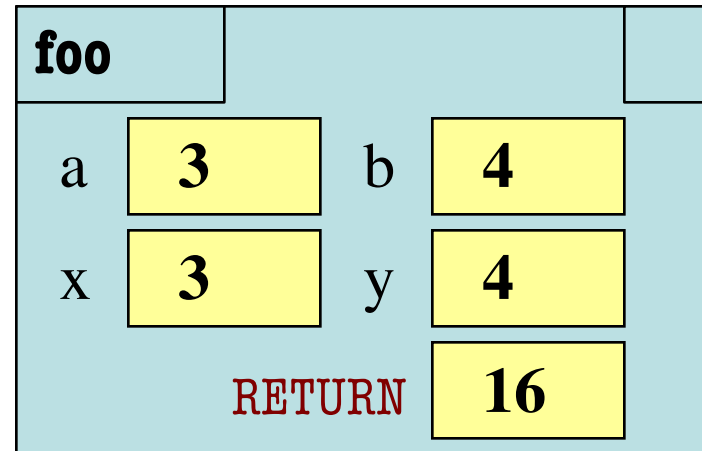
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    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1 x = a  
2 y = b  
3 return x*y+y
```

Function Call

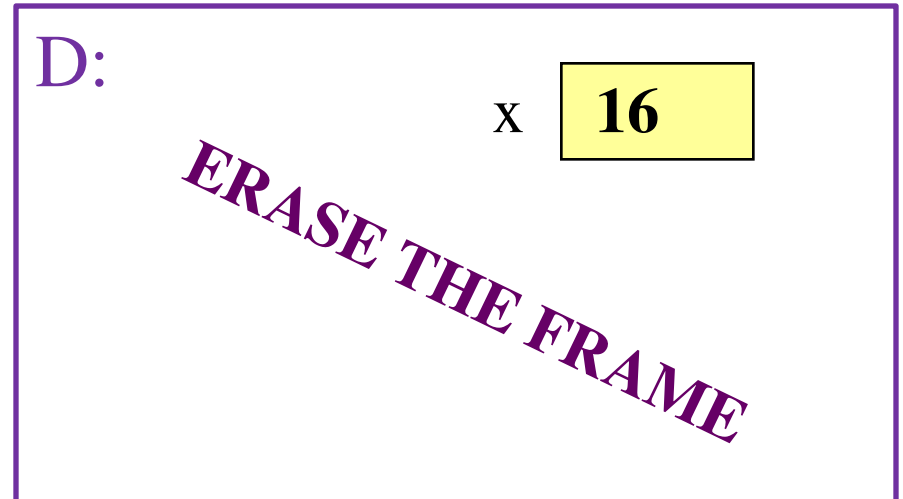
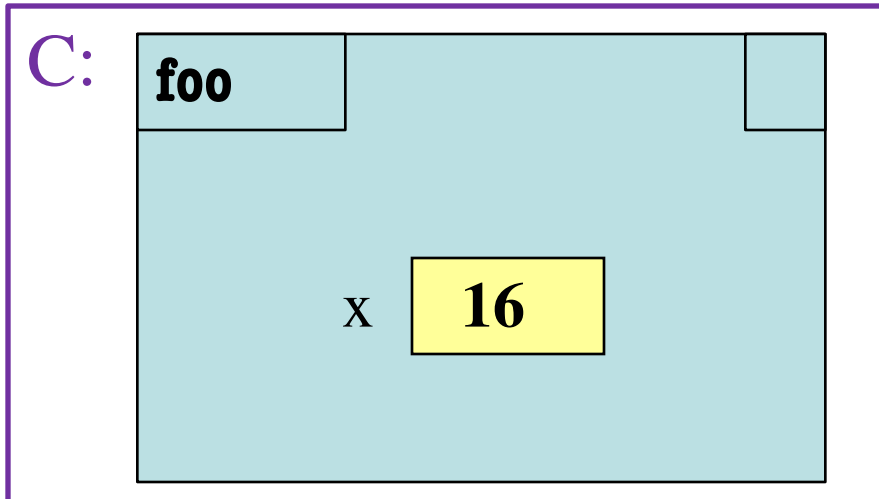
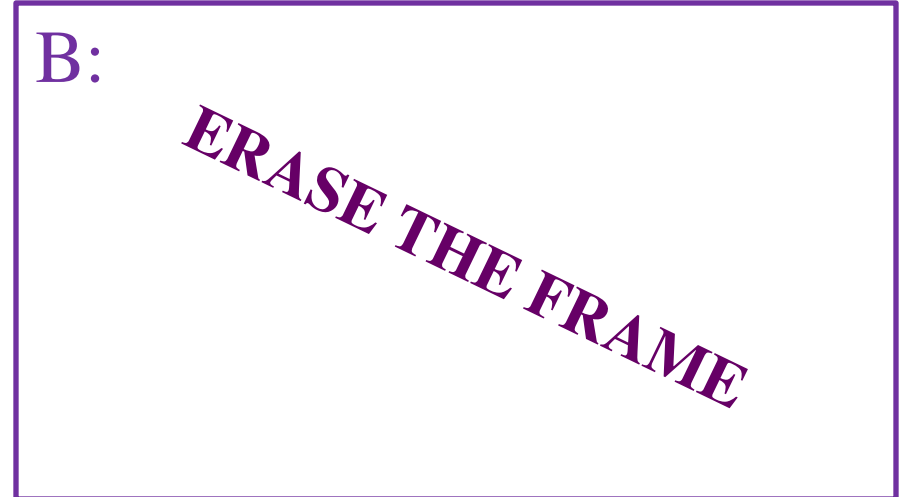
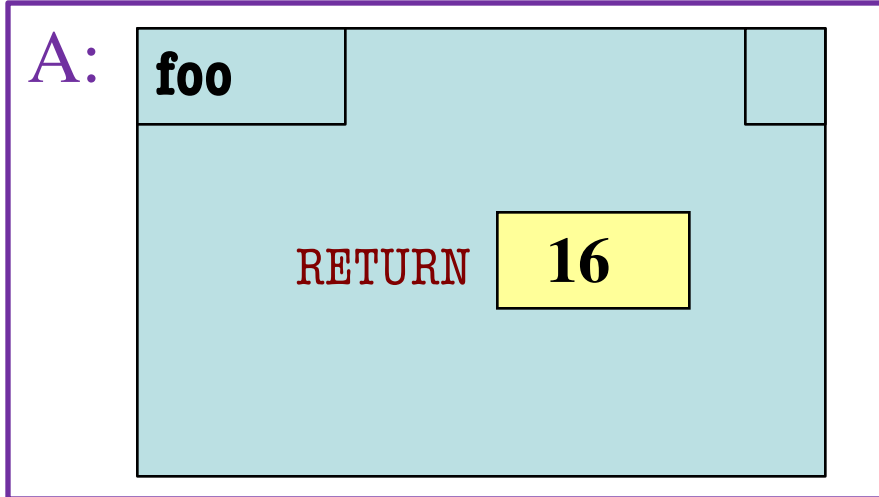
```
>>> x = foo(3,4)
```

C:



What is the **next step**?

Which One is Closest to Your Answer?



Exercise Time

Function Definition

```
def foo(a,b):
```

```
    """Return something  
    Param x: a number  
    Param y: a number"""
```

```
1  x = a  
2  y = b  
3  return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

D:

x

16

ERASE THE FRAME

Exercise Time

Function Definition

```
def foo(a,b):  
    """Return something  
    Param x: a number  
    Param y: a number"""  
1   x = a  
2   y = b  
3   return x*y+y
```

Function Call

```
>>> x = foo(3,4)
```

D:

Variable in
global space

x

16

ERASE THE FRAME

Visualizing Frames: The Python Tutor

```
→ 1 def max(x,y):  
  2     if x > y:  
  3         return x  
  4     return y  
  5  
  6 a = 1  
  7 b = 2  
→ 8 max(a,b)
```

[Edit code](#)

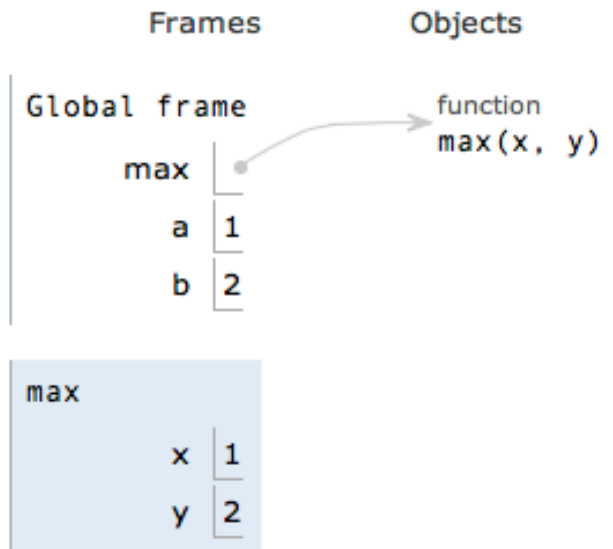
<< First

< Back

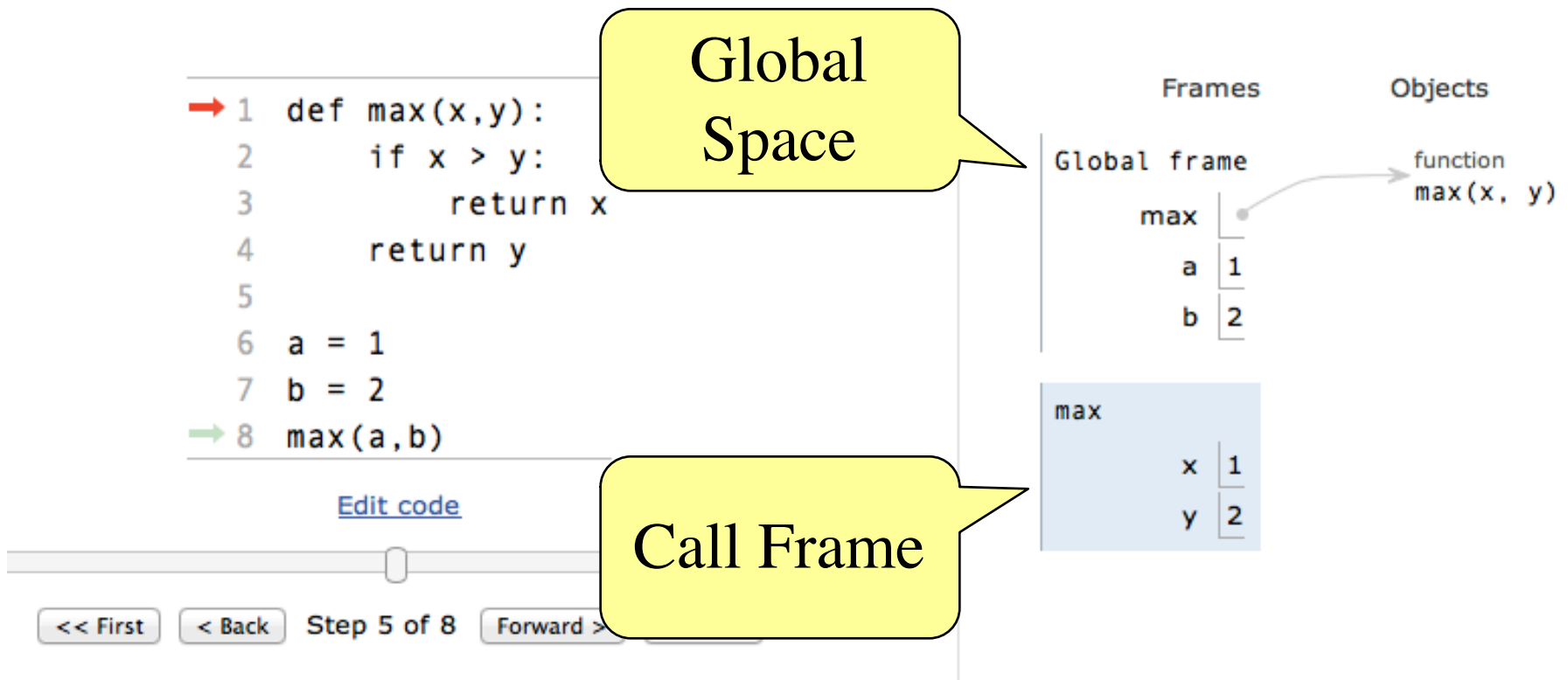
Step 5 of 8

Forward >

Last >>



Visualizing Frames: The Python Tutor



Visualizing Frames: The Python Tutor

The image shows a Python Tutor interface with the following code:

```
1 def max(x,y):  
2     if x > y:  
3         return x  
4     return y  
5  
6 a = 1  
7 b = 2  
8 max(a,b)
```

Annotations and frames:

- Global Space:** A yellow callout points to the code, indicating the global namespace.
- Call Frame:** A yellow callout points to the function call `max(a,b)` on line 8.
- Global Frame:** A table showing the global namespace:

max	function max(x, y)
a	1
b	2
- Call Frame:** A table showing the local namespace for the `max` function:

x	1
y	2
- Green Callout:** A green callout points to the Global Frame with the text "Variables from second lecture go in here".

Navigation controls at the bottom include: `<< First`, `< Back`, `Step 5 of 8`, `Forward >`.

Visualizing Frames: The Python Tutor

```
→ 1 def max(x,y):  
  2     if x > y:  
  3         return x  
  4     return y  
  5  
  6 a = 1  
  7 b = 2  
→ 8 max(a,b)
```

[Edit code](#)

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Step 5 of 8

Forward >

Last >>

Frames Objects

Global fr
max
a
b

max

x	1
y	2

Missing line numbers!

Visualizing Frames: The Python Tutor

Line number
marked here
(sort-of)

```
→ 1 def max(x,y):  
  2     if x > y:  
  3         return x  
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  6 a = 1  
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→ 8 max(a,b)
```

[Edit code](#)

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Step 5 of 8

Forward >

Last >>

Frames

Objects

Global fr

max

Missing line
numbers!

a

b

max

x

1

y

2

Next Time: Concrete Examples