CS 4783/5783

Differential Privacy and Machine Learning

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  - Medical records of patients (Eg. learn how much smoking affects chances of getting cancer)
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  - Genetic information (Eg. to learn genetic predispositions)

AOL Data Release

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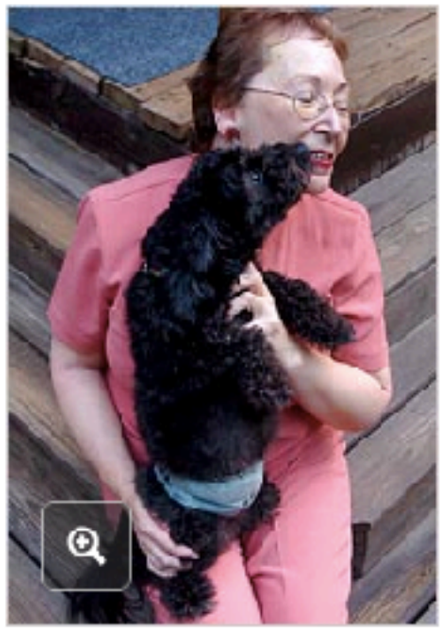
TECHNOLOGY

A Face Is Exposed for AOL Searcher No. 4417749

By **MICHAEL BARBARO** and **TOM ZELLER Jr.** AUG. 9, 2006

Buried in a list of 20 million Web search queries collected by AOL and recently released on the Internet is user No. 4417749. The number was assigned by the company to protect the searcher's anonymity, but it was not much of a shield.

No. 4417749 conducted hundreds of searches over a three-month period on topics ranging from "numb fingers" to "60 single men" to "dog that urinates on everything."



Thelma Arnold's identity was betrayed by AOL records of her Web searches, like ones for her dog, Dudley, who clearly has a problem.

Erik S. Lesser for The New York Times

RYAN SINGEL SECURITY 03.12.10 02:48 PM

NETFLIX CANCELS RECOMMENDATION CONTEST AFTER PRIVACY LAWSUIT

Netflix is canceling its second $1 million Netflix Prize to settle a legal challenge that it breached customer privacy as part of the first contest's race for a better movie-

Netflix Challenge [NS'08]

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NETFLIX

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	Movies				
User 1		5		1	
User 2	1			1	1
User 3		4			

- Given ratings by users for some movies

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- How?!!!

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- Only a very small overlap with IMDB was required
- You pretty much get the persons viewing record from / Netflix without consent

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  - Or classifier learnt from data?

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What is the problem?

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Say “Fill Nates” from WA was in the dataset, and is very very rich.

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- Building classifier and releasing only the classifier
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  - Say we have classifier from two or more counties/hospital, one of them has “Fill Nates”
  - Say we use regression for learning the classifier
  - By looking at weight put on income column of dataset, we can infer if “Fill Nates” was part of study and which hospital

Defining Privacy

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Dataset +

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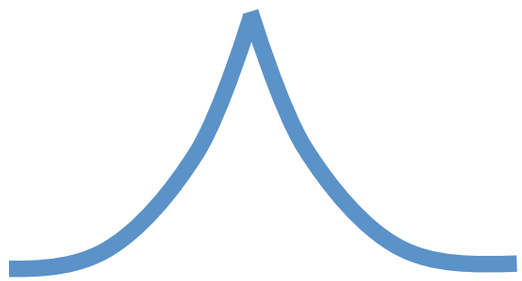
Learning Algorithm



Distribution of outcome

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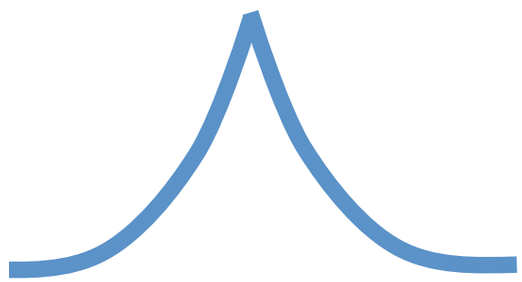

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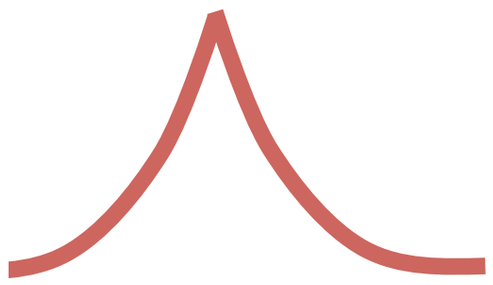

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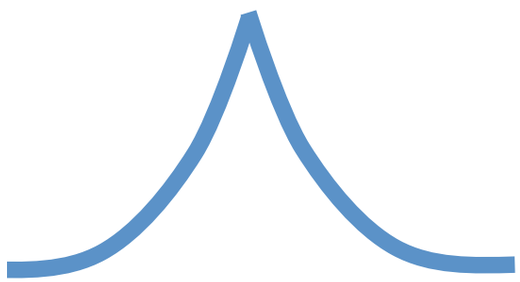

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Similar

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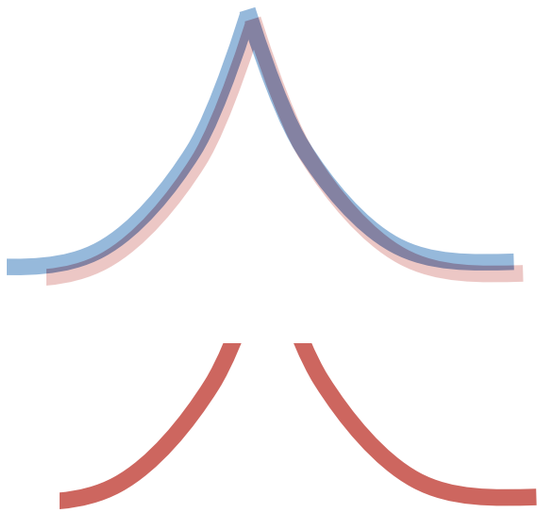

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- δ=0 is called pure differential privacy

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≀≀

1 (for small ϵ)

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- Hence cannot be differentially private

Obtaining Differential Privacy

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- More privacy we want the more noise we add

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- Add noise to it M + 2 max_income Laplace(0,1)/ ϵ

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$$\leq e^{\epsilon}$$

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Hence

$$P(A(S) \in C) = \int_C p_{A(S)}(x)dx$$

$$\leq e^{\epsilon} \int_C p_{A(S')}(x)dx$$

$$= e^{\epsilon} P(A(S') \in C)$$

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- Can we do better?

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$$f(S) = \text{argmin}_{\mathbf{w}} \frac{1}{n} \sum_{t=1}^{n} \ell(\mathbf{w}^\top x_t, y_t) + \lambda \|\mathbf{w}\|^2$$

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- Add vector version of noise to f, only scale now is of order O(1/$\epsilon$$\lambda$n)

Differential Privacy in ML

- Differential private versions of PCA, clustering algorithms, deep learning etc. have been explored

- Nice properties of Differential Privacy
    - post processing is ok
    - compostability lemma

- Recently Differential Privacy was used as tool to allow statistically safe reuse of data